

EE 320

2/5/14

Lecture 5

Ch. 2 solid-state  
Electronics

TABLE 2.1

Insulators

Semiconductors

Conductors

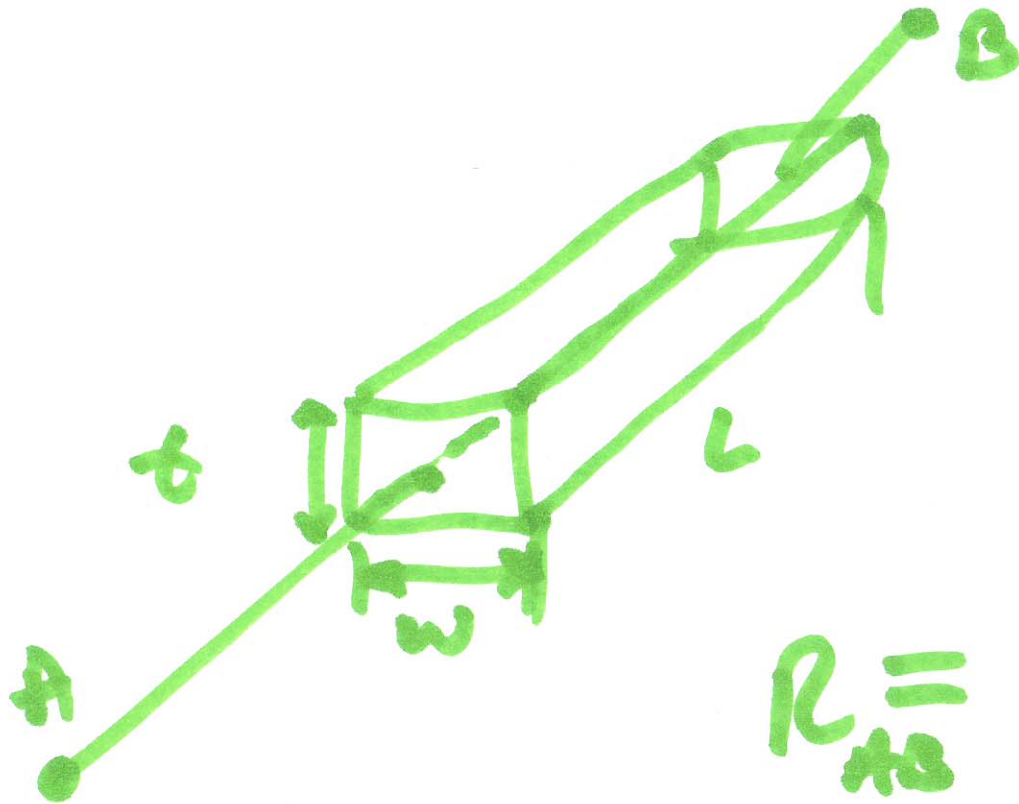
$$10^5 < \rho$$

$$10^{-3} < \rho < 10^5$$

$$\rho < 10^{-3} \Omega \cdot \text{cm}$$

$\Omega \cdot \text{cm}$   
↓ resistivity  
↑

1)



