

EE 420 / ECG 620

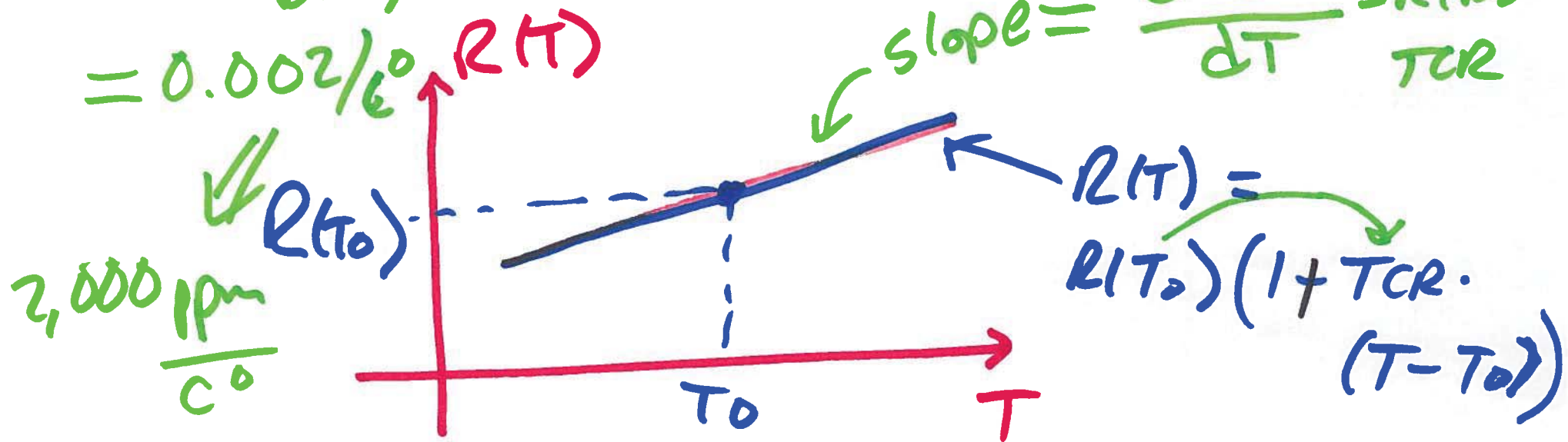
Analog IC Design

Lecture 20

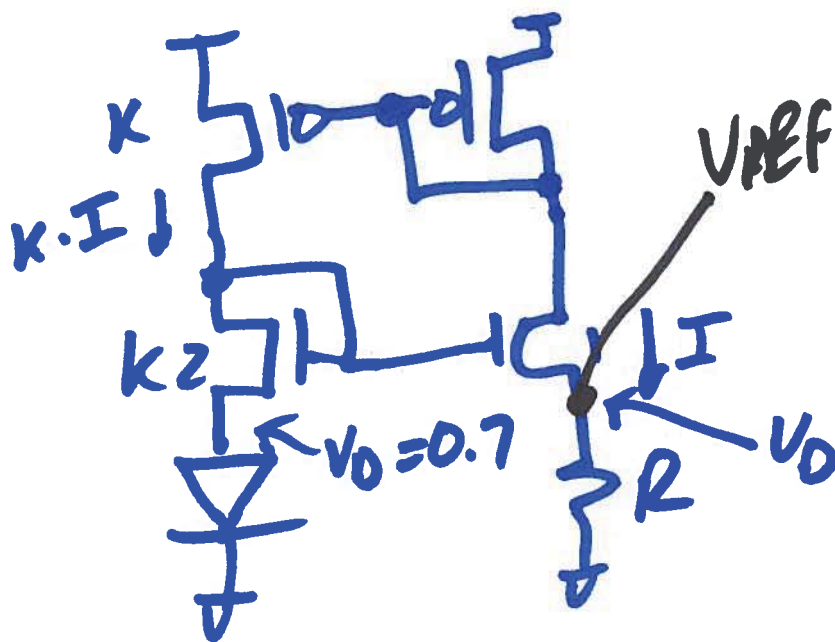
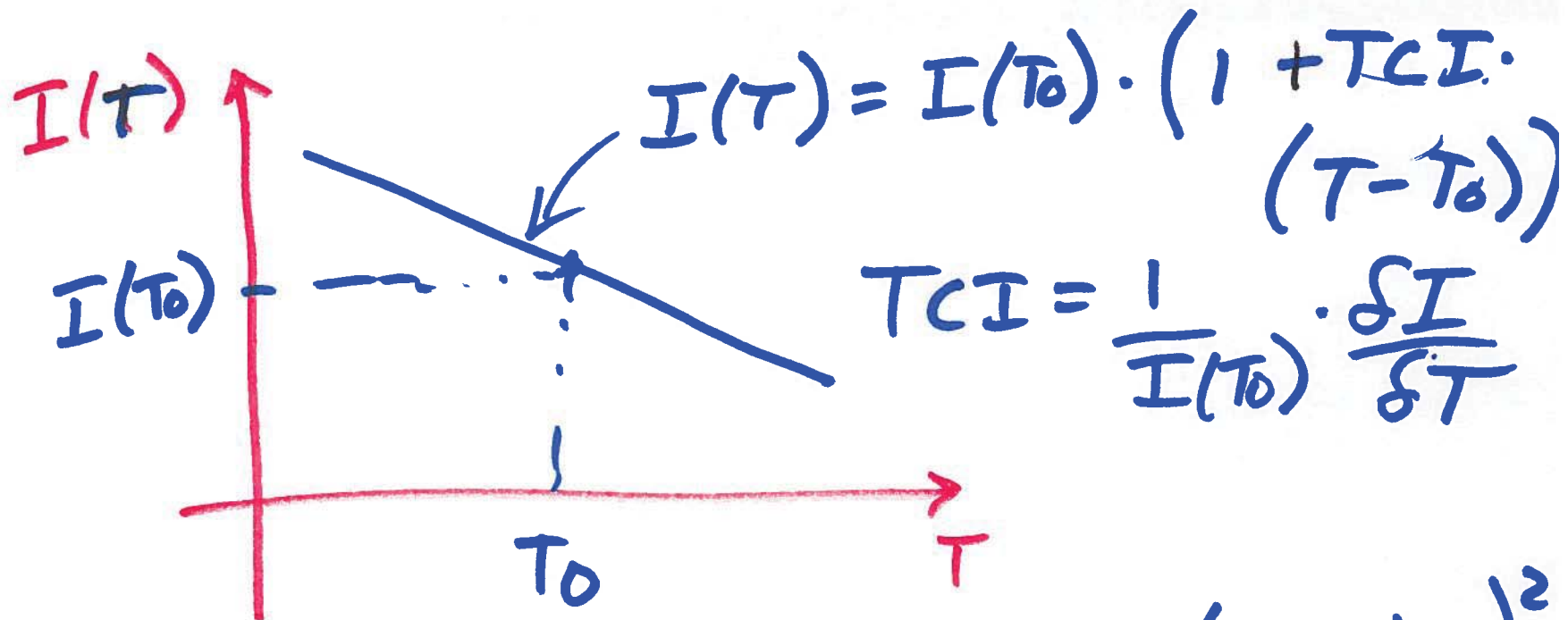
April 3, 2017

$$TCR = \frac{1}{R(T_0)} \frac{dR(T)}{dT}$$
$$= 0.002/^\circ C$$

$$\text{slope} = \frac{dR(T)}{dT} = R(T_0) \cdot TCR$$



1)



$$KI = k \cdot \frac{k_{PN}}{2} \cdot \frac{W}{L} (V_{DS} - V_{TN})^2$$

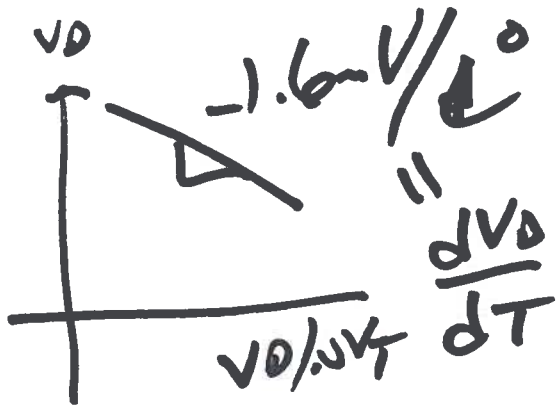
$$I = \frac{k_{PN}}{2} \cdot \frac{W}{L} (V_{DS} - V_{TN})^2$$

