

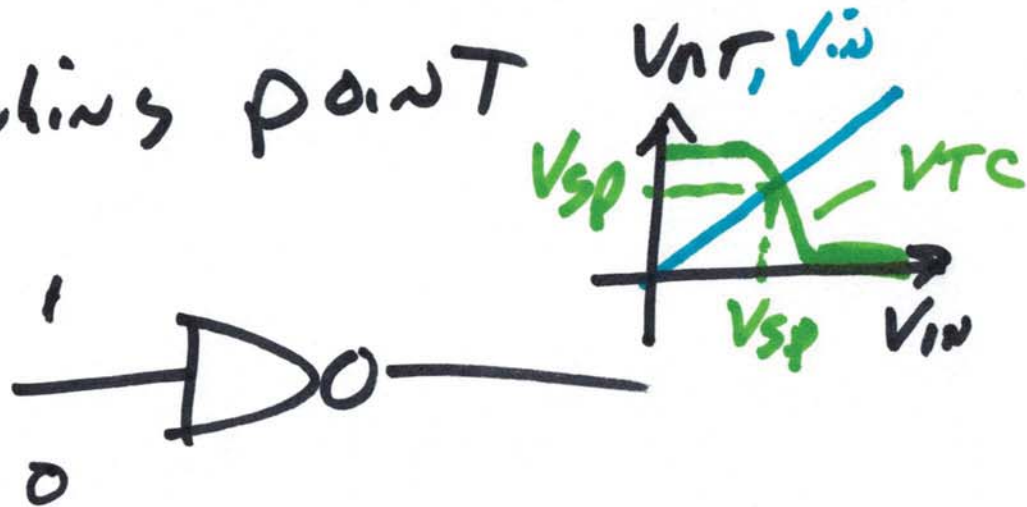
Lecture 18

EE 421 / ELG 621

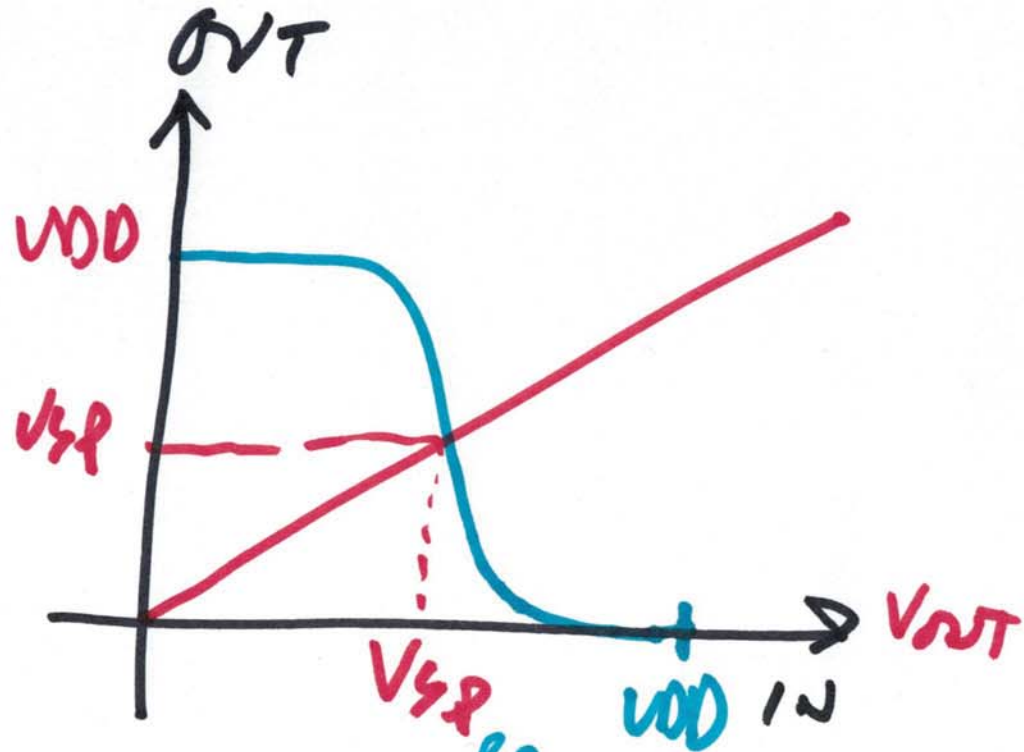
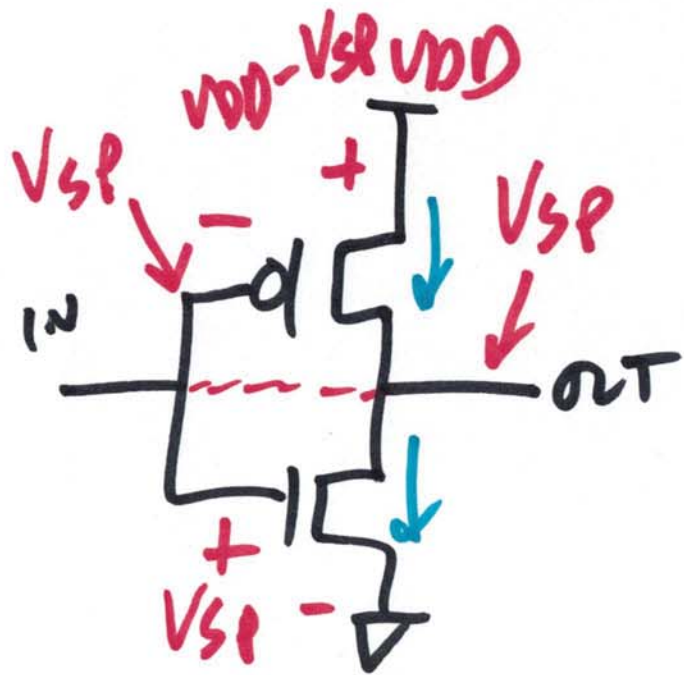
Digital IC Design

