

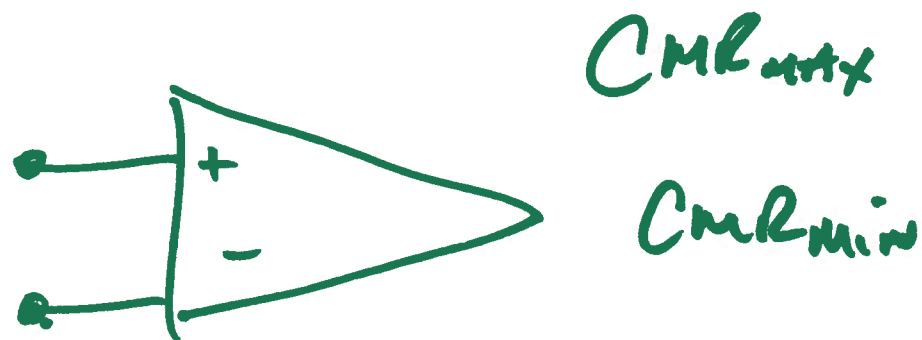
EE 420 / ECE 620  
Analog IC Design

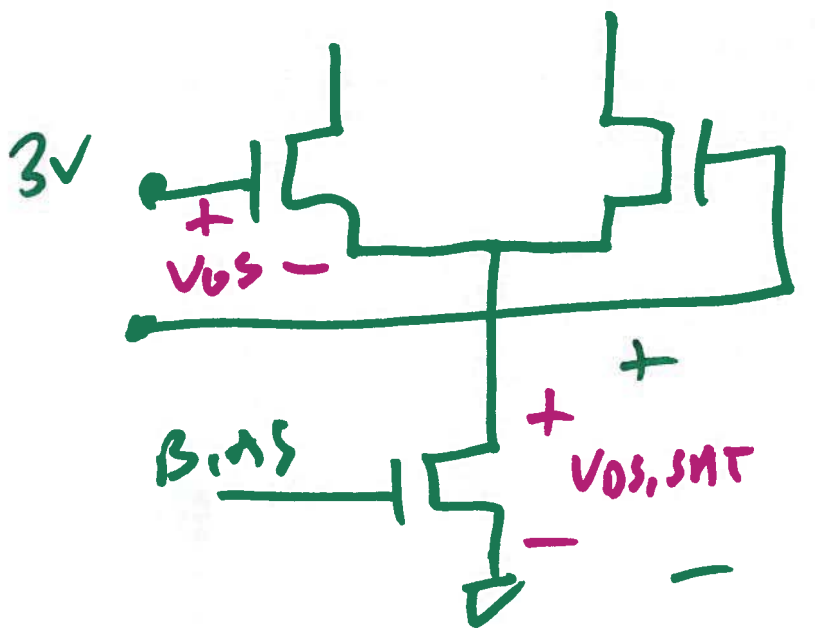
Lecture 18

MARCH 27, 2017

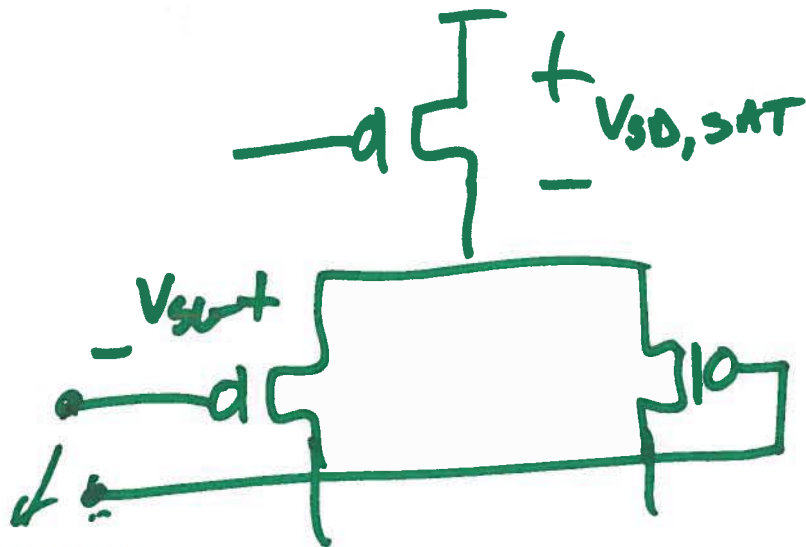
DC behavior of diff-amps

INPUT common-mode range (CMR)