$$R_{AB} = \frac{L}{t} \cdot \frac{L}{w} \quad \Omega \cdot \text{cm}$$

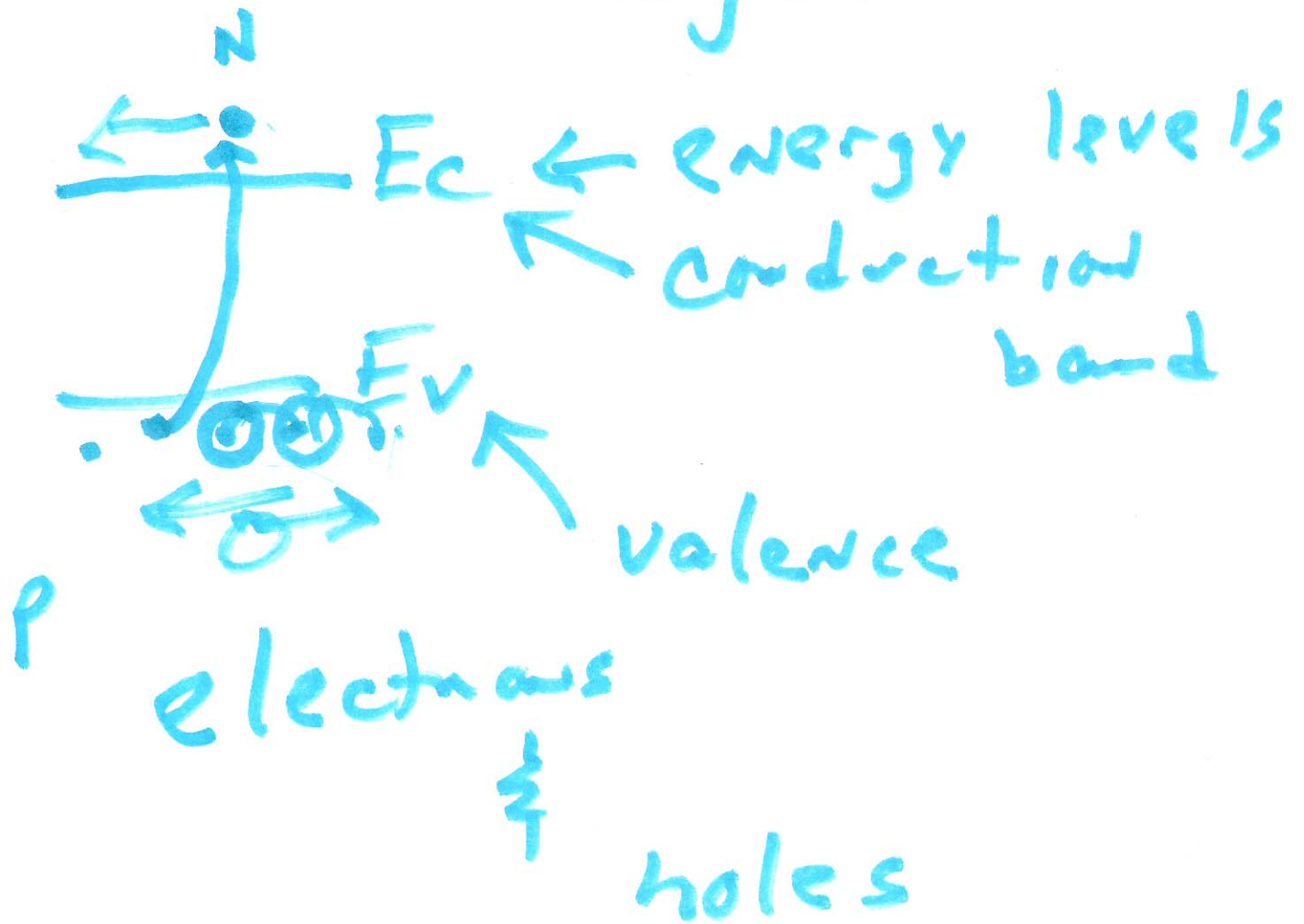
Conductors have few valence electrons

Si - 4 valence electrons

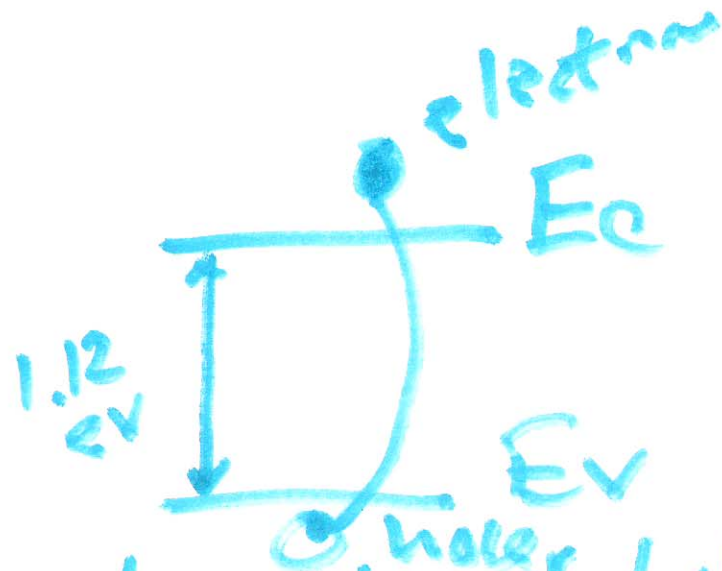
Cu - 10 valence  
Al - 3 valence

Silicon  $\rightarrow$  SiO<sub>2</sub> - 8e  
dioxide

Put Si atoms together



Si at room temp



$n_i$  = intrinsic  
# of carriers

$$= 6.73 \times 10^9$$

carriers  
 $\text{cm}^{-3}$

$p$  = density of holes  
holes/ $\text{cm}^3$

$n$  = electrons/ $\text{cm}^3$

# of Si atoms

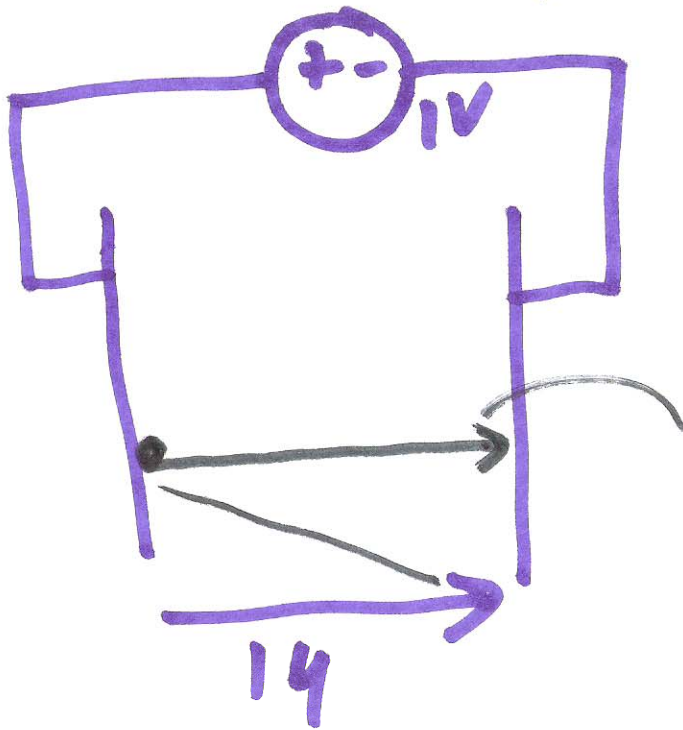
