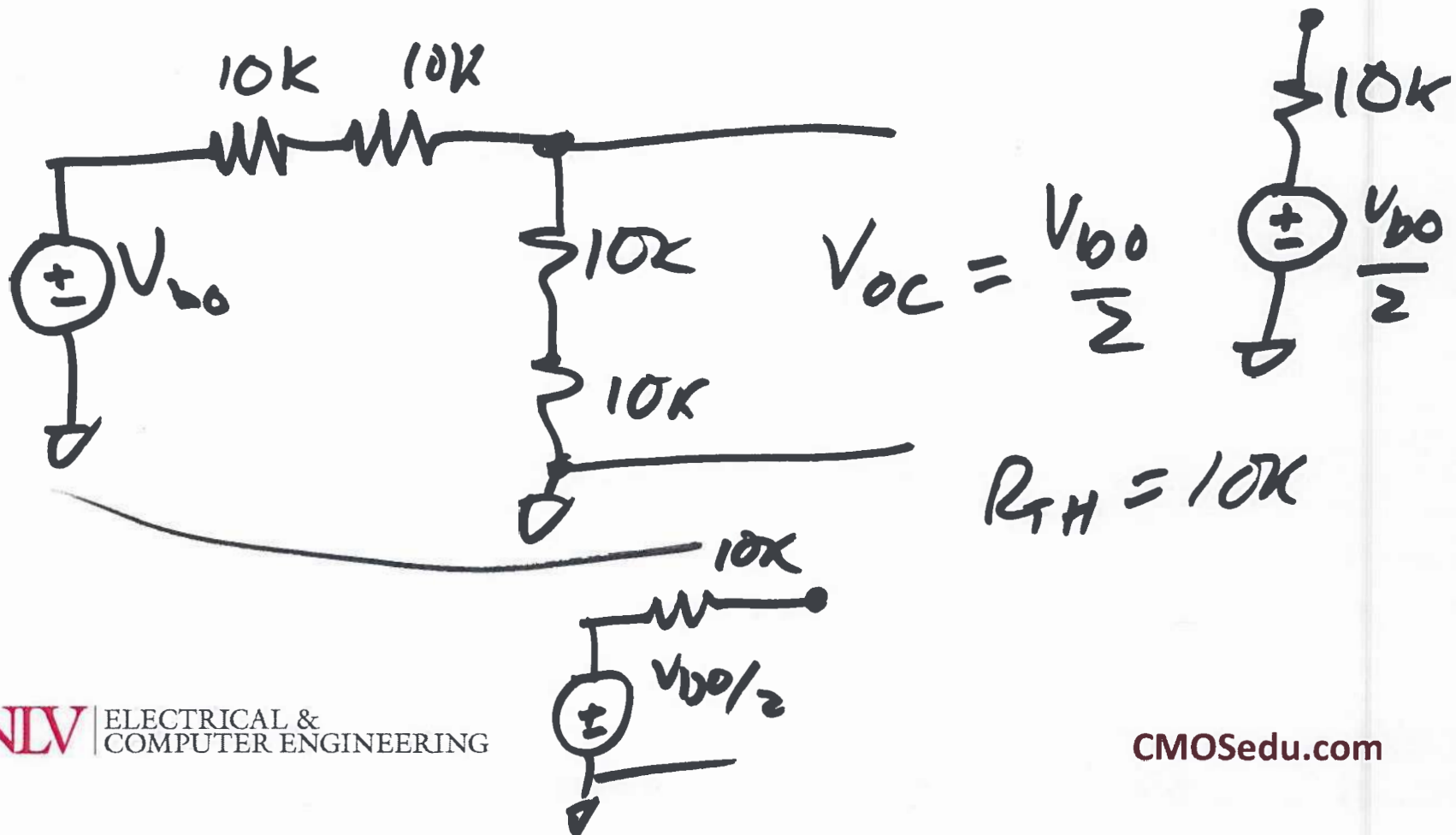


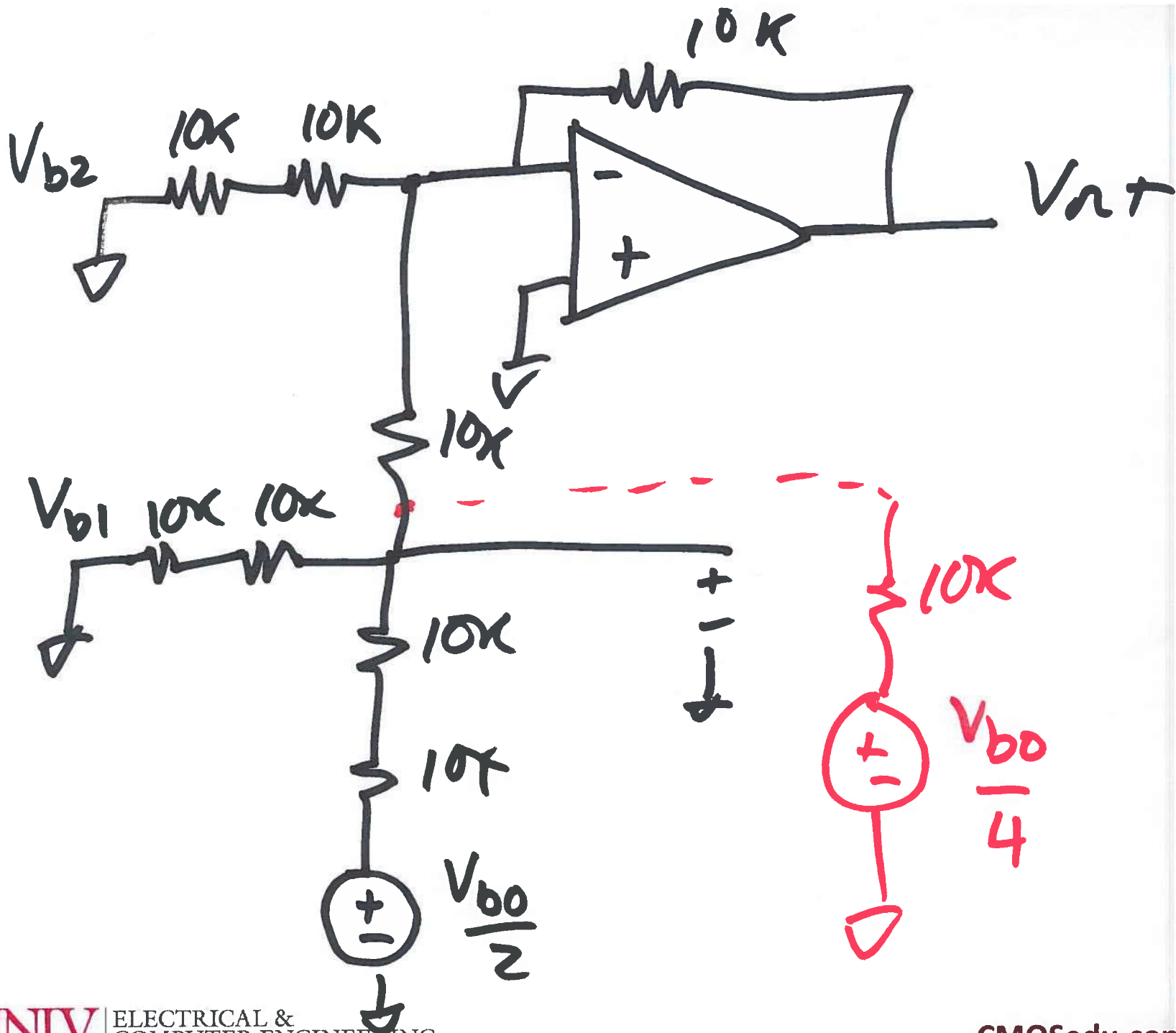
EE 220 Circuits 1

Lecture 16