OCT. 31, 2018

Inverter  
Switching point



1)



$$\frac{K_{PN}}{2} \frac{W}{L} (\beta_N / 2) (V_{sp} - V_{THN})^2 = \frac{K_{PP}}{2} \frac{W}{L} (\beta_P / 2) (V_{DD} - V_{sp} - V_{THP})^2$$

$$\sqrt{\frac{\beta_N}{\beta_P}} (V_{sp} - V_{THN}) = V_{DD} - V_{sp} - V_{THP}$$

$$V_{sp} \left( \frac{\sqrt{\beta_N}}{\sqrt{\beta_P}} + 1 \right) = V_{DD} - V_{THP} + \sqrt{\frac{\beta_N}{\beta_P}} V_{THN}$$

2)

$$V_{SP} = \frac{V_{DD} - V_{THD} + \sqrt{\frac{\beta_N}{\beta_P}} V_{THN}}{1 + \sqrt{\frac{\beta_N}{\beta_P}}}$$

~~DO~~

$$\beta_N \rightarrow K_{A_n} \cdot \frac{W_n}{L_n}$$

$$\beta_P \rightarrow K_{B_p} \cdot \frac{W_p}{L_p}$$

$$\beta_N \gg \beta_P$$

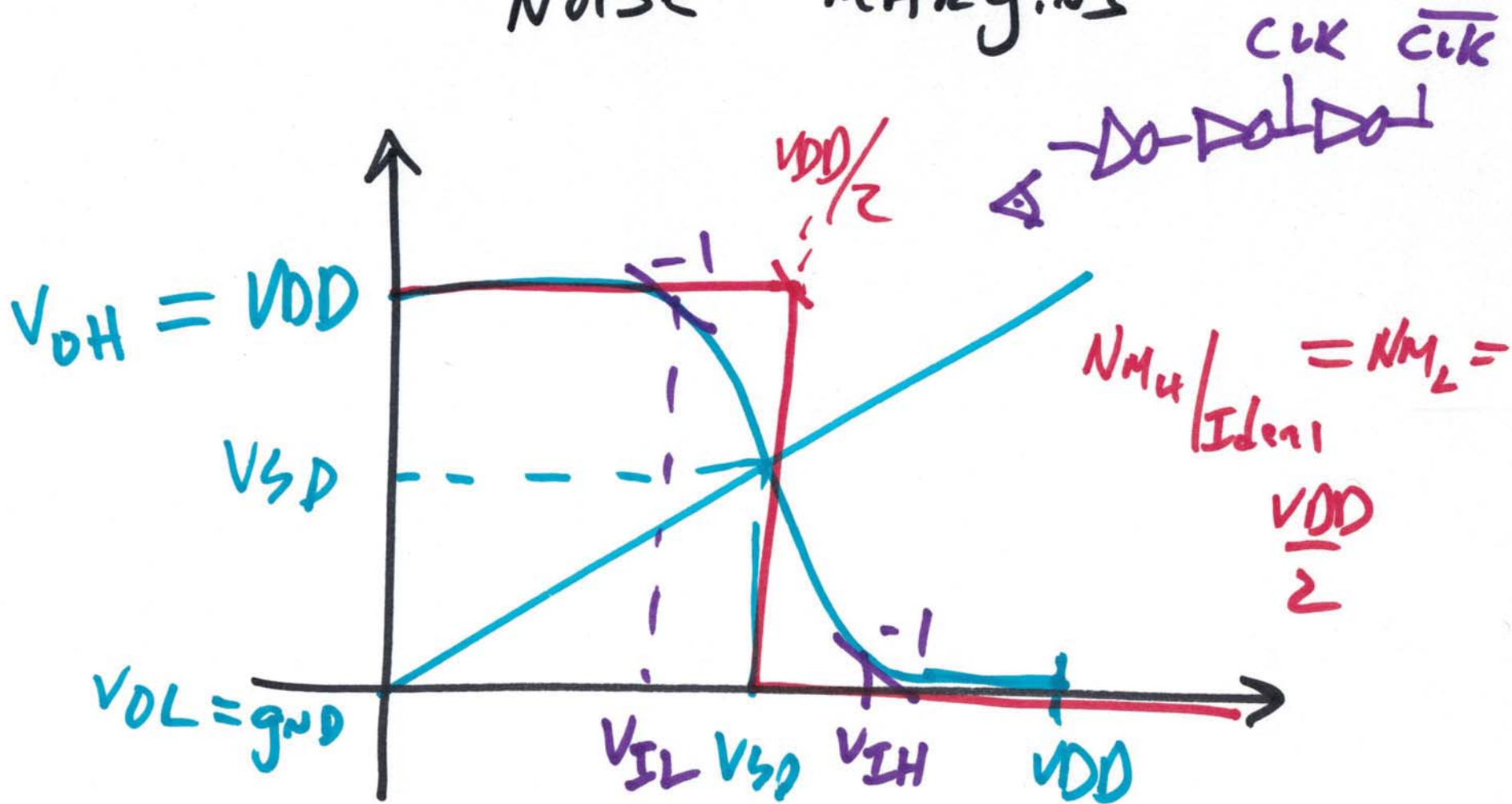
$$V_{SP} \rightarrow V_{THN}$$

$$r_{Dn} = r_{Dn}' \cdot \frac{W_p}{W_n}$$

$$r_{Dn} \gg r_{Dp}$$

3)