$$10^{22} \text{ Si atoms} \\ \text{cm}^{-3}$$

mobility

free carriers  $\left\{ \begin{array}{l} \text{electrons} \\ \text{holes} \end{array} \right.$

$$\mu \leftarrow = \frac{\text{Velocity, cm/s}}{\mathcal{E}, \text{Electric field V/cm}}$$

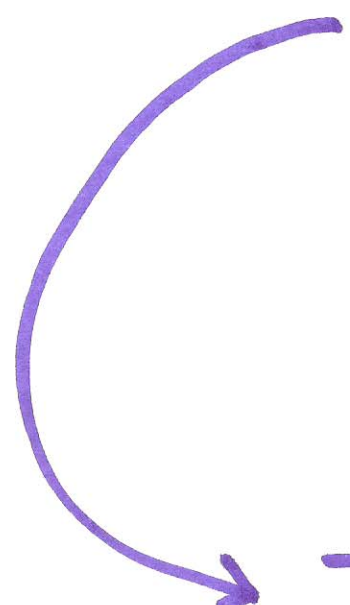
Mobility



$$\mu \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$\mathcal{E} = \frac{1\text{V}}{14} = 10^6 \frac{\text{V}}{\text{cm}}$$
$$= 10^4 \text{V/cm}$$

two types of currents  
drift  $\rightarrow$  has electric field  
diffusion  $\rightarrow$  no electric field