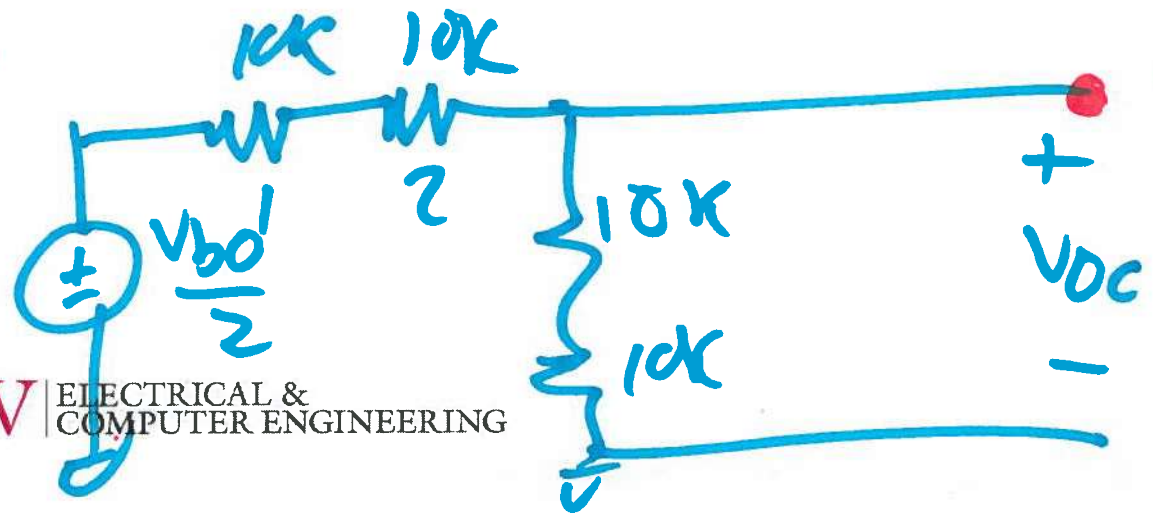
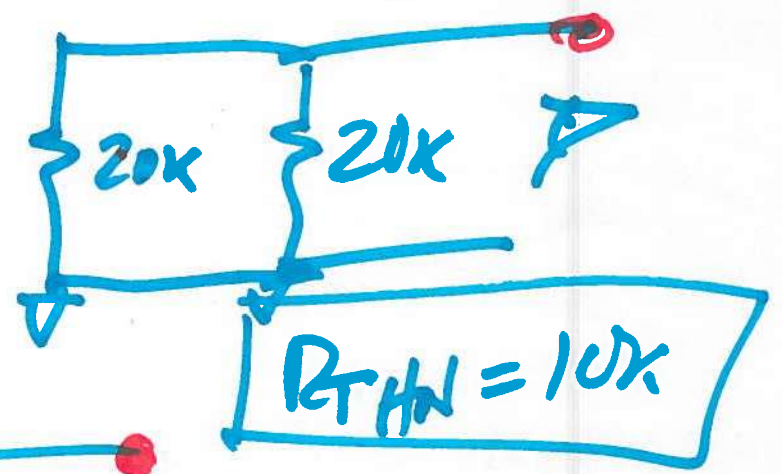
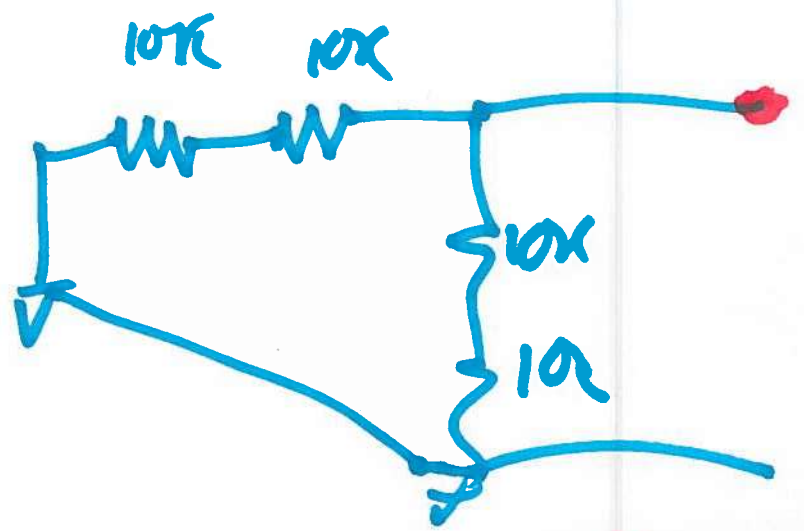