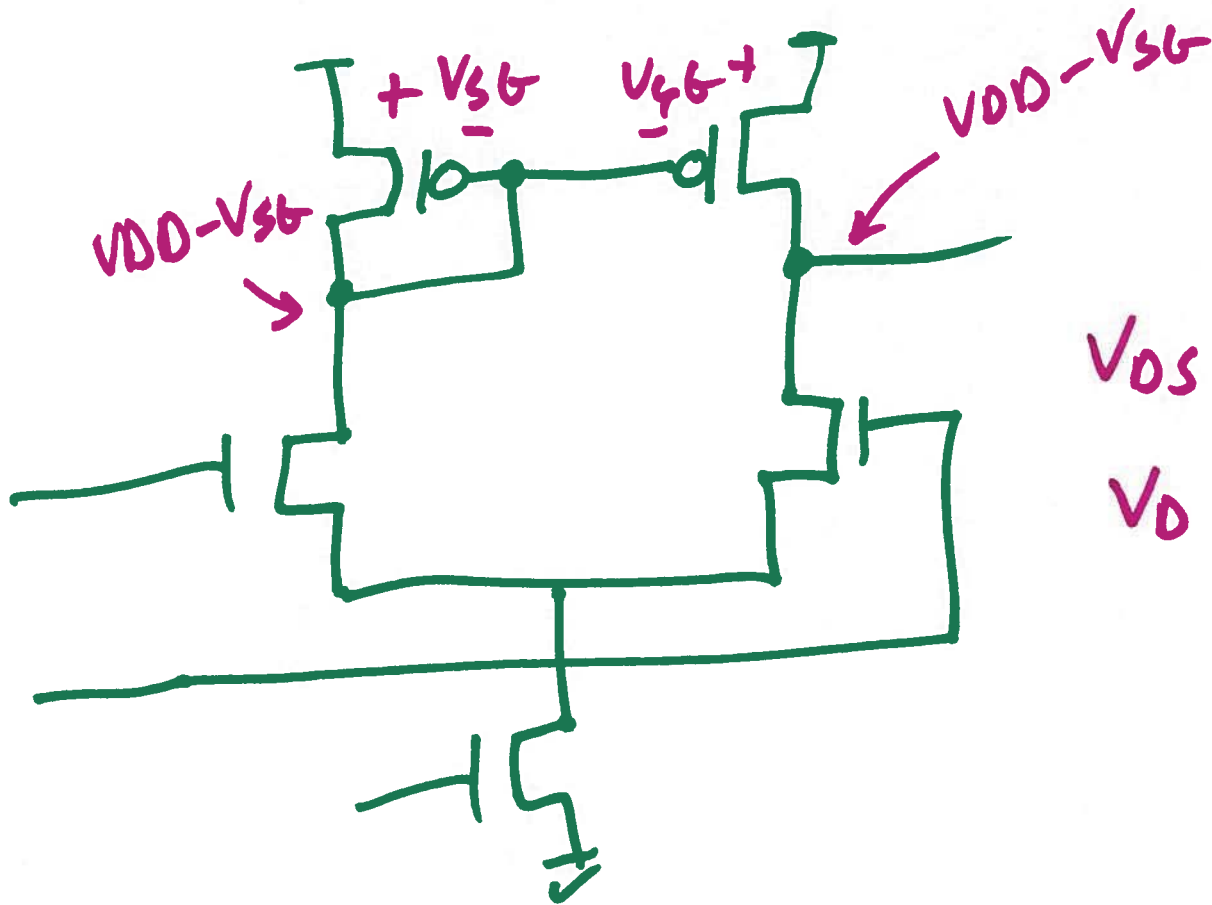


$$\begin{aligned}
 CMR_{min} &= V_{GS} + V_{DS,SAT} \\
 &= 2V_{DS,SAT} + V_{THN} \\
 &= 1.3V
 \end{aligned}$$



$$\begin{aligned}
 CMR_{max} &= V_{DD} - V_{DS,SAT} \\
 &\quad - V_{SG}
 \end{aligned}$$

2)