$$V_D = V_{TN} \quad I_n = \frac{KI_0}{I_S}$$

2)

$$\frac{\delta I}{\delta T} = \frac{\delta}{\delta T} \left(\frac{V_D}{R} \right) = \frac{d}{dT} (V_D \cdot R^{-1})$$

$$= \frac{1}{R} \frac{\delta V_D}{\delta T} + V_D \frac{(-1)}{R^2} \frac{\delta R}{\delta T}$$



$$\frac{\delta I}{\delta T} = \frac{V_D}{R} \cdot \frac{1}{V_D} \cdot \frac{\delta V_D}{\delta T} + I \cdot \frac{1}{R} \frac{\delta R}{\delta T}$$

$$I_D \approx I_{SE}$$

$$TCI = \frac{1}{I} \frac{\delta I}{\delta T} = \frac{1}{V_D} \cdot \frac{\delta V_D}{\delta T} + \frac{1}{R} \frac{\delta R}{\delta T}$$

$$\frac{\delta I}{\delta T} = 0.08 \frac{\mu V}{C^\circ}$$

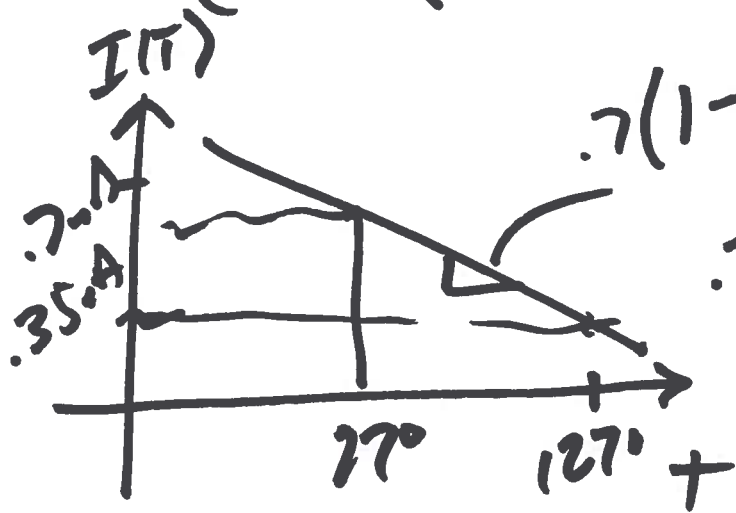
$$I(T) = I(T_0) (1 + TCI(T - T_0))$$

$$I(T) = I(T_0) \cdot (1 + \alpha I(T - T_0))$$

$$I(T_0) = \frac{I}{1K} = I \cdot \alpha I = \frac{1}{V_D} \cdot \frac{\delta V_D}{\delta T} \cdot \frac{1}{R} \cdot \frac{\delta R}{\delta T}$$