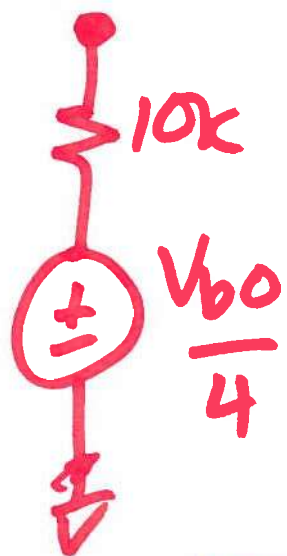
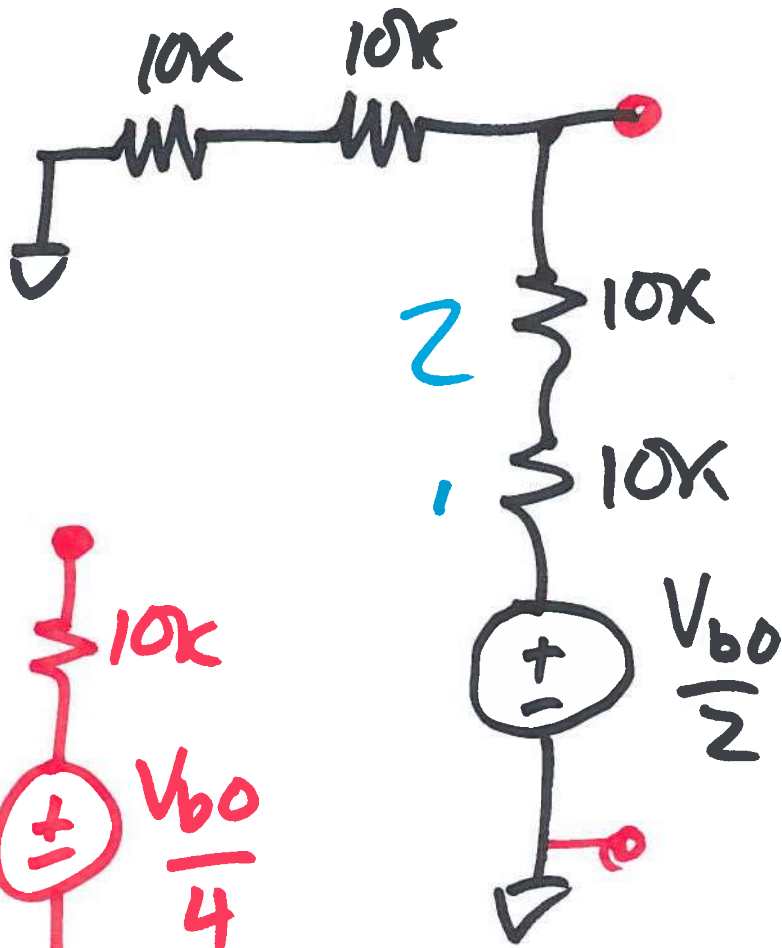
OCT. 22, 2018