$$V_{DS} \geq V_{GS} - V_{THN}$$

$$V_D - V_S \geq V_G - V_S - V_{THN}$$

$$V_D \geq V_G - V_{THN}$$

$$V_G \leq V_D + V_{THN}$$

$$\leq V_{DD} - V_{SG} + V_{THN}$$

$$\leq V_{DD} - V_{SD,SAT}$$

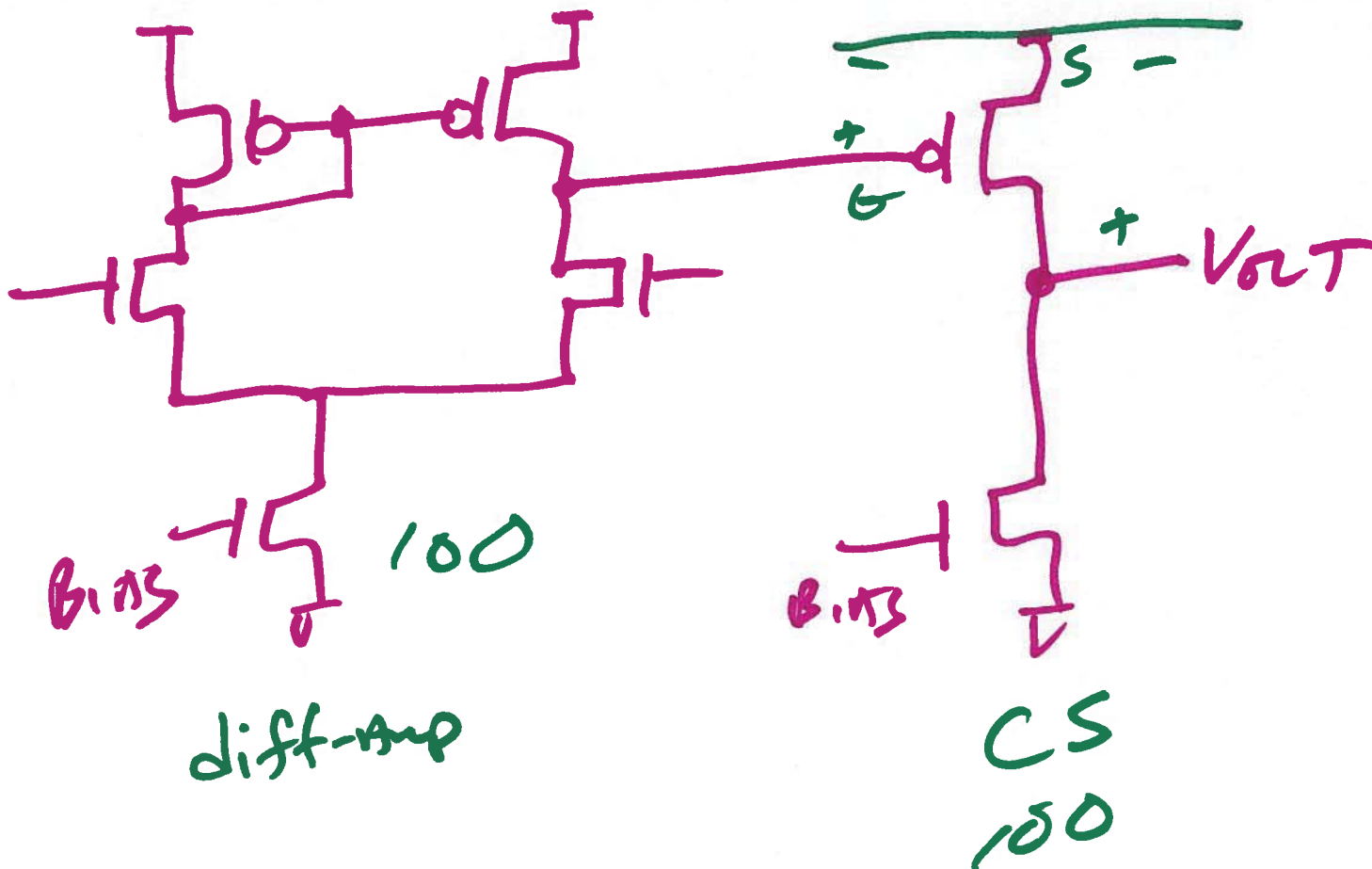
$$-V_{THP} - V_{THN}$$

$$\approx V_{DD} - V_{SD,SAT}$$

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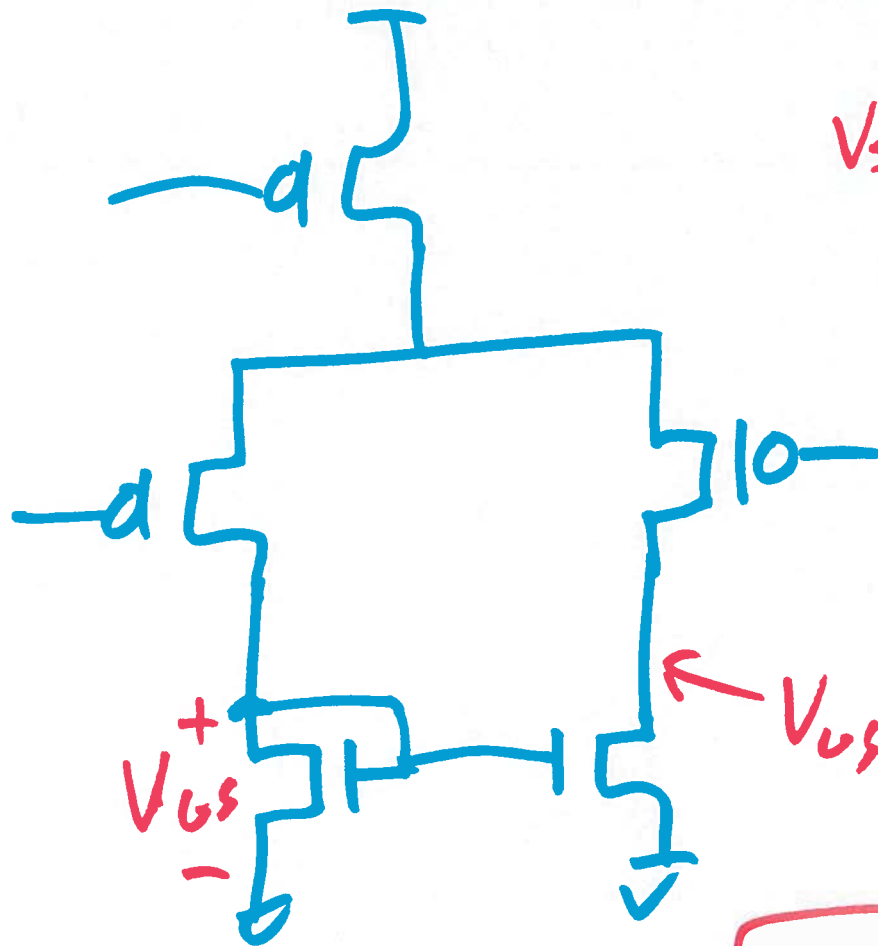
$$C_{M,R_{MAX}} \approx V_{DD} - V_{SD,SAT} \quad V_G$$