$$I(T) = 0.7 \mu A \cdot \left(\frac{-1.6 - V/k}{.7} \cdot 0.002 \right)$$

$$\left(1 + (-0.004286)(T - 300) \right) = \frac{-0.0016}{.7} \cdot 0.002$$



$$.7(1 - 0.004286 \cdot 100)$$

$$.7 \cdot (.5114)$$

$$= \frac{-4,286}{C^\circ} \text{ ppm}$$

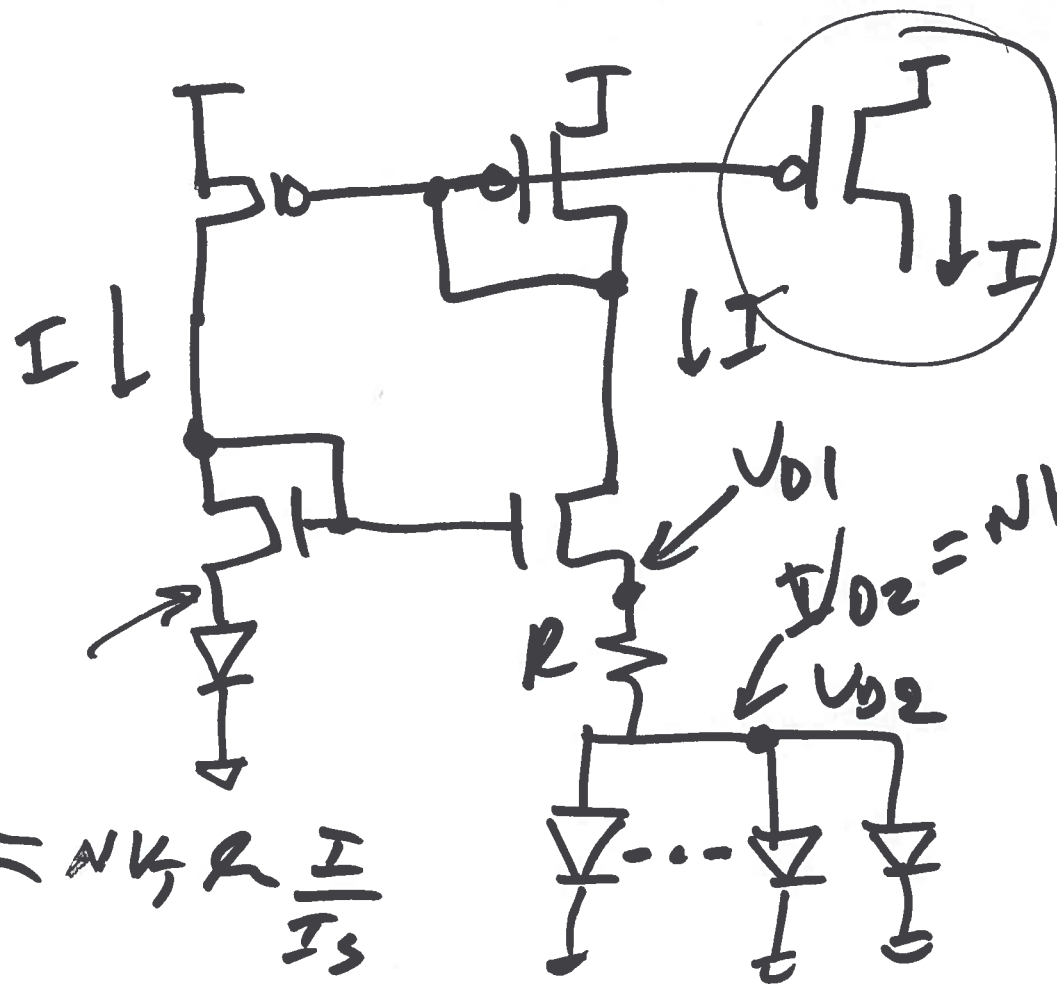
4)

$$\frac{\delta V_{REF}}{\delta T} = \frac{\delta I \cdot R}{\delta T} = R \cdot \frac{\delta I}{\delta T} + I \cdot \frac{\delta R}{\delta T}$$

$$V_{REF} = I \cdot R \quad \underbrace{TCI} \quad \underbrace{TCR}$$

$$TCV_{REF} = \frac{1}{V_{REF}} \cdot \frac{\delta V_{REF}}{\delta T} = \frac{R \cdot \frac{\delta I}{\delta T}}{I \cdot R} + \frac{I \cdot \frac{\delta R}{\delta T}}{I \cdot R}$$

