

EE 421 / ECE 621

Digital IC Design

Lecture 13

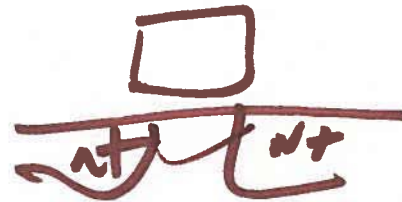
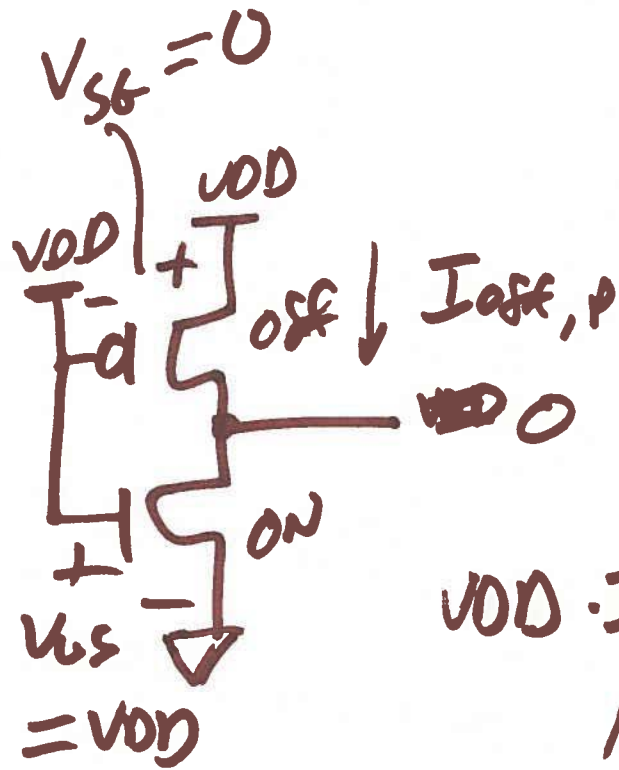
OCT. 11, 2017

