

Density of Si (crystalline)  
 $\sim 10^{22} \frac{\text{atoms}}{\text{cm}^3}$

# Lecture 6 EE 320

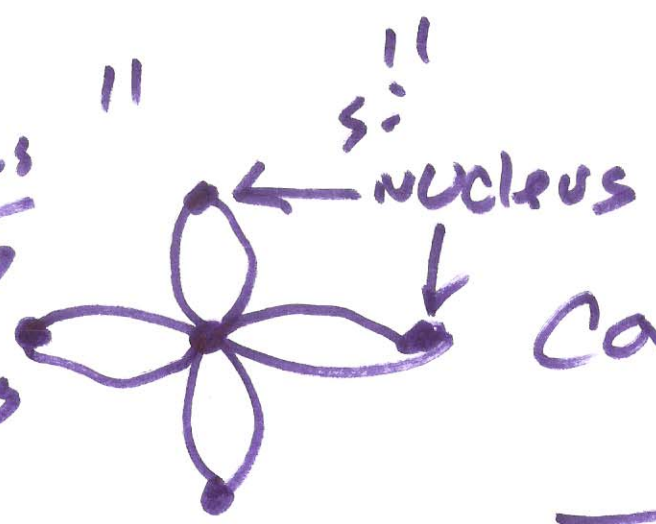
Feb. 10, 2014

How valence electrons in Si. (4)  
 " " P (5)  
 " " B (3)

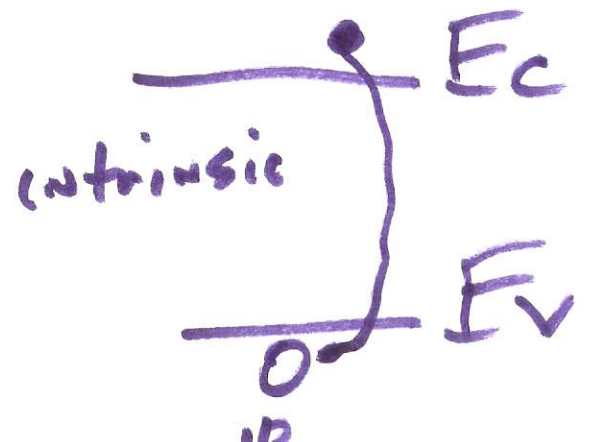
$n = 10^{11} \frac{\text{electrons}}{\text{cm}^3}$

$p = 10^{11} \text{ holes}$

$n_i^2 = pn$



Covalent Bond



$10^{10} \frac{\text{carriers}}{\text{cm}^3}$

Si:

$n = p = 10^{10}$

1)

$$N_{Si} = 10^{22}$$

Doped Si

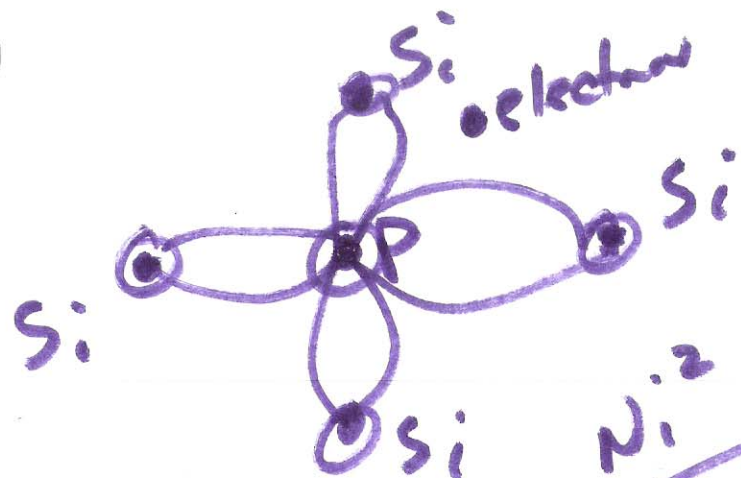
MEANS "add vuts to the # of donor atoms like"

P → Si

$$N_D = \# \text{ of donor atoms}$$

add  $10^{16}$  phosphorus atoms  $\frac{\text{atoms}}{\text{cm}^3}$

$$N_P = N_i$$



What is n?

$$N = N_D + N_i$$

$$N \approx N_D$$

Assume?

complete ionization

$$P \approx \frac{N_i}{N_D} = \frac{N_i}{N_D + N_i}$$

↑  
Assume?