1)

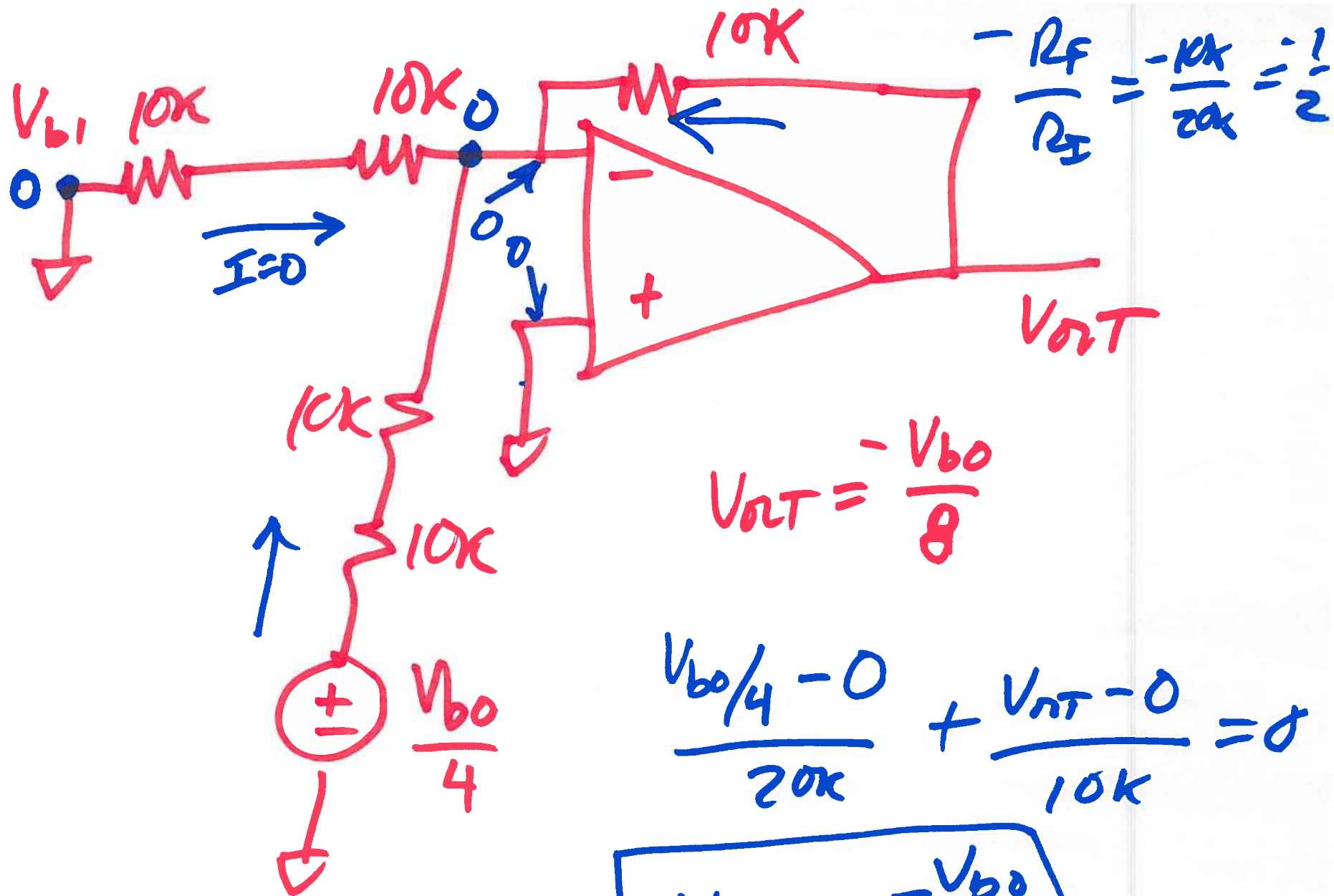


2)