# NOISE MARGINS



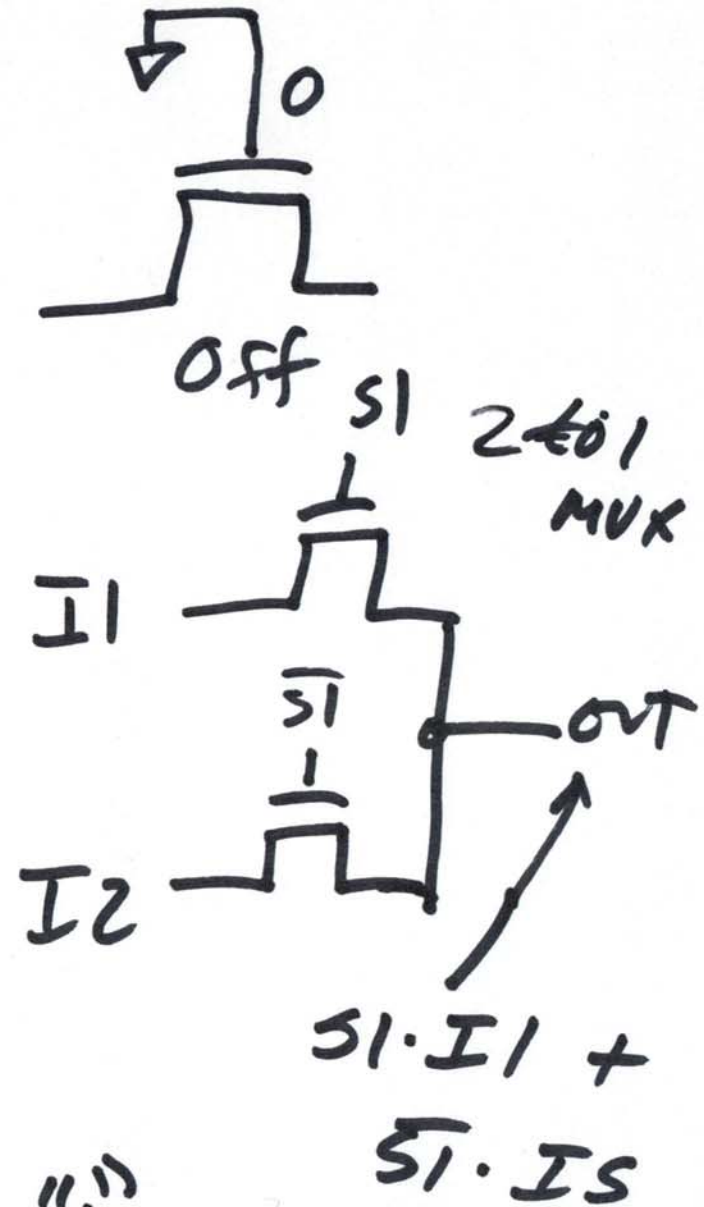
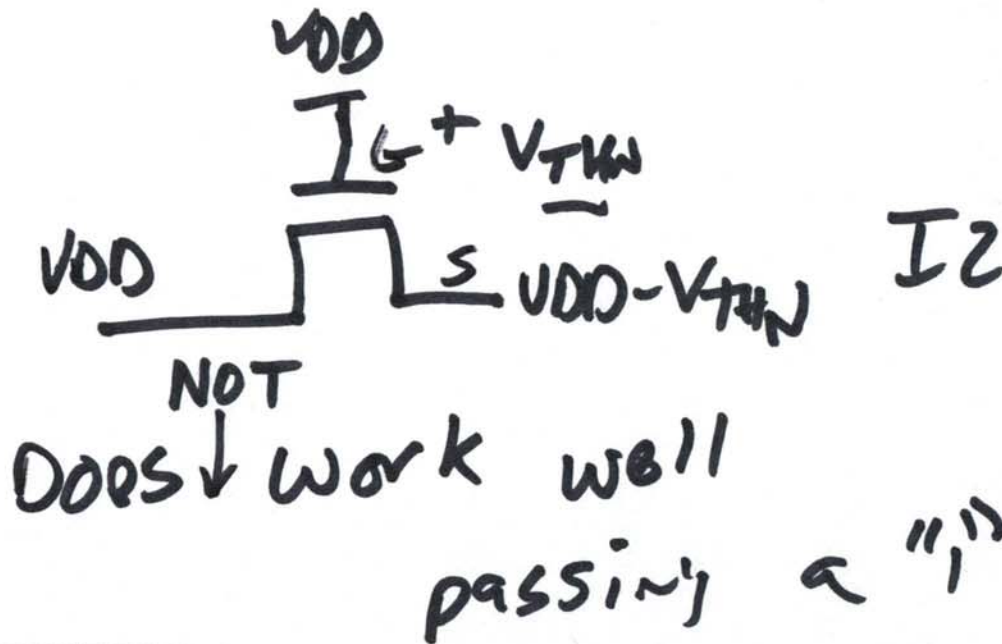
