

EE 422 ECG 622

Analog IC Design

April 3, 2013

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Lecture 17

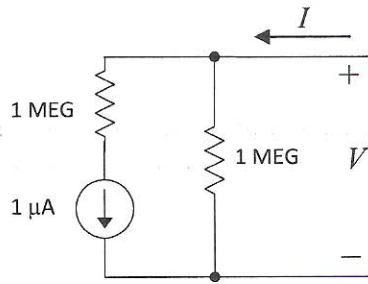
$$\frac{5 - V_x}{100k} = 1.2A \cdot 0.3 \cdot V_x \text{ for } V_x \text{ small}$$

$$5 - V_x = \frac{10^5 \cdot 360 \cdot 10^{-6}}{100k} \cdot V_x = 36 \cdot V_x$$

$$5 = (1 + 36)V_x$$

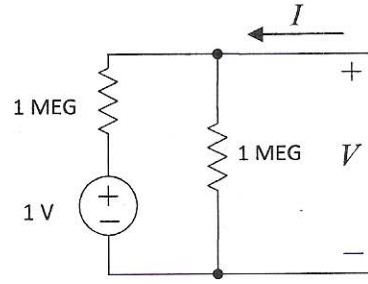
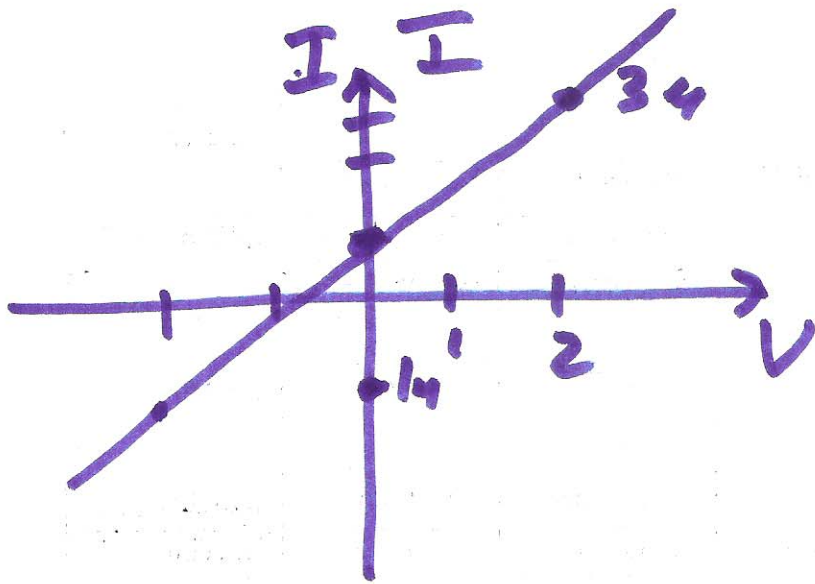
$$V_x = \frac{5}{37} \approx \underline{\underline{.13V}}$$

1. Determine equations for how the current, I in the following circuits, changes with changes in the voltage, V . Sketch the change in I for V changing from -2 V to $+2$ V. (20 points)



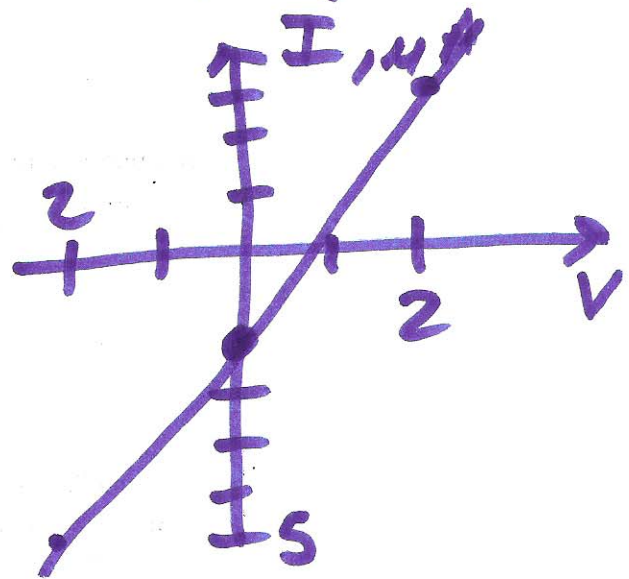
$$I = \frac{V}{10^6} + 10^{-6}$$

$$= 10^{-6}(V+1)$$



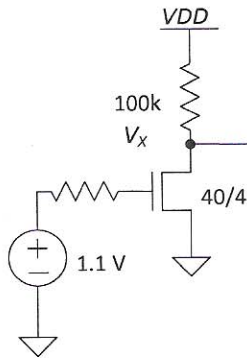
$$I = \frac{V}{10^6} + \frac{V-1}{10^6}$$

$$= 10^{-6}(2V-1)$$



2)

2. Determine V_x in each of the following. Show your work for credit. (20 points)



$$V_{GS} = 1.1$$

Assume SAT.