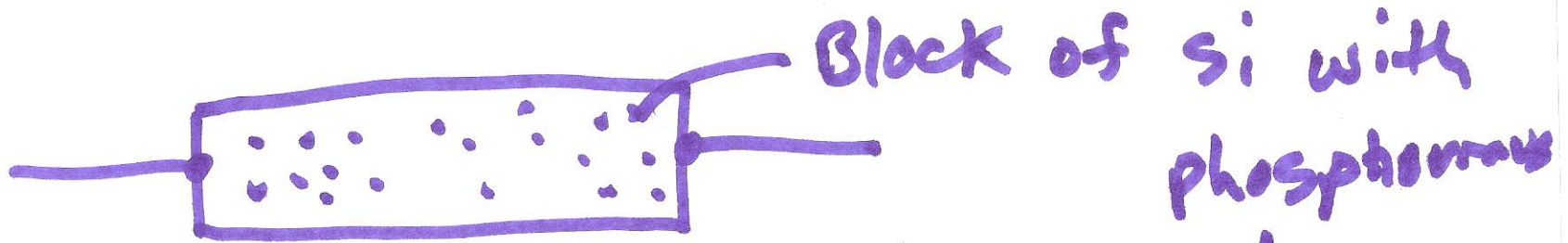
$J = Q \cdot v$

Current density  $A/cm^2$

Charge density  $C/cm^3$

velocity  $\frac{cm}{s}$

6)



$$N \approx N_D + N_i$$

$$10^{16} + 10^{10}$$

$$N \approx N_D$$

$N_D$   
 ↙  
 ↗ # of  
 donor  
 atoms  
 $\frac{10^{16} \text{ atoms}}{\text{cm}^3}$

7)

Dope Si with  $10^{15}$  Boron atoms

What type of s/c is it?

What is its carrier concentration?

p-type semiconductor

$$N_A = 10^{15} \frac{\text{atoms}}{\text{cm}^3} = \# \text{ of acceptor atoms}$$

$$p = N_A + n_i \approx N_A$$

$$p = 10^{15} \text{ holes/cm}^3$$

8)

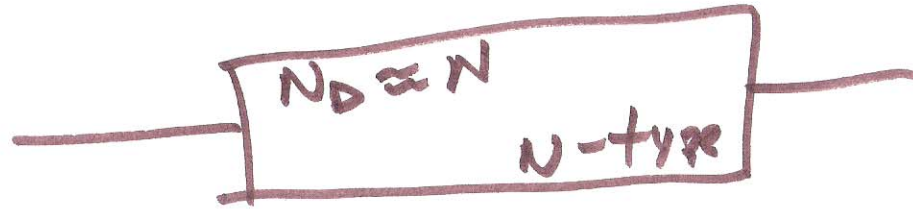


$p \cdot n = n_i^2$       Under equilibrium  
 N-type       $n = N_D + n_i \approx N_D$   
 MASS action Law       $p \approx \frac{n_i^2}{N_D}$

P-type       $p = N_A + n_i \approx N_A$   
                   $n \approx \frac{n_i^2}{N_A}$

# Drift Current

$$J = Q \cdot v$$



$$Q_n = q \cdot N \cdot \frac{\# \text{ of electrons}}{\text{cm}^3}$$

← electron charge

$$v = \mu_n \cdot E$$

← electron mobility

$$J_N = q \cdot N \cdot \mu_N \cdot E$$

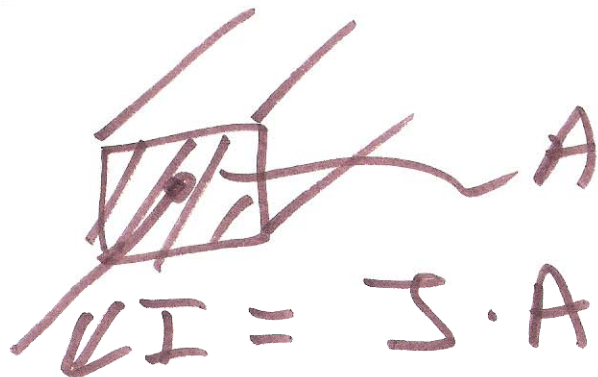
↑ electron movement in  
conduction  
band