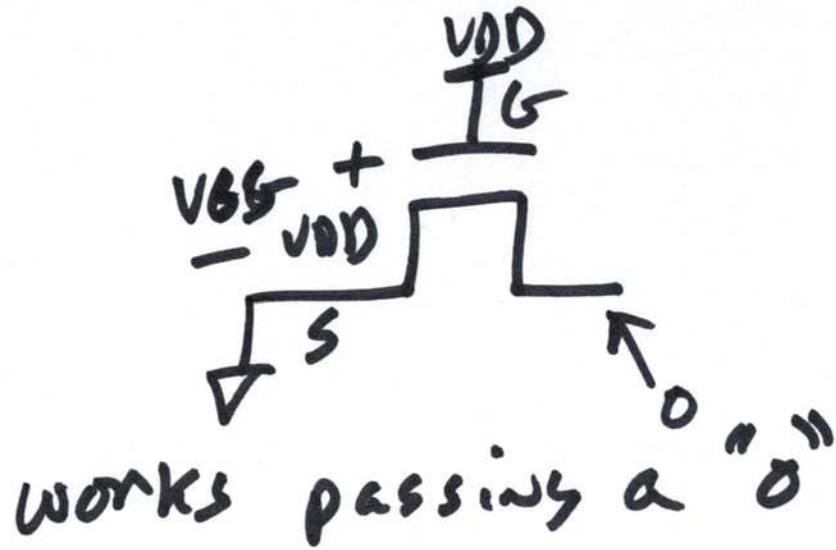
$$NM_H = V_{OH} - V_{IH}$$