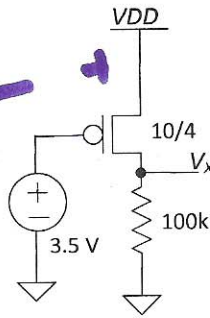
$$I_D = \frac{40}{4} \cdot \frac{120 \mu\text{A/V}}{2} (1.1 - 0.8)^2$$

$$I_D = \frac{1.2 \mu\text{A}}{2} \cdot 3^2 = 600 \mu\text{A} \cdot 0.9 = 540 \mu\text{A}$$

$V_D = 5 - 540 \cdot 100\text{k} < 0$
Not in saturation
in triode

$$I_D = \frac{V_{DD} - V_x}{100\text{k}} = \frac{120 \mu\text{A}}{V} \cdot \frac{40}{4} \left((1.1 - 0.8) - \frac{V_x}{2} \right)^2$$

3)



$$V_{SG} = 5 - 3.5 = 1.5$$

$$I_D = \frac{40 \mu\text{A/V}}{2} \cdot \frac{10}{4} \cdot (1.5 - 0.9)^2$$

$$= 50 \mu\text{A} \cdot 0.36$$

$$= 18 \mu\text{A}$$

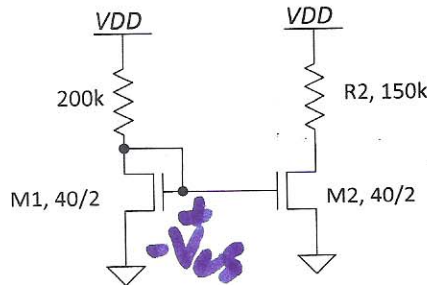
$$V_x = 100\text{k} \cdot 18 \mu\text{A}$$

$$= 1.8 \text{ V}$$

YPS
 $V_{SD} \geq V_{SG}$
✓

3. Calculate the currents and voltages in the following circuit. What is the maximum value allowed for R2 so that M2 remains operating in the saturation region? Show your work for credit. (20 points)

$$\begin{array}{r} 240 \\ .6 \\ \hline 1440 \end{array} \quad \begin{array}{r} 240 \\ 144 \\ \hline 384 \end{array}$$



$$\begin{array}{r} 240 \\ .6 \\ \hline 144.0 \\ 240 \\ .04 \\ \hline 29.60 \end{array}$$

$$\frac{V_{DD} - V_{GS}}{200k} = \frac{120 \mu A/V \cdot 40}{2} \left(V_{GS} - 0.8 \right)^2$$