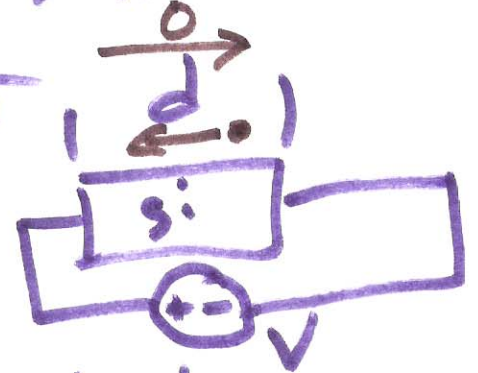
2)

two kinds of current

- 1) drift current  $\rightarrow$  An E field
- 2) diffusion current

mobility

$$\epsilon = \frac{V}{d}$$



$\mu_n$  = mobility of electrons =

$$\mu \rightarrow \frac{\text{Velocity (cm/s)}}{\text{E field (V/cm)}} \quad \text{cm}^2/\text{V}\cdot\text{s}$$

$\mu_p$  = mobility of holes

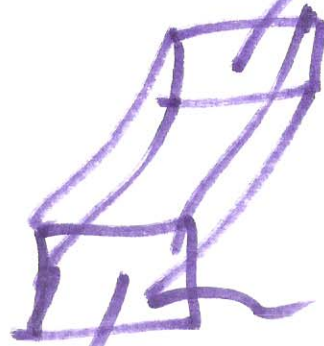


3)

$$J = Qv \rightarrow \frac{C/s}{C/C^3}$$

current density,

$$\frac{V}{E} = 4$$



cross-section  
Area

$$I = J \cdot \text{Area}$$

Amps  $\uparrow$   $C/m^2$

$A/m^2$

$$J_n = -q \cdot N \cdot \mu_n \cdot \vec{E}$$

$$J_p = q_p \cdot \mu_p \cdot \vec{E}$$

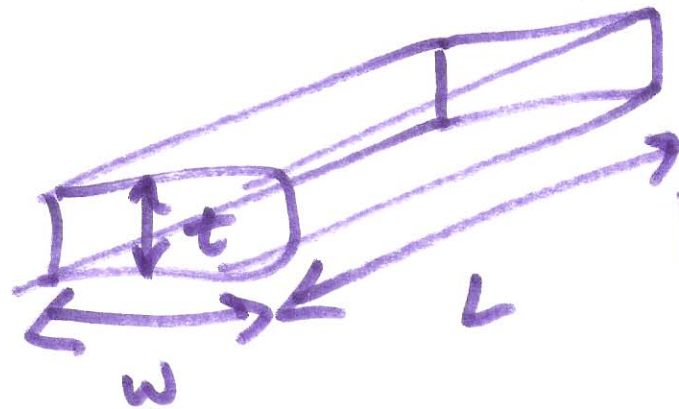
4)

$$J_T = J_n + J_p = qE \cdot (u_n N + u_p P)$$

$\sigma$  = conductivity =

$$q(u_n N + u_p P)$$

$$\rho = \frac{1}{q(u_n \cdot N + u_p \cdot P)} \quad \Omega \cdot \text{cm}$$



$$R = \frac{\rho}{t} \cdot \frac{L}{w}$$

Example Crystalline Si

$14\mu\text{m} = 10^{-6}\text{m} = 0.0001\text{cm}$  doped with  $10^{15}$  Boron atoms  $\frac{\text{atoms}}{\text{cm}^3}$

$t = 104\mu\text{m} = 0.001\text{cm}$

$L = 2004\mu\text{m} = 0.002\text{cm}$

$W = 104\mu\text{m} = 0.001\text{cm}$

$N_D = 0$  No donor atoms

$N_A = 10^{15} \frac{\text{atoms}}{\text{cm}^3}$  (acceptor atoms)

at room estimate  $n_i, n_i = 10^{10}$

$p = 10^{15} \frac{\text{holes}}{\text{cm}^3}$ , assuming complete ionization &  $N_A \gg n_i$

$n = \frac{n_i^2}{p} = \frac{10^{20}}{10^{15}} = 10^5 \rightarrow 10,000 \frac{\text{electrons}}{\text{cm}^3}$

$$\rho = \frac{1}{q(N_A n + \mu_p P)} = \frac{1}{1.6 \times 10^{-19} \cdot 10^{15} \cdot 200}$$

$$\mu_p = \frac{2800 \text{ cm}^2}{\text{V}\cdot\text{s}} = 320 \cdot 10^{-24}$$

$$R = \frac{\rho}{t} \cdot \frac{L}{W} = \frac{31.25 \Omega \cdot \text{cm}}{0.001 \text{ cm}} \cdot \frac{0.02 \text{ cm}}{0.001 \text{ cm}} \cdot \frac{1}{0.0320}$$