# two-stage op-amp



$$A_{OL} = 10,000$$

4)



$$V_{SD} \geq V_{SG} - V_{THP}$$

$$V_S - V_D \geq V_S - V_G - V_{THP}$$

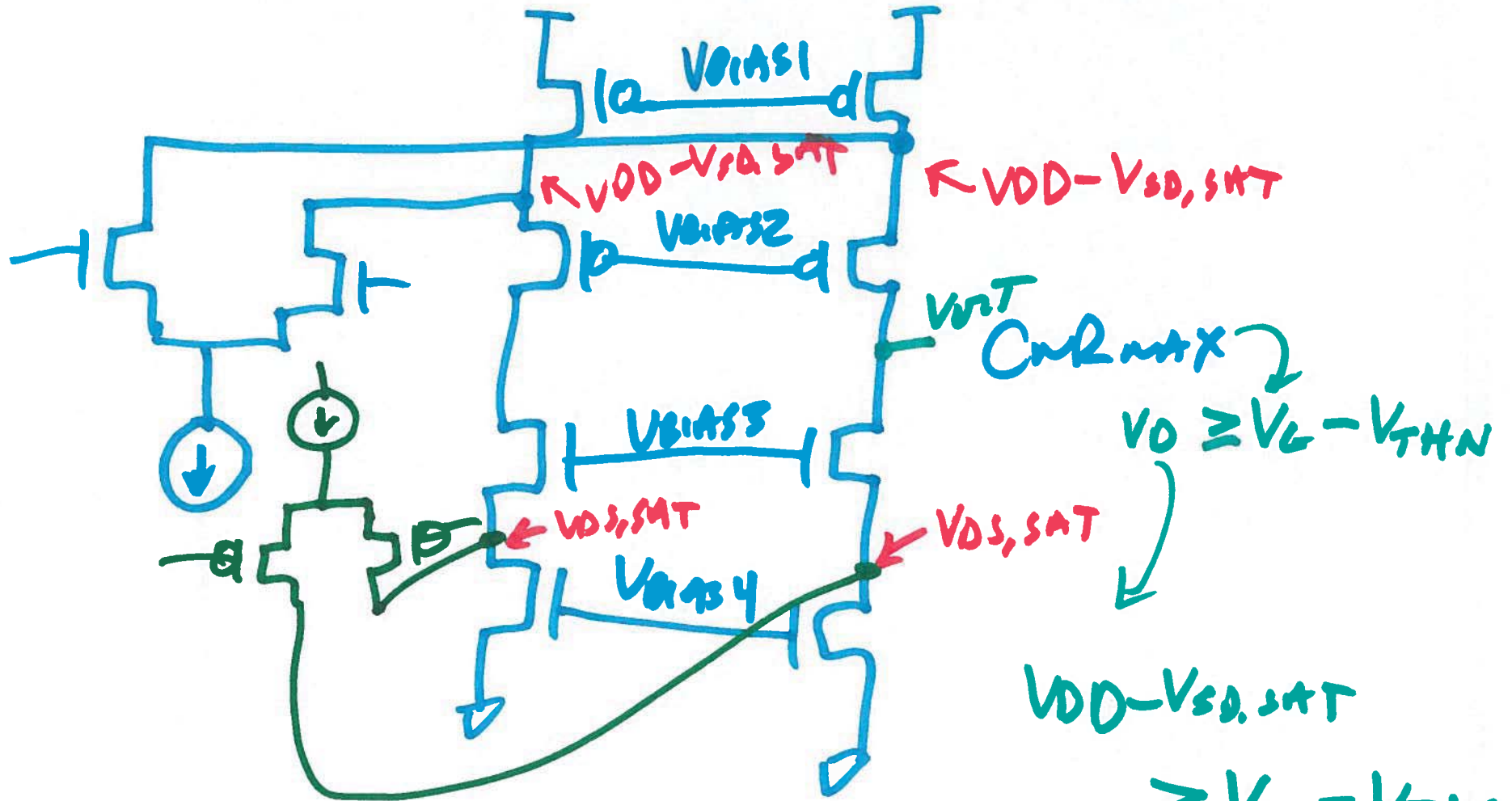
$$V_G \geq V_D - V_{THP}$$

$$\geq V_{GS} - V_{THP}$$

$$\geq V_{DS, SAT} + V_{THN} - V_{THP}$$

$$CMR_{min} \approx V_{DS, SAT}$$

5)