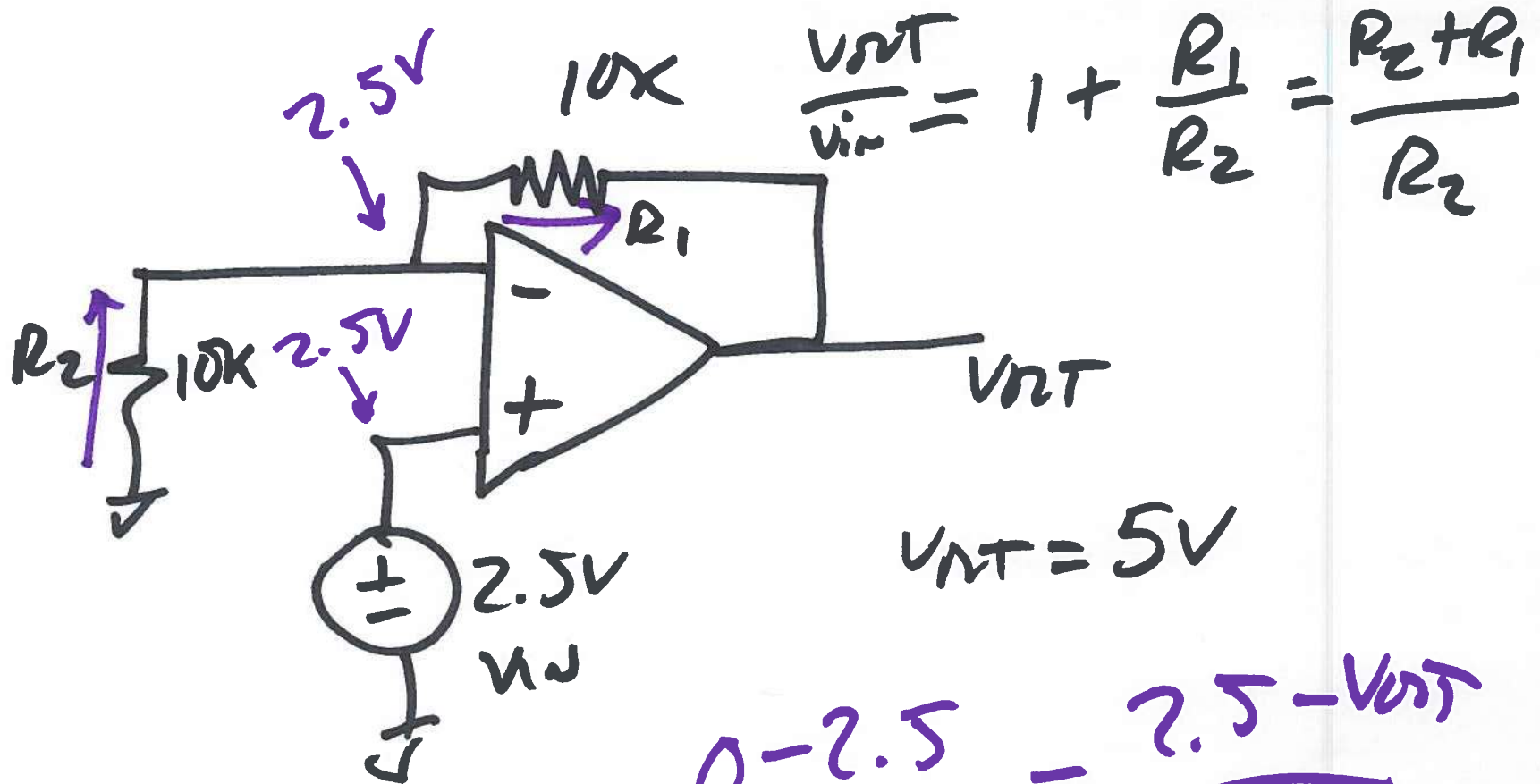


$$V_{DC} = \frac{V_{b0}}{4}$$

3)