$$V_{REF}(T) = V_{REF}(T_0) \left(1 + TCV_{REF} \cdot (T - T_0) \right)$$



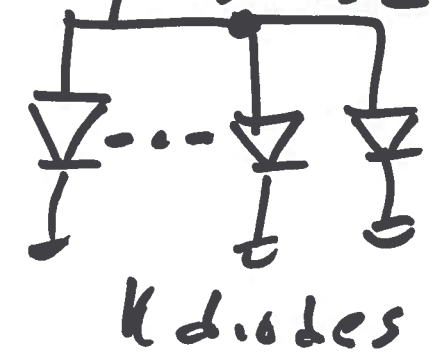
$$I_0 = I_s e^{V_0 / N V_T} K$$

$$V_D = N V_T \ln \frac{I_0}{I_s}$$

$$\frac{I}{K I_s} = I_s e^{V_0 / N V_T}$$

$$V_0 = N V_T \ln \frac{I_0}{K I_s}$$

$$V_{D1} = N V_T \ln \frac{I}{I_s}$$



k diodes

$$I = \frac{V_{D1} - V_{D2}}{R} = \frac{N V_T \ln \frac{I}{I_s} - N V_T \ln \frac{I}{K I_s}}{R}$$

$$= \frac{N V_T \ln K}{R}$$

-5

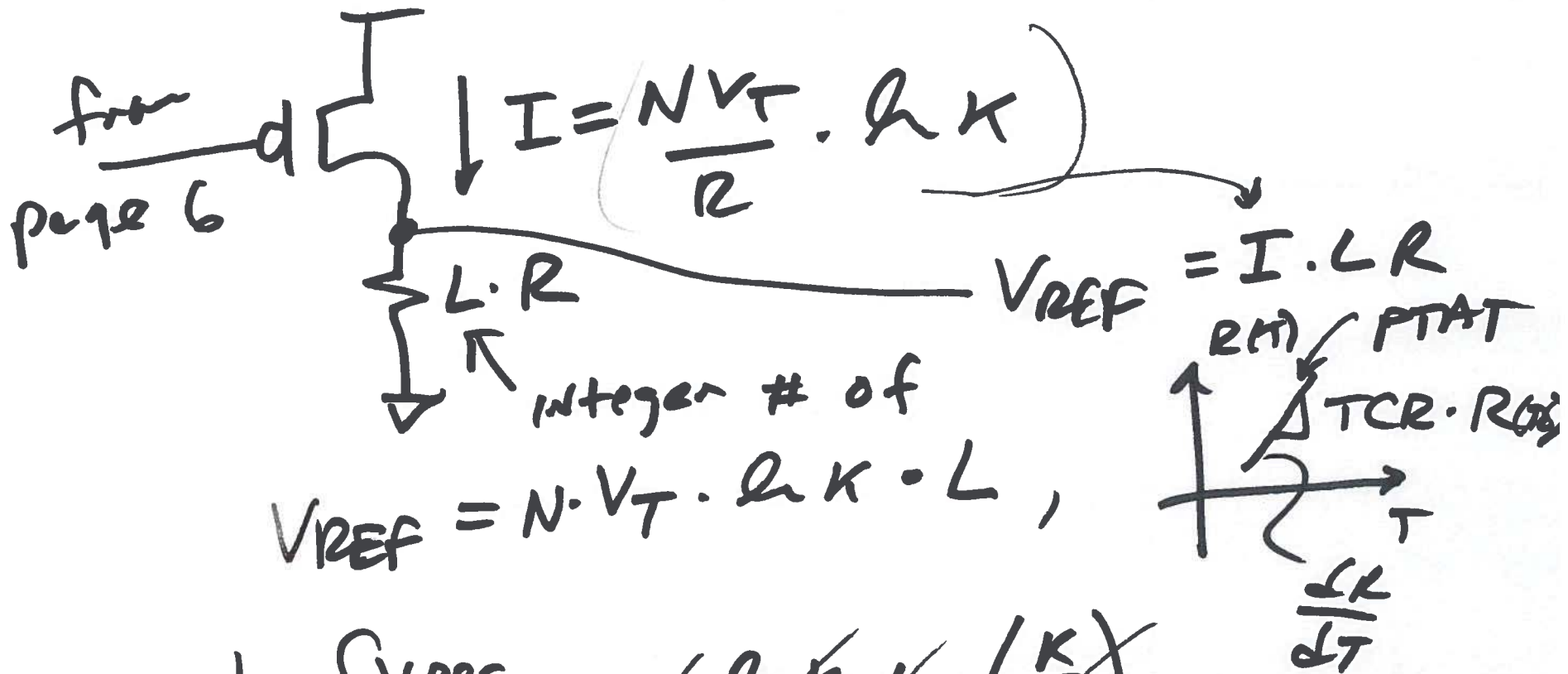
6)

$$\frac{\delta I}{\delta T} = \frac{\delta N V_T R^{-1} Q K}{\delta T}, \quad I = \frac{N V_T \cdot Q K}{R}$$