Condition

$$V_{SD} \geq V_{SL} - V_{THP}$$

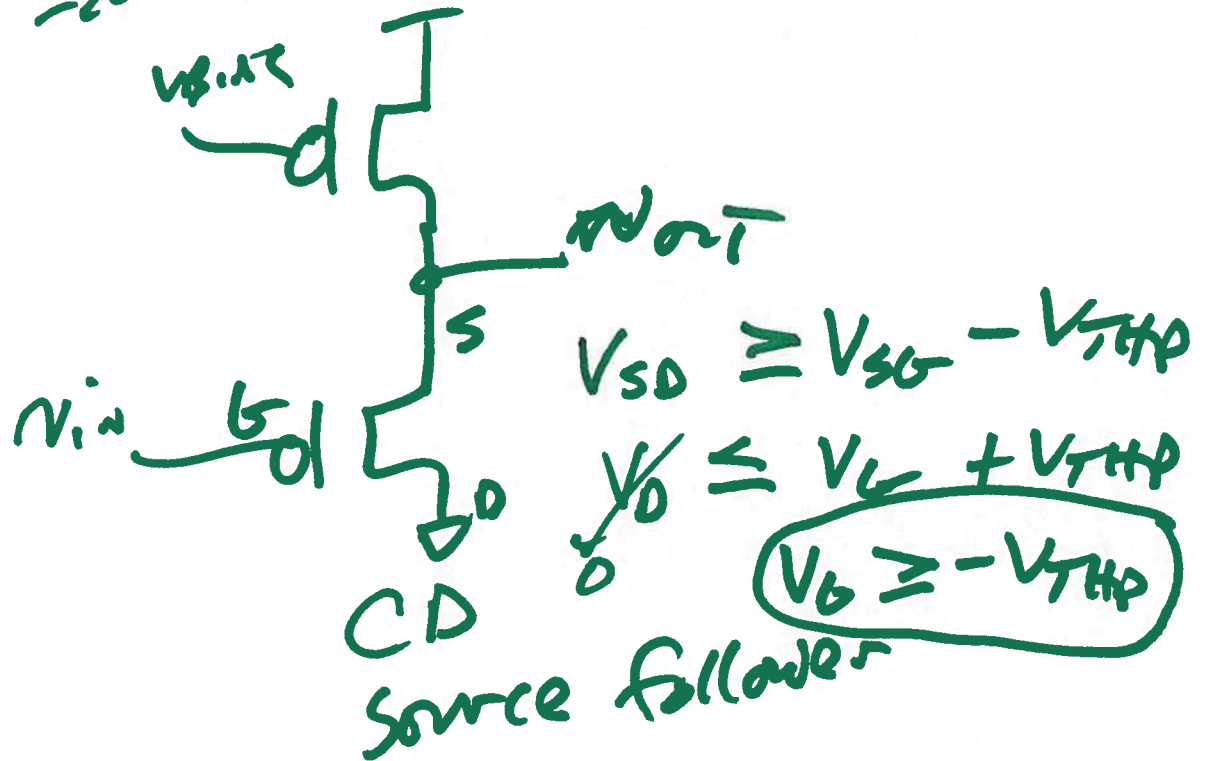
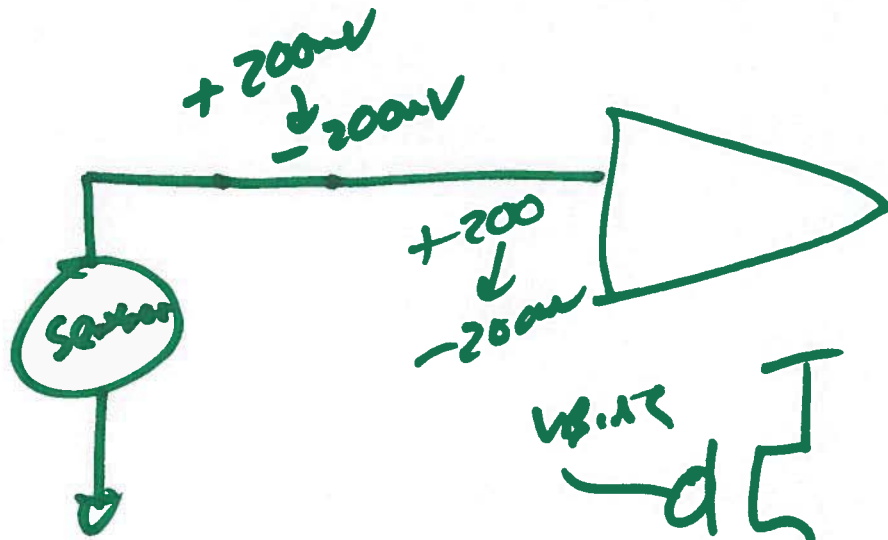
$$V_0 \leq V_G + V_{THP}$$