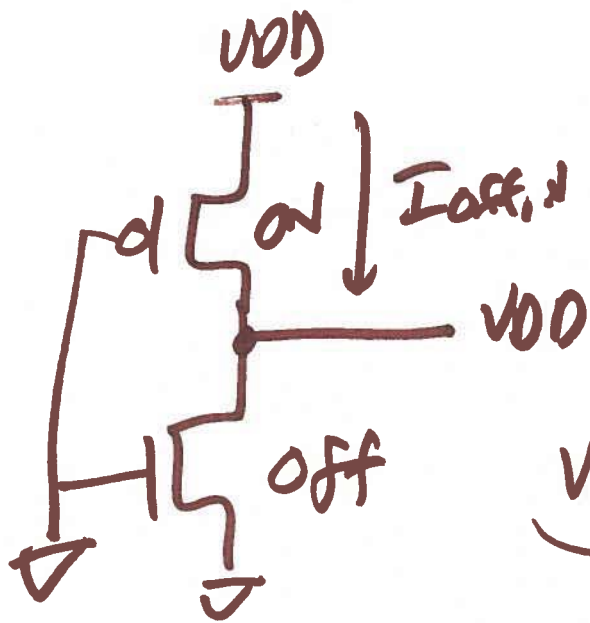
161ga transistors

10^9 transistors

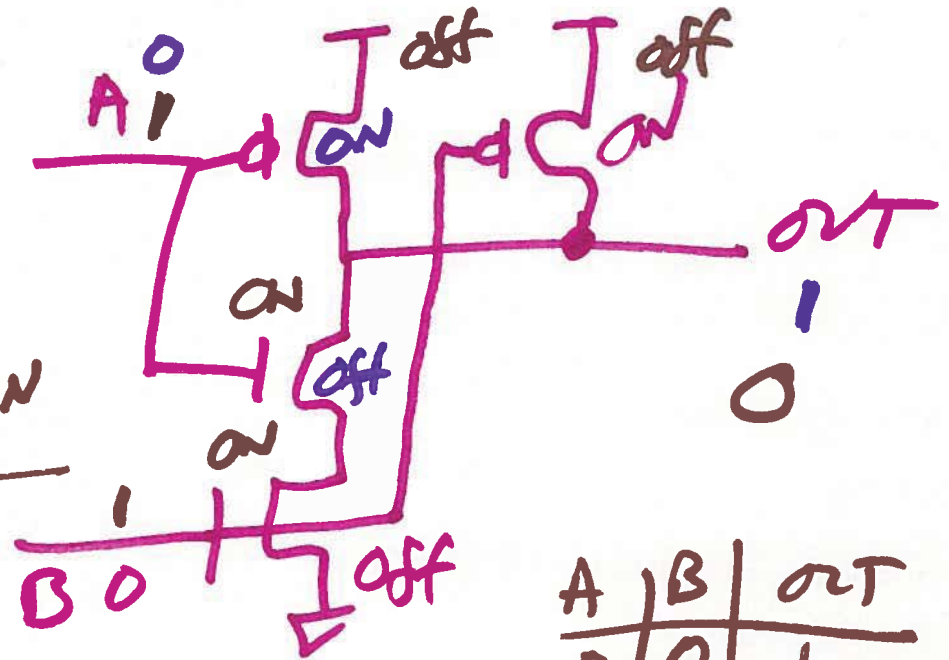
$$10^{-9} \cdot 10^9 = \underline{\underline{1A}}$$

Reduce

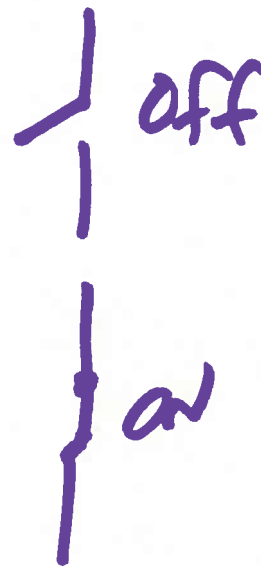
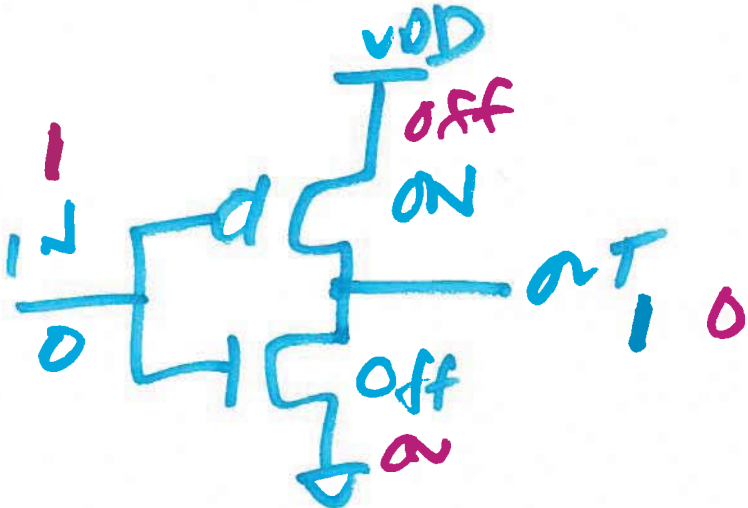




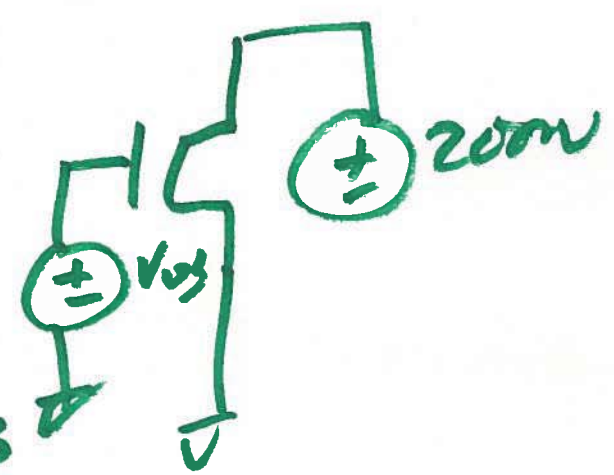
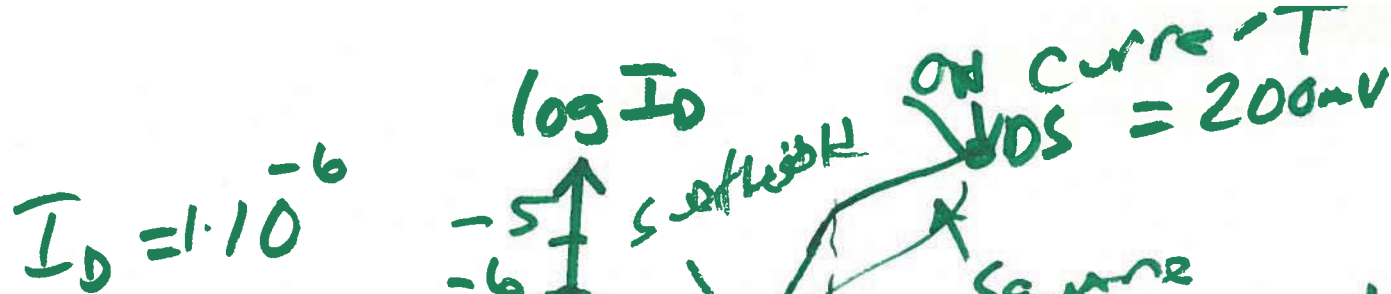
$$VDD \cdot I_{off, N}$$