4)



$$\frac{0 - 2.5}{10k} = \frac{2.5 - V_{out}}{10k}$$

$$V_{out} = 5V$$

5)

$$I = C \frac{dv}{dt}, \quad v = \frac{1}{C} \int i \cdot dt$$

$$\frac{0.54 \text{ A}}{1.54 \text{ s}} = \frac{1}{3}$$

$$i(t) = \frac{1}{3} \left(t - \frac{1}{2} \text{ s} \right)$$

$$\frac{1}{2} \text{ s} \leq t \leq 2 \text{ s}$$

$$i(t) = \frac{1}{3} t$$

$$v(t) = \frac{1}{C} \int_{\frac{1}{2}}^{2} \left(t - \frac{1}{2} \text{ s} \right) dt$$

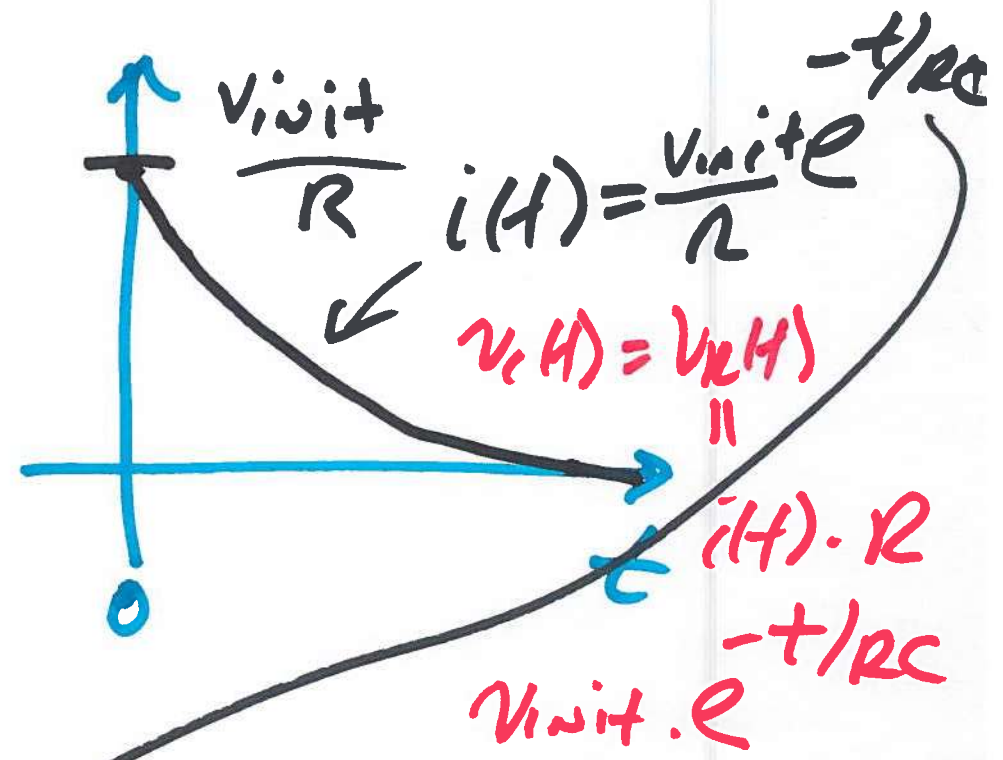
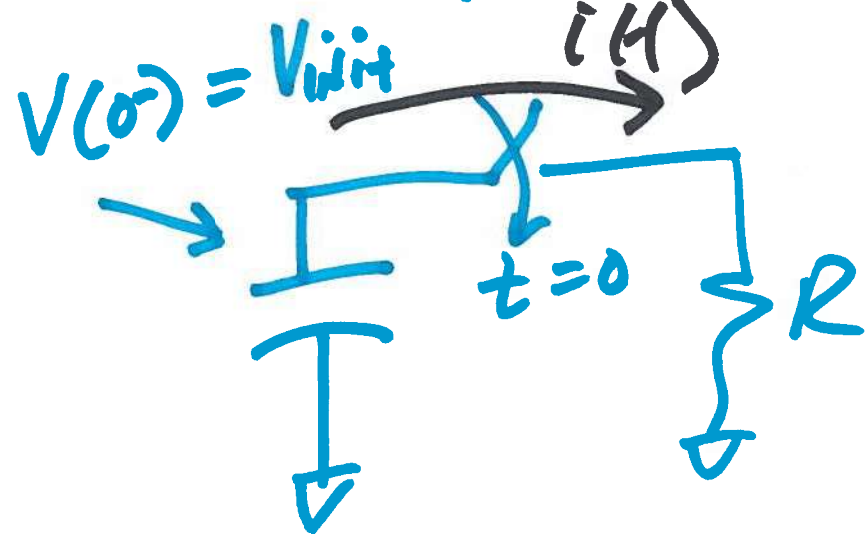
$$v(t) = \int_0^{1/2 \text{ s}} \frac{1}{3} t \cdot dt = \frac{1}{6} t^2 \Big|_0^{1/2 \text{ s}}$$