$$V_G \leq V_{DD} - V_{SD,SAT} + V_{THN}$$

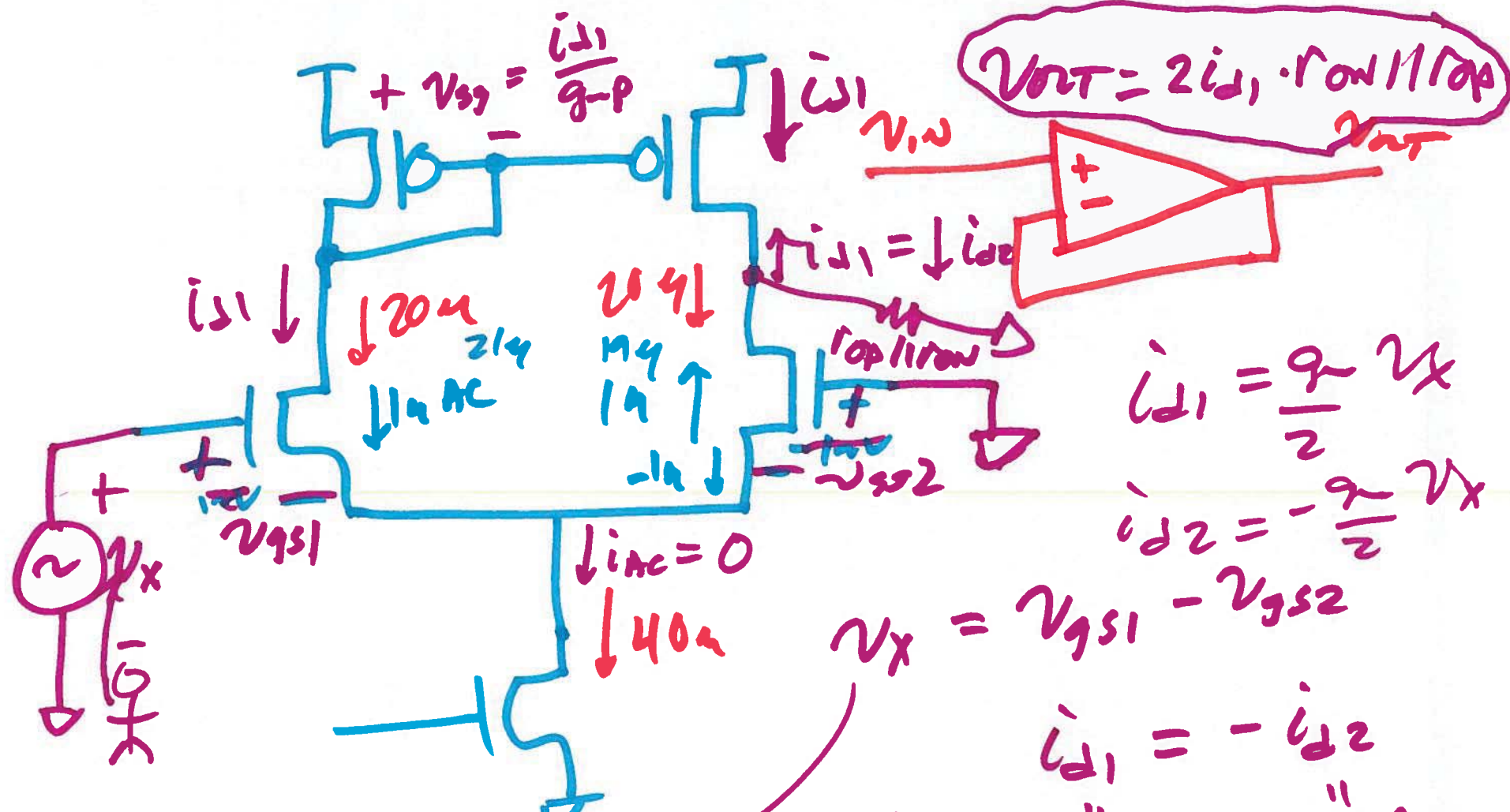
$$V_G \geq V_{GS,SAT} - V_{THP}$$

6)

$$V_{GS,SAT} \leq V_G + V_{THP}$$



1)



$$v_{out} = 2i_{d1} \cdot r_{op1} || r_{op2}$$

$$i_{d1} = \frac{g_m v_x}{2}$$

$$i_{d2} = -\frac{g_m v_x}{2}$$

$$v_x = v_{gs1} - v_{gs2}$$

$$i_{d1} = -i_{d2}$$

$$v_x = \frac{i_{d1}}{g_m} - \frac{i_{d2}}{g_m} \quad g_m v_{gs1} = -g_m v_{gs2}$$

$$v_{gs1} = \frac{i_{d1}}{g_m}$$

$$v_{gs2} = \frac{-i_{d2}}{-g_m} = \frac{i_{d2}}{g_m}$$

$$v_x = \frac{2}{g_m} \cdot i_{d1}$$

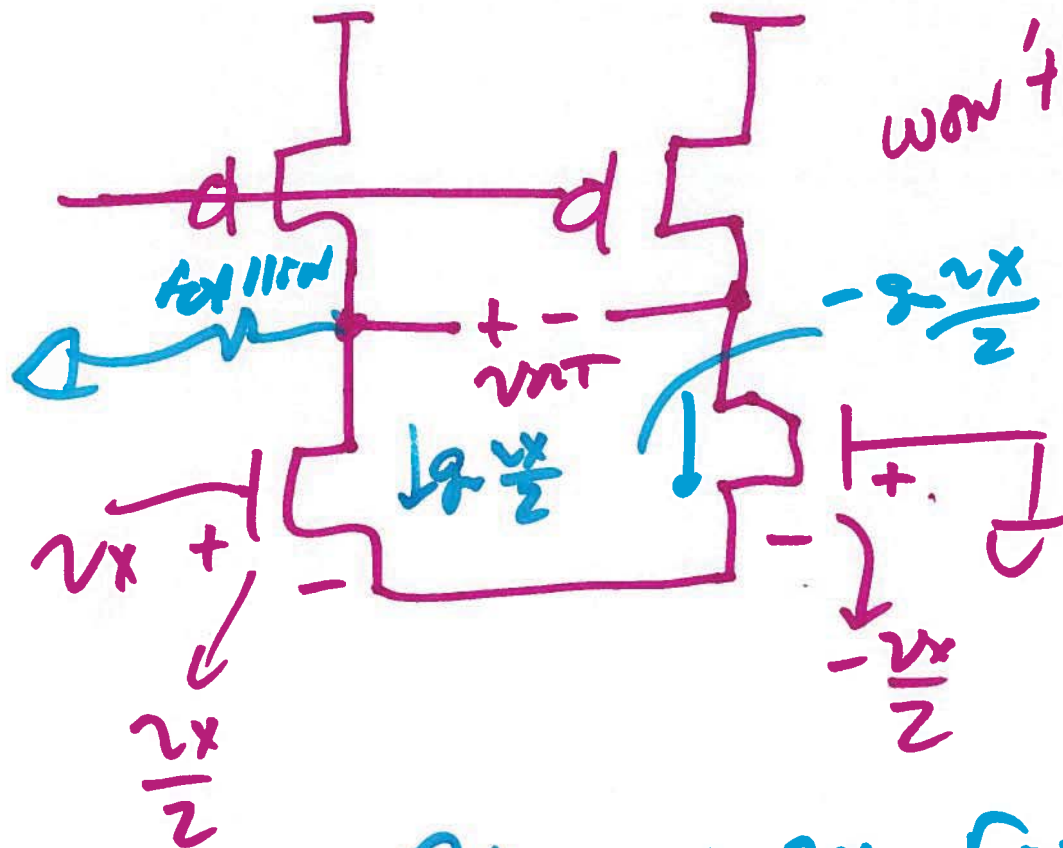
8)