A	B	OUT
0	0	1
0	1	1
1	0	1
1	1	0



2)



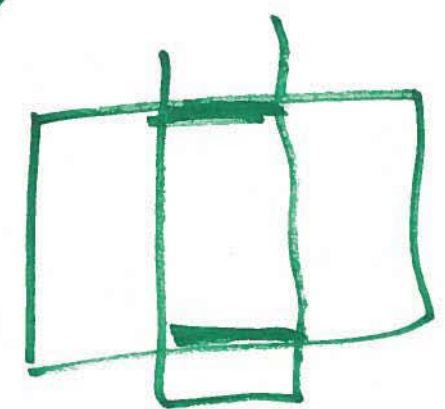
Subthreshold current

$V_{gs} = V_{ds} = V_{DD}$
 $V_{gs} = 0$
 $I_{off,N}$

$I_{on,N}$

$I_D = I_{D0} e^{\frac{V_{gs}}{nV_T}}$

$I_C = I_S e^{\frac{V_{be}}{nV_T}}$



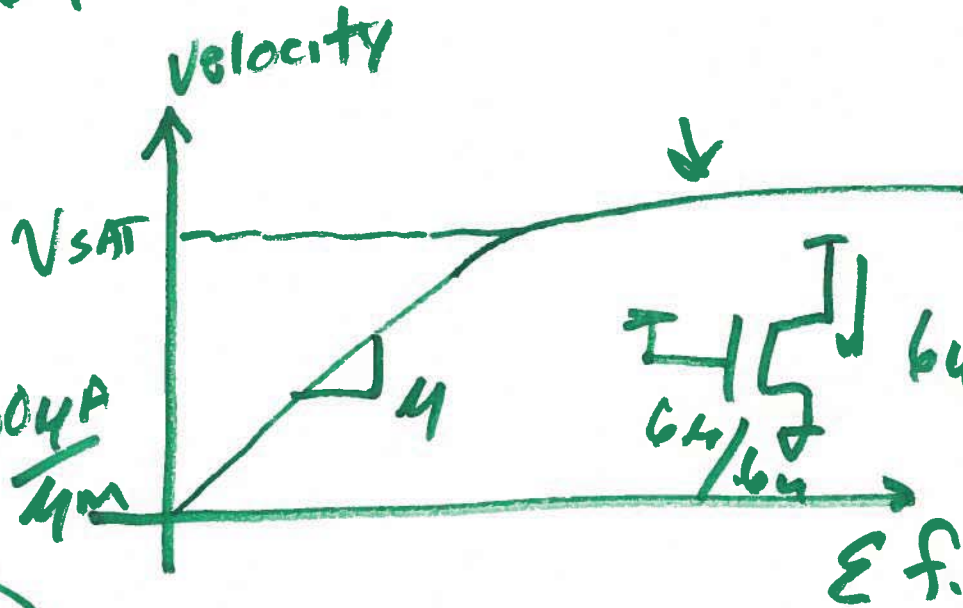
$I_D = \frac{k_p \mu}{2} \frac{W}{L} (V_{gs} - V_{th})^2$