$$\frac{1}{10^8} \cdot \frac{1}{6} \cdot (1.5 \times 10^6)^2$$

$$\frac{2.25 \cdot 10^{-12}}{60 \cdot 10^{-12}}$$

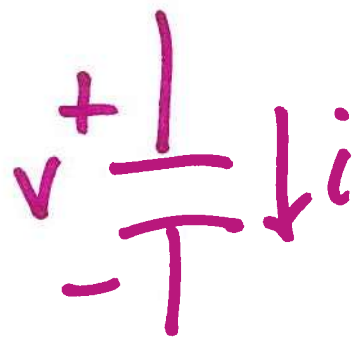
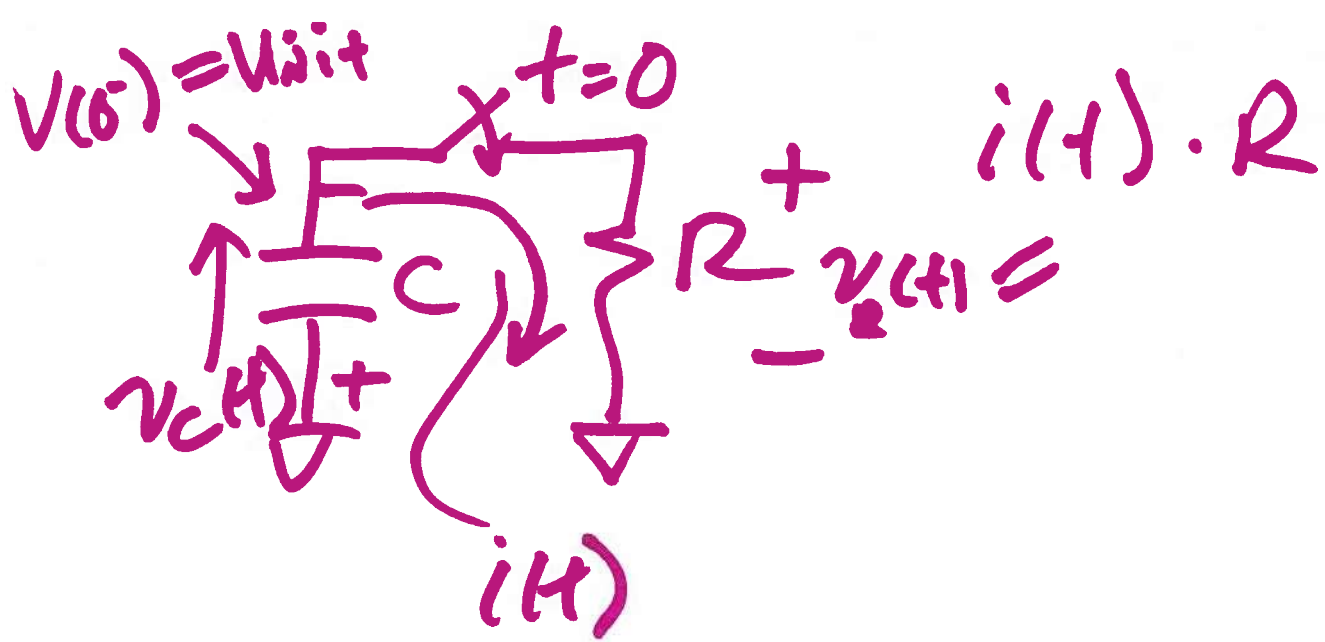
b)

first-order (NO source)