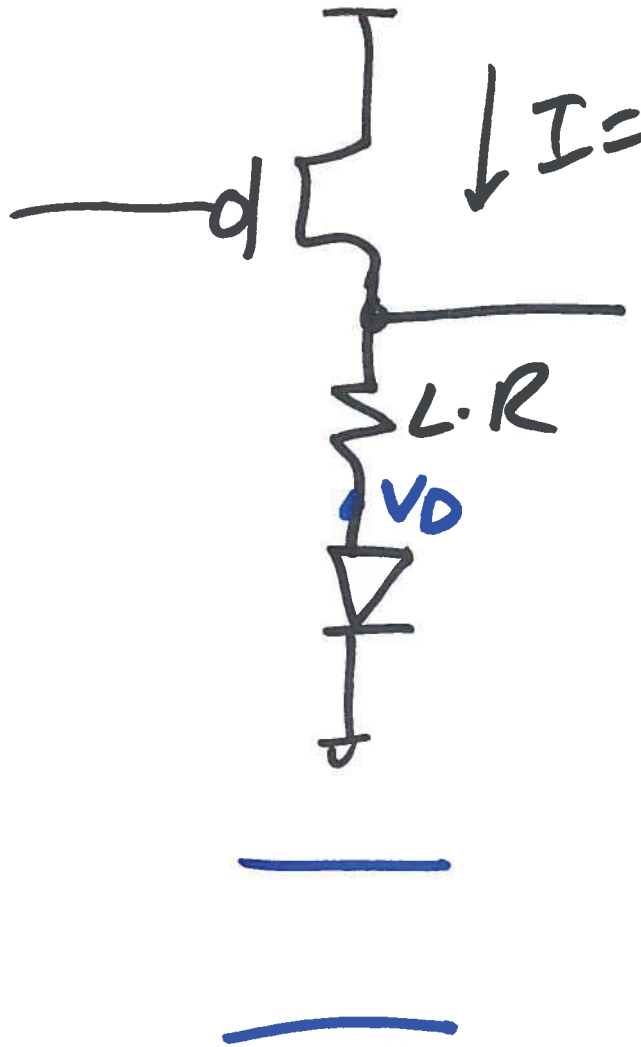
$$V_T = \frac{kT}{q}$$

$$\frac{1}{I} \frac{\delta I}{\delta T} = \frac{N \cdot Q \cdot K \cdot R}{N \cdot Q \cdot K \cdot V_T} \left(\frac{1}{R} \frac{\delta V_T}{\delta T} + V_T \cdot \left(-\frac{1}{R} \frac{\delta R}{\delta T} \right) \right)$$

$$TC_I = \frac{1}{I} \frac{\delta I}{\delta T} = \frac{1}{V_T} \frac{\delta V_T}{\delta T} + \frac{-1}{R} \frac{\delta R}{\delta T}$$



$$TCV_{REF} = \frac{1}{V_{REF}} \frac{\delta V_{REF}}{\delta T} = \frac{N \cdot Q \cdot K \cdot L \cdot \left(\frac{K}{q}\right)}{N \cdot \frac{K}{q} \cdot T \cdot Q K \cdot L}$$



BAND gap voltage $\frac{dV_{REF}}{dT} = 0$

$$I = \frac{NVT}{L} \cdot k$$

$$V_{REF} = NV_T \ln k \cdot L + V_D$$

$$\frac{dV_{REF}}{dT} = 0 = N \cdot \frac{k}{q} \ln k \cdot L - \frac{1.6 \text{ mV}}{C_0}$$

$$\frac{N \cdot k}{q} \ln k \cdot L = \frac{1.6 \text{ mV}}{C_0}$$

$\frac{1}{0.000085} \cdot \ln 8 \cdot L = 0.0016$

$$L = 0.0016$$

$L = 9.41$

a)