$g_m = \frac{I_D}{nV_T}$

3)

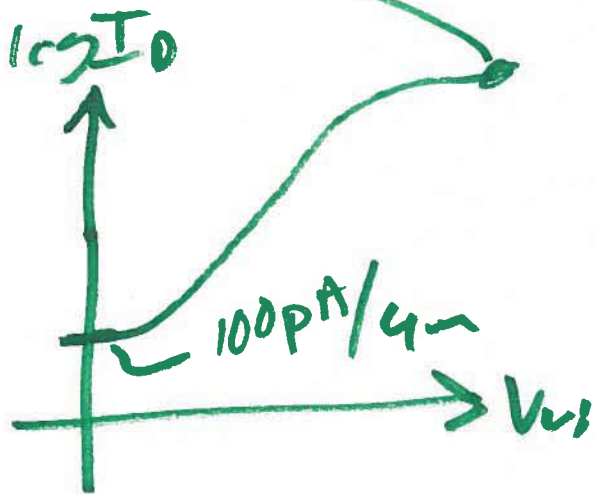
$$\mu = \frac{\text{Velocity } v, \text{ cm/s}}{\text{E-field, } \sqrt{\text{V/cm}}}, \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$\frac{64}{0.64} = 100 \frac{\mu\text{A}}{\mu\text{m}}$$



$$I_{ON} = 400 \frac{\mu\text{A}}{\mu\text{m}}$$

$$\frac{64 \cdot 400 \mu\text{A}}{4} = 2.4 \mu\text{A} \rightarrow 2,400 \mu\text{A}$$



$$I_D = \frac{\mu_n \cdot C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{THN})^2 \text{ Long channel}$$

$$I_D \propto V_G$$

4)



$$P_{avg} = I_{avg} \cdot V_{DD} = I_{avg}$$

$$Q = C_L \cdot V_{DD}$$

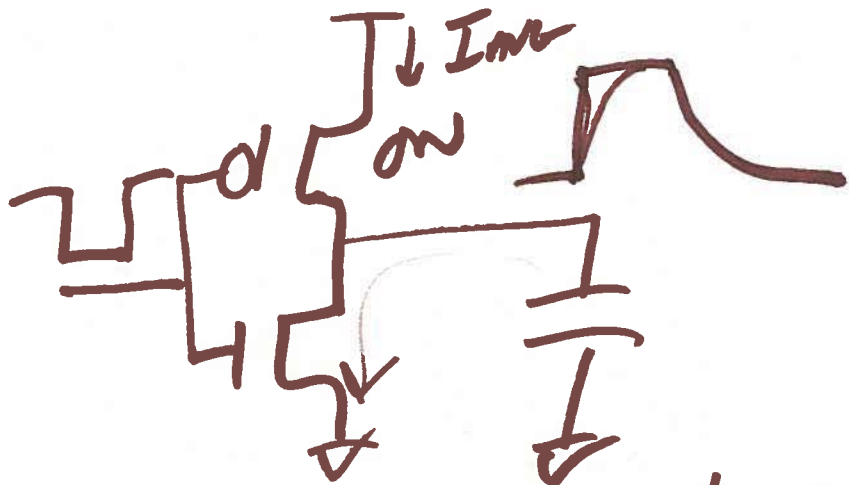
$$I_{avg} = \frac{C_L \cdot V_{DD}}{T_{CLK}}$$