$$V_{out} = 2i_{d1} \cdot r_{on} \parallel r_{op}$$

$$V_x = \frac{2}{g_{m1}} i_{d1} \rightarrow i_{d1} = g_{m1} \frac{V_x}{2}$$

$$\frac{V_{out}}{V_x} = g_{m1} \cdot r_{on} \parallel r_{op}$$



won't bias up without

Common-mode feedback circuit

$$A_d = g_m r_{o1} r_{op}$$

$$v_+ = g_m \frac{v_x}{2} \cdot r_{o1} r_{op} \text{ differential mode gain}$$

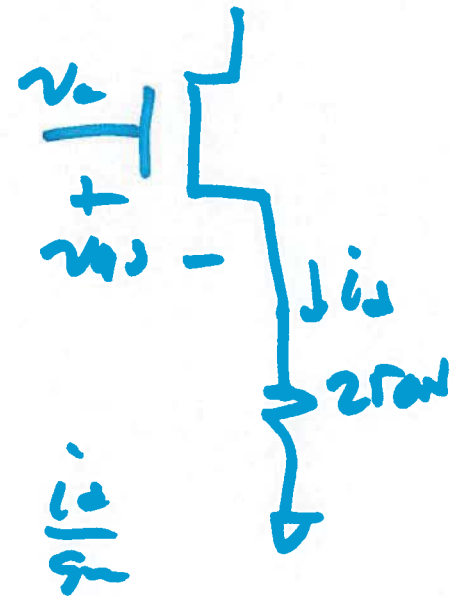
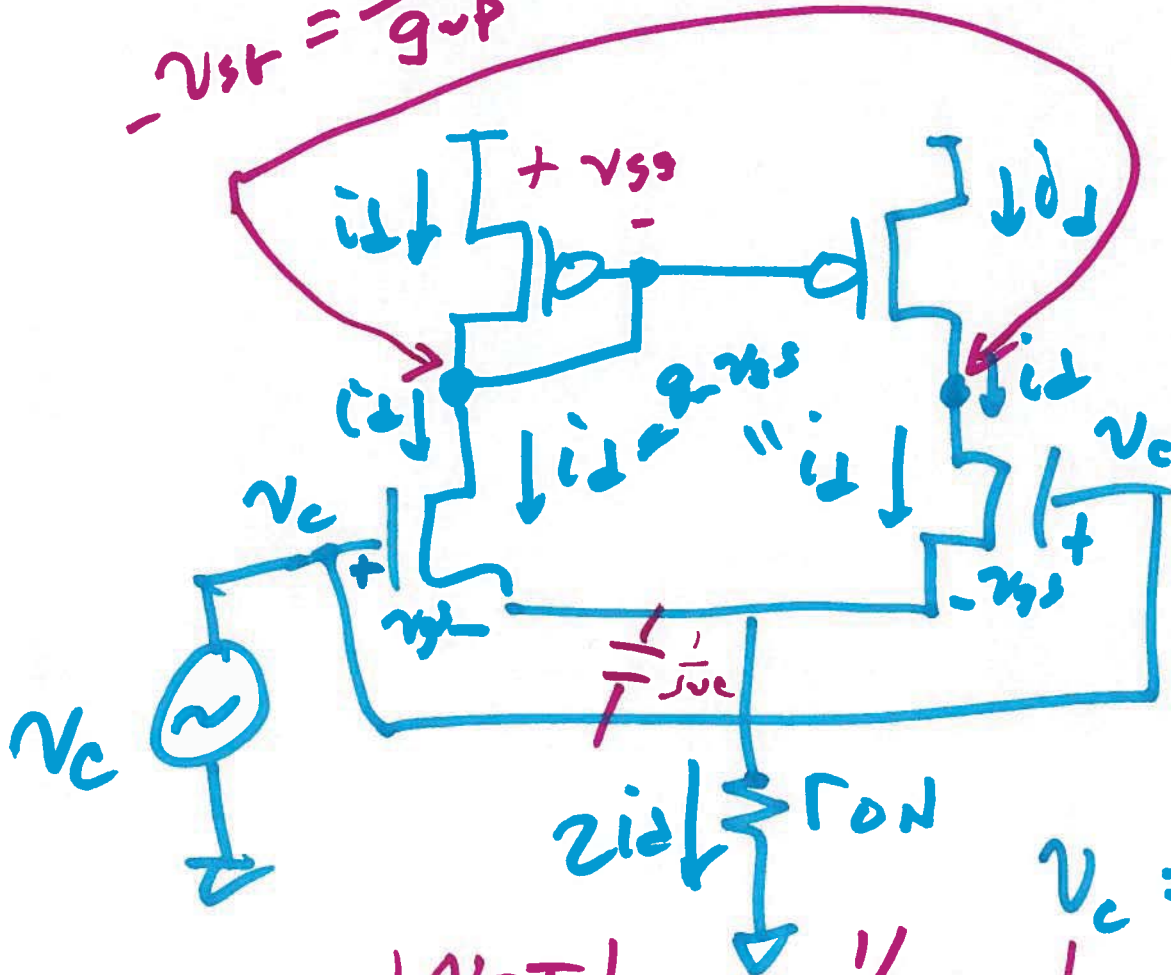
$$v_- = -g_m \frac{v_x}{2} \cdot r_{o1} r_{op}$$