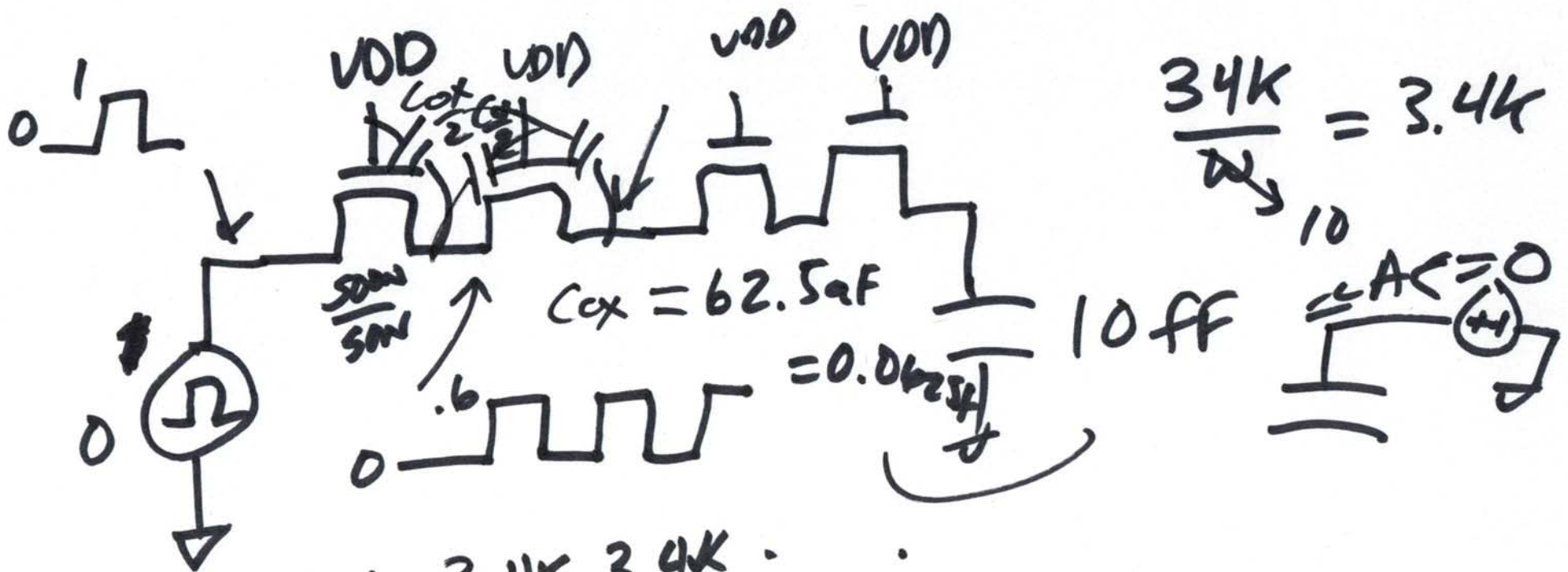
$$NM_L = V_{IL} - V_{OL}$$

4)