$$J_P = q \cdot p \cdot \mu_P \cdot E$$

↑ hole movement in valence  
band

$$J_{\text{Total}} = J_N + J_P = q \cdot E (N \cdot \mu_N + P \cdot \mu_P)$$

↑  
 $E$  field



$$E = J \cdot \frac{V/cn \cdot \overbrace{A/cn^2} \cdot \overbrace{P = \pi \cdot cn}}{q \cdot (N \cdot q_n + P \cdot q_p)}$$

$$A = \frac{1}{P} \cdot q \cdot (N \cdot q_n + P \cdot q_p)$$

Si-doped with  $10^{16}$  phosphorus atoms  $\frac{\text{atoms}}{\text{cm}^3}$

$$t = 10 \mu\text{m} = 10 \cdot 10^{-6} \text{ m} = 10^{-5} \text{ m} = 0.001 \text{ cm}$$

$$w = 10 \mu\text{m} = 0.001 \text{ cm} = 0.00001 \text{ m}$$

$$L = 100 \mu\text{m} = 0.01 \text{ cm}, \mu_n = 600 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

Calculate  $N$

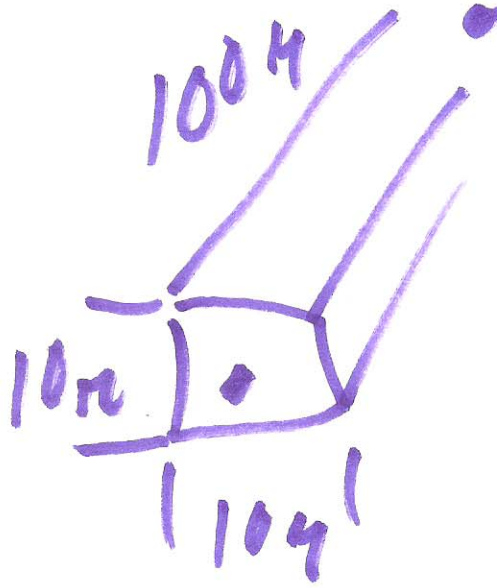
$$N = 10^{16} + 10^{10} \approx 10^{16} \frac{\text{electrons}}{\text{cm}^3} \quad N_i = 10^{10} \frac{\text{carriers}}{\text{cm}^3}$$

Calculate  $P$

$$P = \frac{N_i^2}{N} = \frac{10^{20}}{10^{16}} = 10^{24} \frac{\text{holes}}{\text{cm}^3}$$

10,000

13)



$$\rho = \frac{1}{q(N_M N + p \cdot 4p)} \approx \frac{1}{q N_M N}$$

$$= \frac{1}{1.6 \times 10^{-19} \frac{C}{e} \cdot \frac{10^{16} \frac{cm^{-3}}{cm^3} \cdot 600 \frac{cm^2}{V \cdot s}}{V \cdot s}}$$

$$= 1.04 \Omega \cdot cm$$

$$R = \rho \cdot \frac{L}{W \cdot t} = \frac{1.04 \cdot 0.01 cm}{0.001 \cdot 0.001}$$

$$R = 10.4 k\Omega$$

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Quiz do  
for Bonus

14)

$$2.10) \quad \mathcal{E} = 2,500 \text{ V/cm}$$

$$\mu_N = 700 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}, \quad \mu_P = 250 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$N = 10^{17} / \text{cm}^3 \quad P = 10^3 / \text{cm}^3$$

$$J_N = q \cdot N \cdot \mathcal{E} \cdot \mu_N$$

$$J_P = q \cdot P \cdot \mathcal{E} \cdot \mu_P$$

$$2.14) \quad \mu = \frac{v}{E} \rightarrow v = \frac{\mu}{E}$$

$$J_n = q_n \cdot \mu_n \cdot E$$

$$J_p = q \cdot p \cdot \mu_p \cdot E$$