$$v_{MT} = v_+ - v_- = v_x \cdot g_m \cdot r_{o1} r_{op}$$

# Common-mode reject

$$-v_{str} = \frac{i_d}{g_{mP}} = v_{out}$$

CMRR ← ratio  
↑ reject



$$v_c = v_{gs} + z_{id} \cdot r_{OD}$$

$$|A_c| = \left| \frac{v_{out}}{v_c} \right| = \left| \frac{1/g_{mP}}{\frac{1}{g_{mN}} + 2r_{OD}} \right| \quad v_c = i_d \left( \frac{1}{g_{mN}} + 2r_{OD} \right)$$

common input

$$\approx \frac{1}{g_{mP} \cdot 2r_{OD}}$$

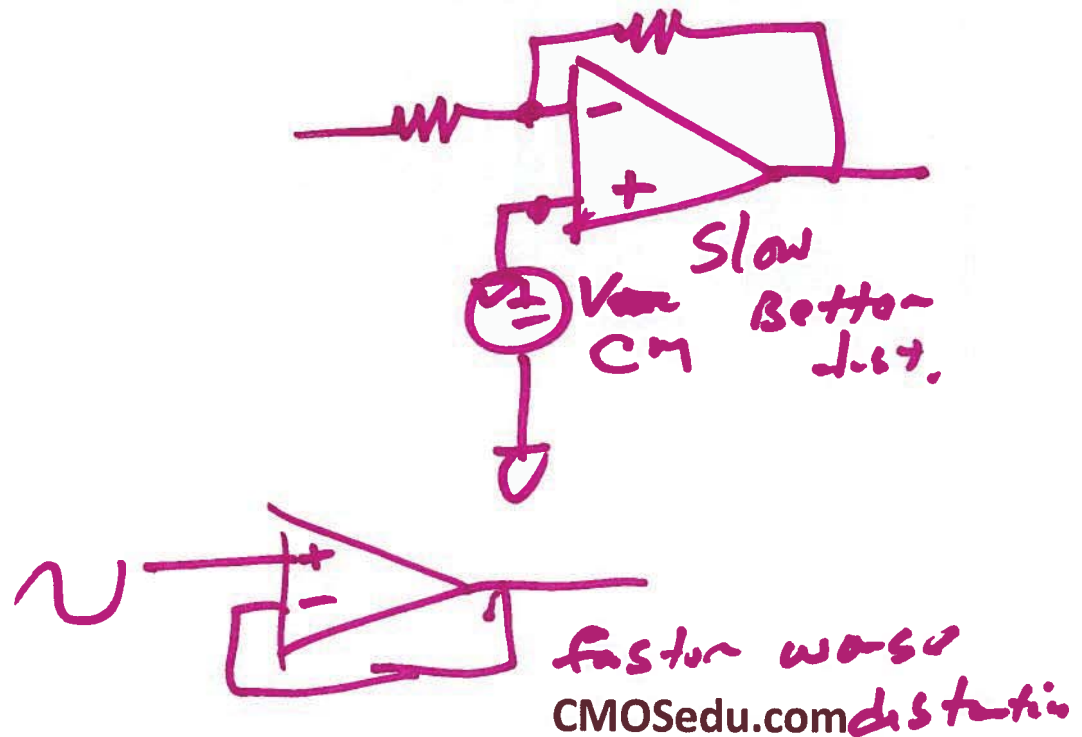
iii)

$$A_c = \text{Common-mode gain} = \frac{1}{g_m \cdot 2r_{on}}$$

$$A_d = \text{difference-mode gain} = g_m \cdot R_{out}/2$$

COMMON-MODE REJECTION RATIO

$$CMRR = 20 \log \frac{A_d}{A_c}$$



(2)

$$CMRR = 60 \text{ dB}$$

$$200 \text{ nV} = \Delta V_e$$

$$\Delta V_{out} = 10 \text{ nV}$$

$$\frac{10 \text{ nV}}{50} = \frac{2 \text{ nV}}{50} \quad \downarrow V_{os} \quad -26 \text{ dB}$$

$$A_c = \frac{10 \text{ nV}}{200 \text{ nV}} = \frac{1}{20} = 0.05 = -26 \text{ dB}$$

$$CMRR = 20 \log \frac{A_d}{A_c} = 60 \text{ dB}$$

$$-6 \text{ dB} = \frac{1}{2}$$

$$-20 \text{ dB} = \frac{1}{10}$$

$$60 \text{ dB} = 20 \log A_d - 20 \log A_c - 26 \text{ dB}$$

$$-14 \text{ dB} = \frac{1}{5}$$

$$+ 26 \text{ dB}$$

$$34 \text{ dB} = 20 \log A_d \Rightarrow A_d = 34 \text{ dB} = 50$$