# NMOS Pass Gate

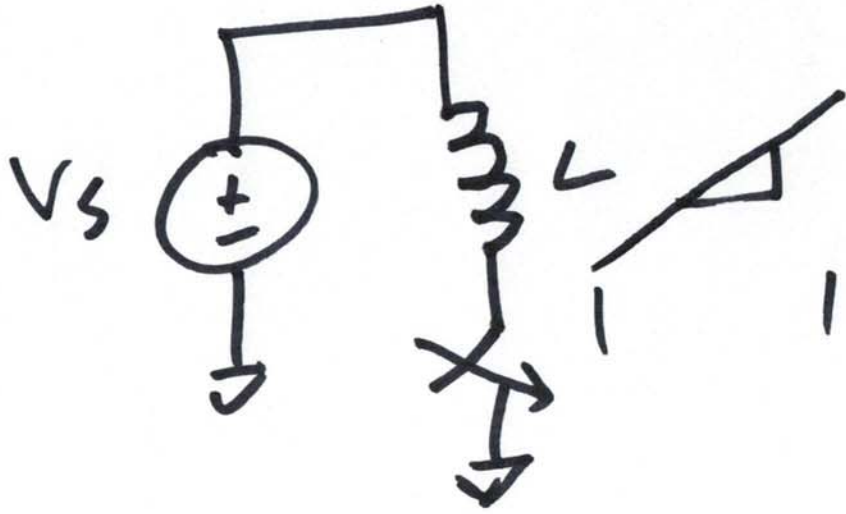




$0.7 \cdot \frac{4}{2} \cdot 3.4k \cdot 62.5 \text{ aF} +$   
 $0.7 \cdot 4 \cdot 3.4k \cdot 10 \text{ fF}$

$34 \text{ ps} \cdot 2.8$   
90 ps

6)



$$V = L \cdot \frac{di}{dt}$$

$$V_s = L \cdot \frac{di}{dt}$$

$i(t)$

switch closes

$$i(t) = \int_0^t i(t) = \int_0^t \frac{V_s}{L} \cdot dt$$

$$i(t) = \frac{V_s}{L} \cdot t$$

switch  
closed

7)

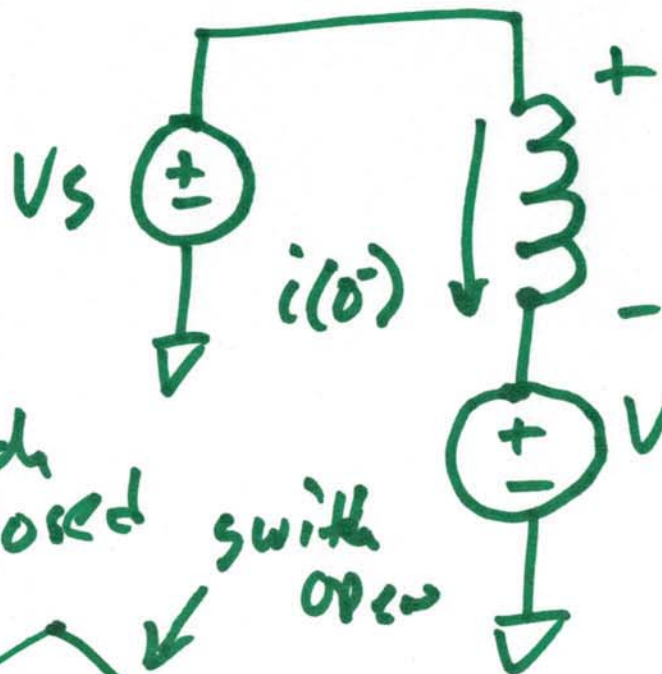
Switch open

$$V = L \frac{di}{dt}$$

$$V_S - V_{out} = L \cdot \frac{di}{dt}$$

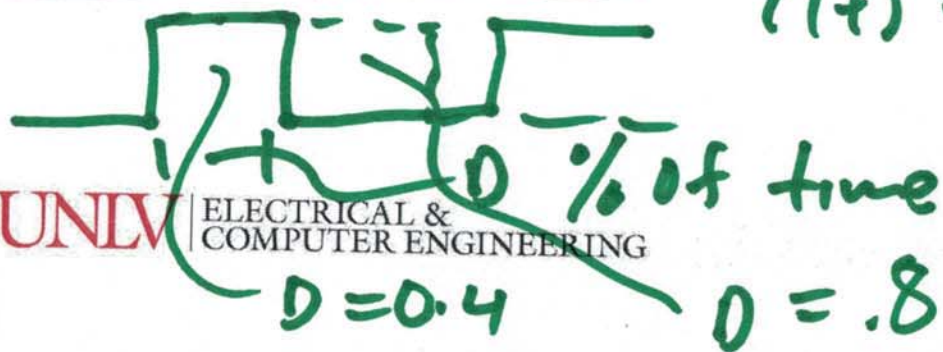
$$\int_{i(0^-)}^{i(t)} di = \int_0^t \frac{V_S - V_{out}}{L} dt$$