$$I_{avg} = C_L \cdot V_{DD} \cdot f_{CLK}$$

$$P_{avg} = C_L \cdot V_{DD}^2 \cdot f_{CLK}$$

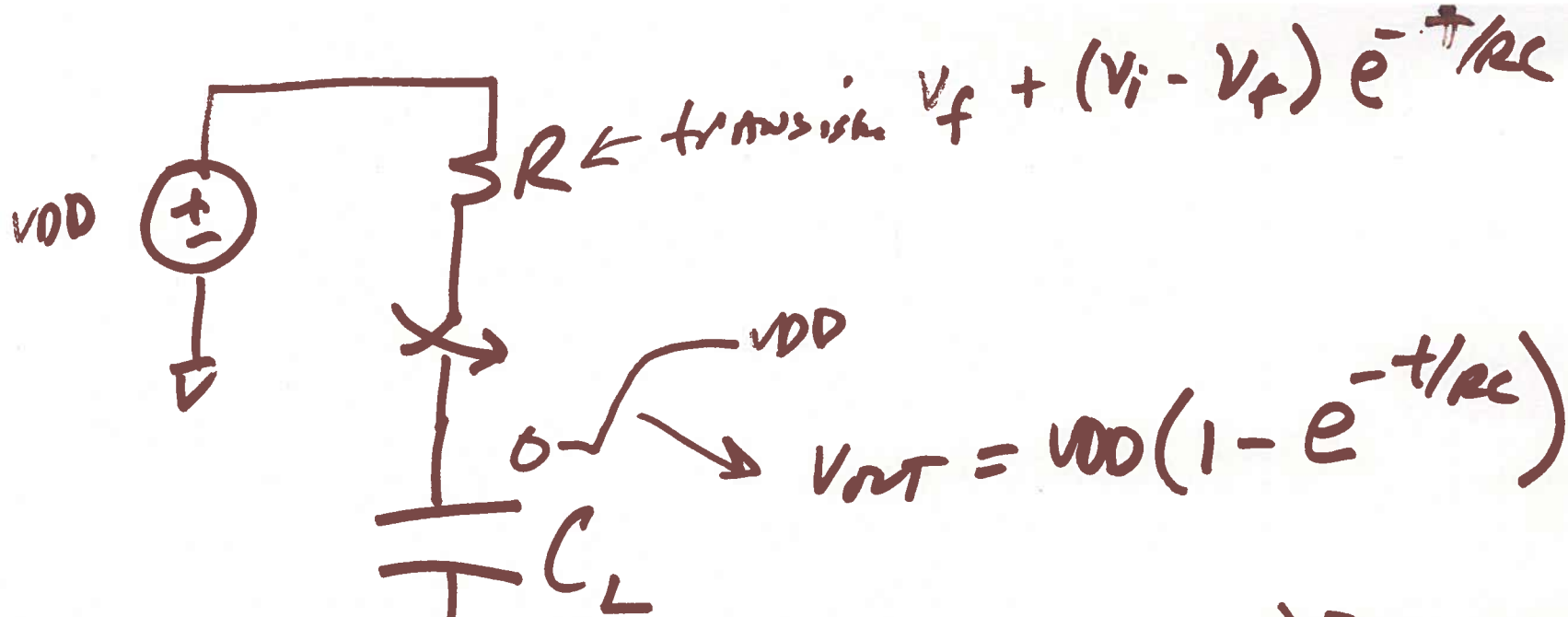
$$E = \frac{1}{2} C_L V_{DD}^2$$

$$P_{avg} = \frac{\frac{1}{2} C_L V_{DD}^2}{T_{CLK}} = \frac{1}{2} C_L V_{DD}^2 f_{CLK}$$



$$P_{PMOS} = \frac{\frac{1}{2} C_L V_{DD}^2}{T_{CLK}}$$

5)



$$P = \frac{v^2}{R} = \frac{(V_{DD} - V_{DD} + e^{-t/RC})^2}{R}$$

$$P_{avg} = \int P(t) dt = \int_0^{T_{CLK}} \frac{V_{DD}^2}{R} e^{-2t/RC} dt = \frac{1}{T_{CLK}} \frac{V_{DD}^2}{R} \int_0^{T_{CLK}} e^{-2t/RC} dt$$

b)

$$P_{avg} = \frac{1}{T_{CLK}} \frac{V_{DD}^2}{R} \int_0^{T_{CLK}} e^{-\frac{2}{RC} \cdot t} \cdot dt$$

$$\text{let } u = -\frac{2t}{RC} \quad \left\{ \begin{array}{l} du = -\frac{2}{RC} dt \\ dt = \frac{RC}{-2} du \end{array} \right.$$

$$= \frac{1}{T_{CLK}} \frac{V_{DD}^2}{R} \frac{RC}{-2} \int_0^{-\frac{2 T_{CLK}}{RC}} e^u du$$

$$= \frac{1}{T_{CLK}} \frac{V_{DD}^2}{R} \frac{RC}{-2} \left[e^{-\frac{2}{RC} T_{CLK}} - 1 \right]$$

$$\boxed{= \frac{1}{2} V_{DD}^2 C_L \cdot f_{CLK}}$$

Decoupling CAP