$$5 - V_{GS} = 1.2 \frac{\mu A}{V} (V_{GS} - 0.8)^2 \cdot 200k$$

$$5 - V_{GS} = 240 (V_{GS}^2 - 1.6V_{GS} + 0.64)$$

$$\begin{array}{r} 153.6 \\ 148.8 \\ -5 \\ \hline 148.6 \end{array}$$

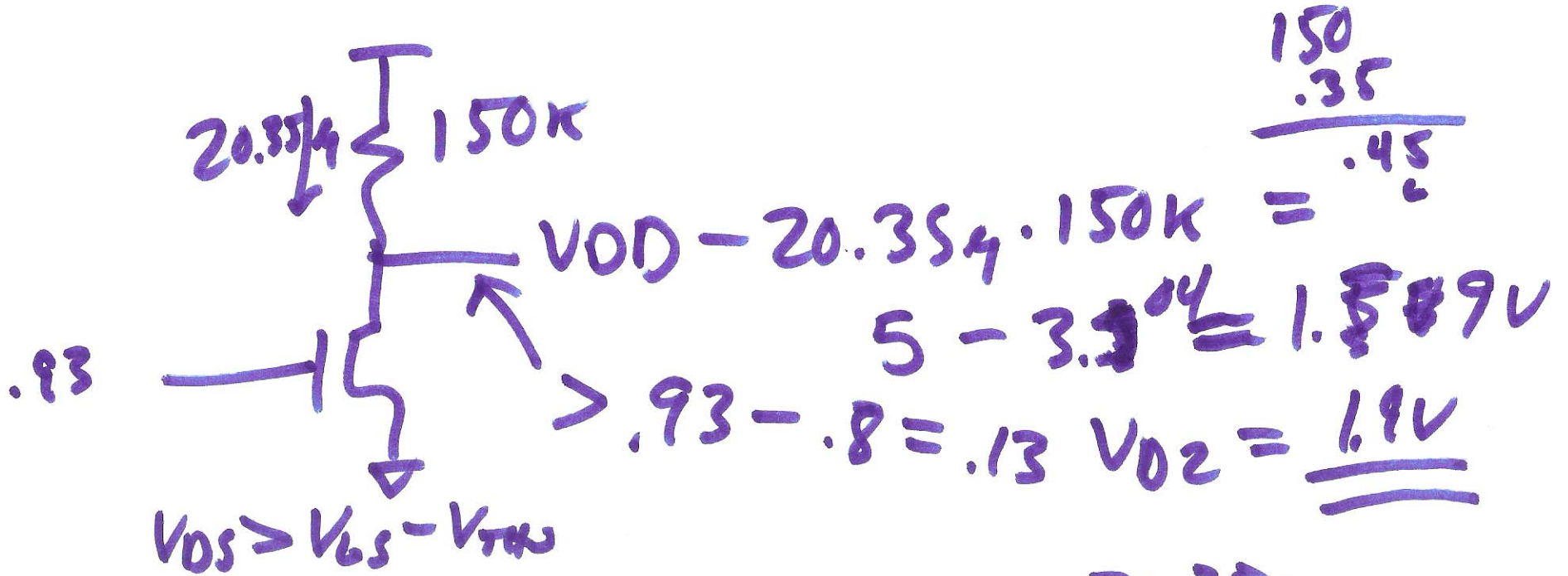
$$0 = 240V_{GS}^2 - 383V_{GS} + 153.6$$

$$V_{GS} = \frac{383 \pm \sqrt{(383)^2 - 4 \cdot 240 \cdot 153.6}}{2 \cdot 240}$$

$$\underline{\underline{V_{GS} = 0.93}}$$

4)

$$I_D = \frac{5 - .93}{200k} = \frac{4.07}{200k} = \underline{\underline{20.35 \mu A}}$$



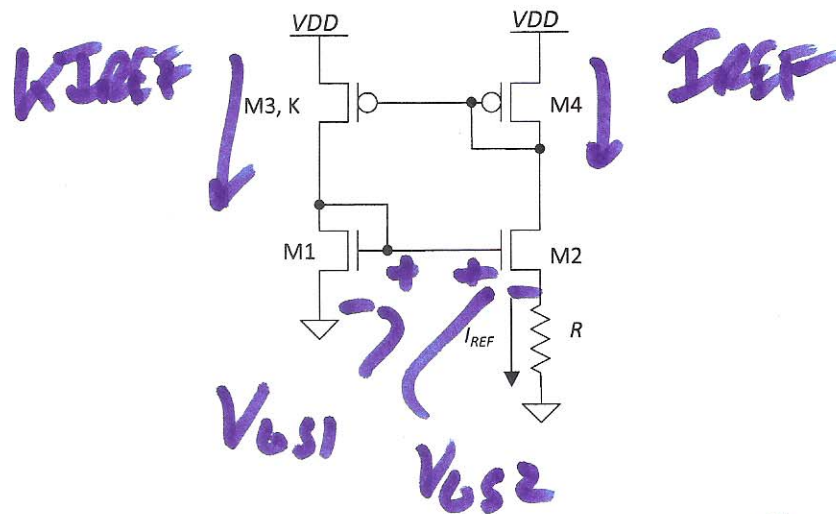
$$I_D \approx \frac{5 - .13}{R_{D,MAX}} = I_D \uparrow 20.35 \mu A$$

$$R_{D,MAX} = \frac{5 - .13}{20.354} = \frac{4.87}{20.35 \mu A} \approx \underline{\underline{240k}}$$

$R_{D,MAX} \approx 240k$

5)