$$i(t) = \frac{V_S - V_{out}}{L} \cdot t + i(0^-)$$

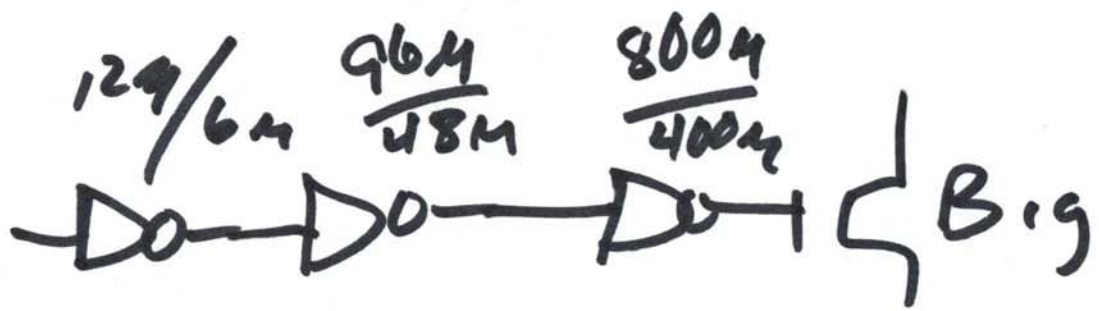
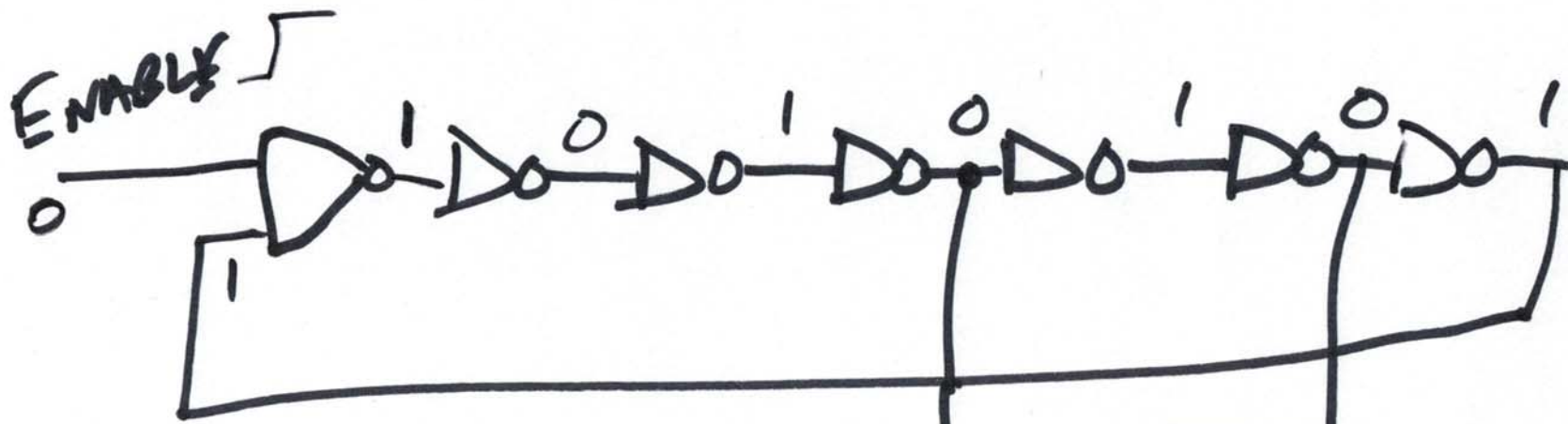


Switch closed  
Switch open

$$V_{out} = V_S \cdot \frac{1}{1-D}$$







$$D = \frac{1}{2}$$

$$\frac{3.47}{1 - D^2} = 7.4$$

2)