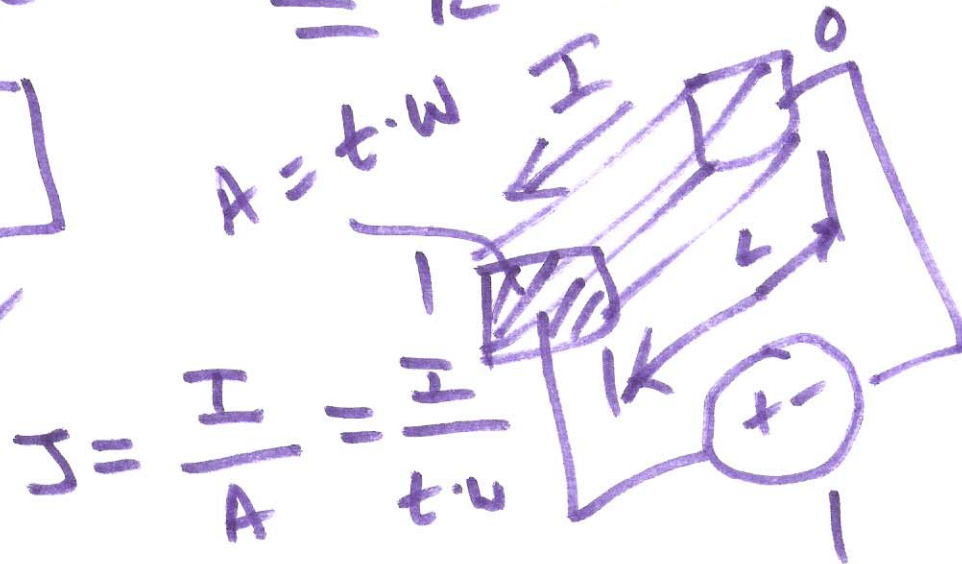


$$R = 625 \text{ K}$$

$$\approx \frac{31.25 \Omega \cdot \text{cm}}{0.001 \text{ cm}}$$

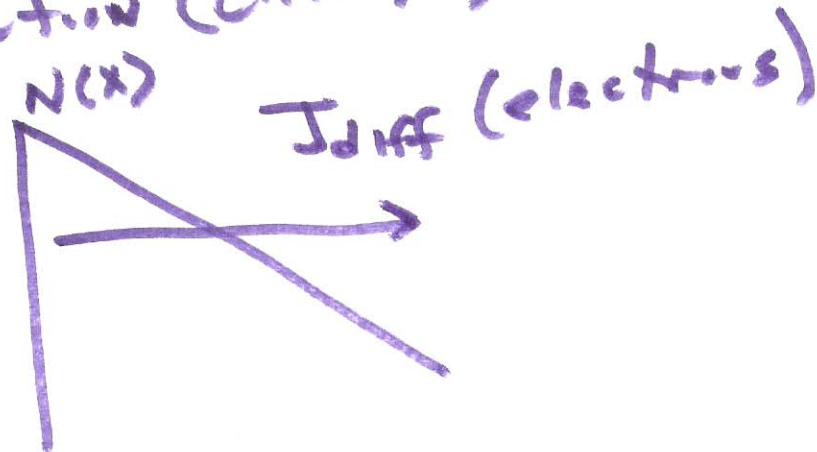
$$E = \frac{1 \text{ V}}{0.02 \text{ cm}} = \frac{50 \text{ V}}{\text{cm}}$$

$$I = \frac{1}{625 \text{ K}}$$



Diffusion current  
No  $E$  field!

for a diffusion current to  
flow we need a carrier  
variation (charge)





2.49

$$J_N = q D_N \cdot \frac{\delta N}{\delta x}$$

$$\frac{\delta N}{\delta x} = \frac{10^{18}}{0.00005 \text{ cm}} = \frac{10^{18}}{5 \cdot 10^{-5} \text{ cm}}$$

$$\frac{\delta N}{\delta x} = 0.2 \cdot 10^{23} \frac{\text{V}}{\text{cm}}$$

$$D_N = \mu_n \cdot \frac{kT}{q}$$

thermal  
voltage  
 $\approx 26 \text{ mV}$

26 mV @  
room temp