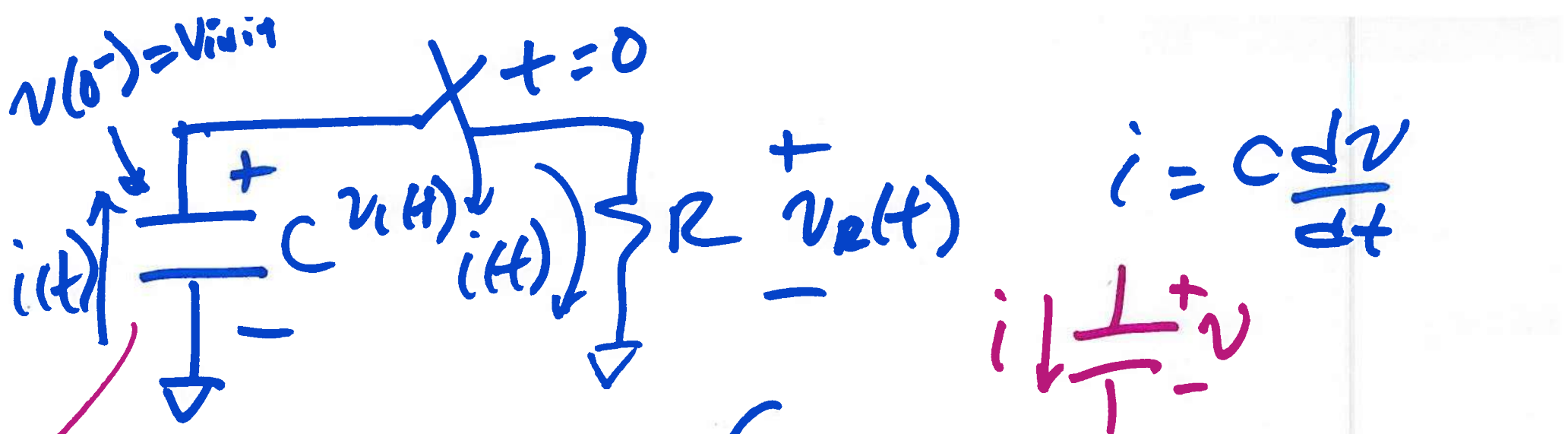
$\tau = RC = \text{time constant}$
 seconds

7)



$$i = C \frac{dv}{dt}$$

$$-v_c = \frac{1}{C} \int i \cdot dt = i(t) \cdot R = v_r$$



$$-i = C \frac{dv_c(t)}{dt} = \frac{1}{R} \int -i(t) dt = v_R(t) = i(t)R$$

$$v_c(t) = i(t) \cdot R = -RC \frac{dv_c(t)}{dt}$$

$$v_c(t) + RC \frac{dv_c(t)}{dt} = 0$$

a)

$$V_c + RC \frac{dV_c}{dt} = 0$$

SEPARATION

$$V_c = -RC \frac{dV_c}{dt}$$

$$-\frac{t}{RC} = \int_0^t \frac{1}{RC} dt = \int_{V_{init}}^{V_c(t)} \frac{dV_c}{V_c} = \ln V_c \Big|_{V_{init}}^{V_c(t)}$$

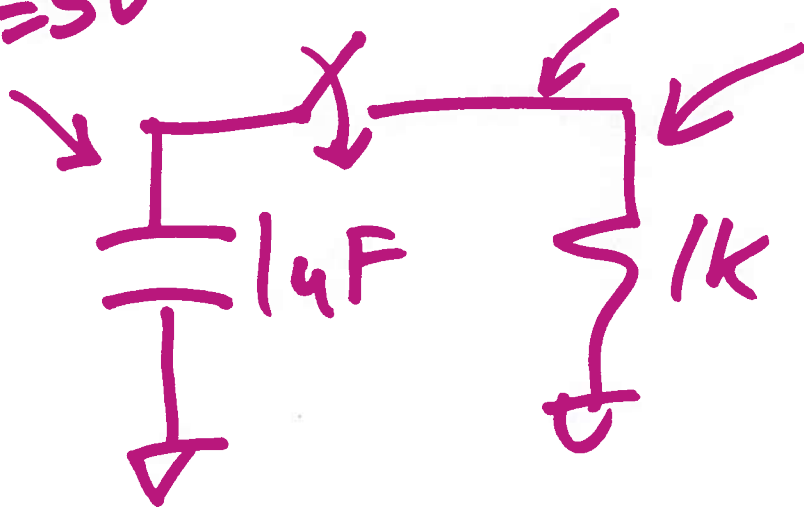
$$-\frac{t}{RC} = \ln \frac{V_c(t)}{V_{init}} = \ln V_c(t) - \ln V_{init}$$

$$V_c(t) = V_{init} e^{-t/RC}$$

$$\ln \frac{V_c}{V_{init}} = \ln A - \ln B = \ln \frac{A}{B}$$

10)

$$V(0) = 5V$$



$$V(t) = 5e^{-t/RC}$$
$$= 5e^{-t/1\mu s}$$

11)