4. Derive an equation for I_{REF} in the following circuit. Note that M3 is K times wider than M4 and M1 and M2 are the same size. (20 points)



$$V_{GS1} = V_{GS2} + I_{REF} \cdot R$$

$$\sqrt{\frac{2KI_{REF}}{\beta_N}} + V_{THN} = \sqrt{\frac{2I_{REF}}{\beta_N}} + V_{THN} + I_{REF} \cdot R$$

$$\sqrt{\frac{2I_{REF}}{\beta_N}} (\sqrt{K} - 1) = I_{REF} \cdot R$$

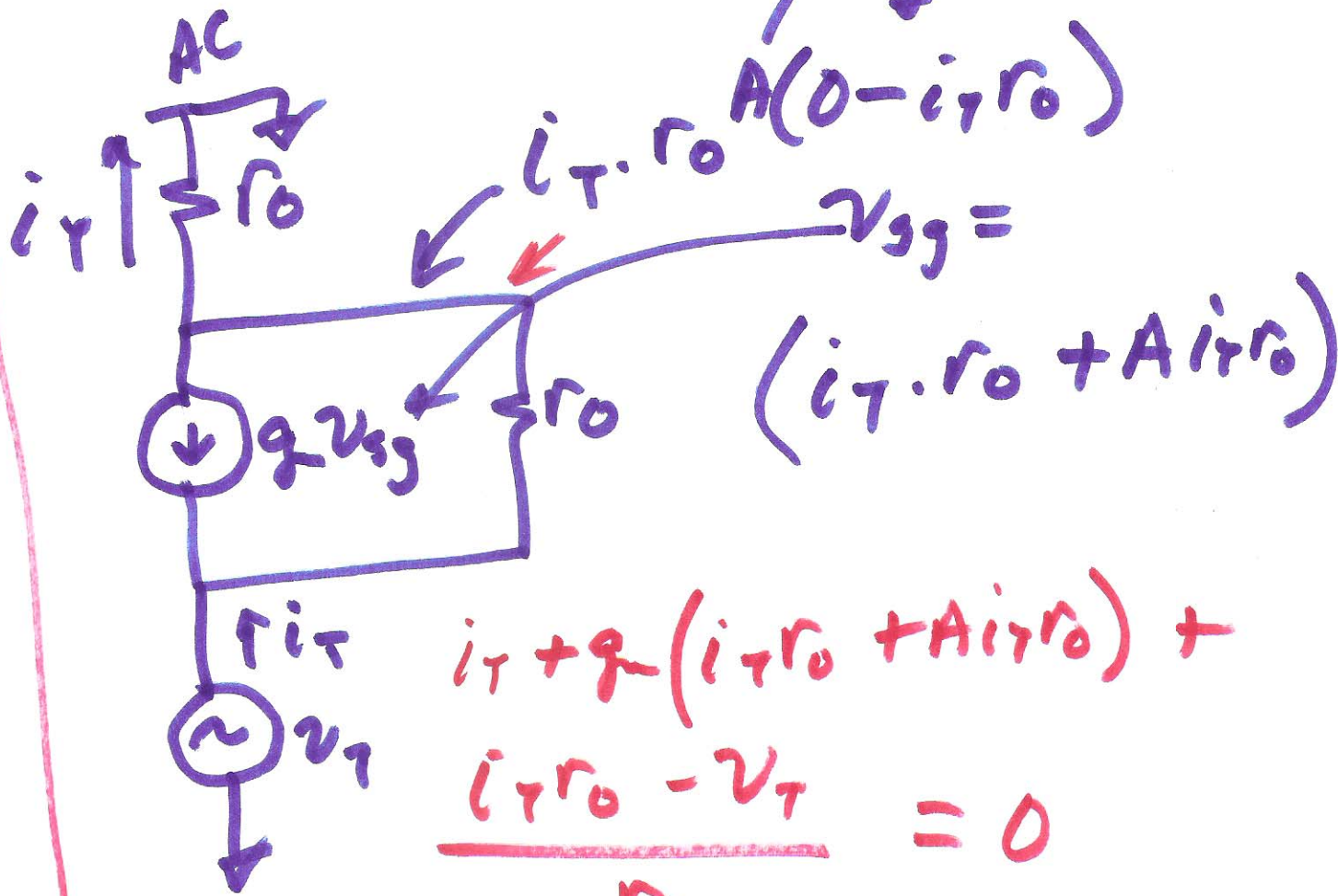
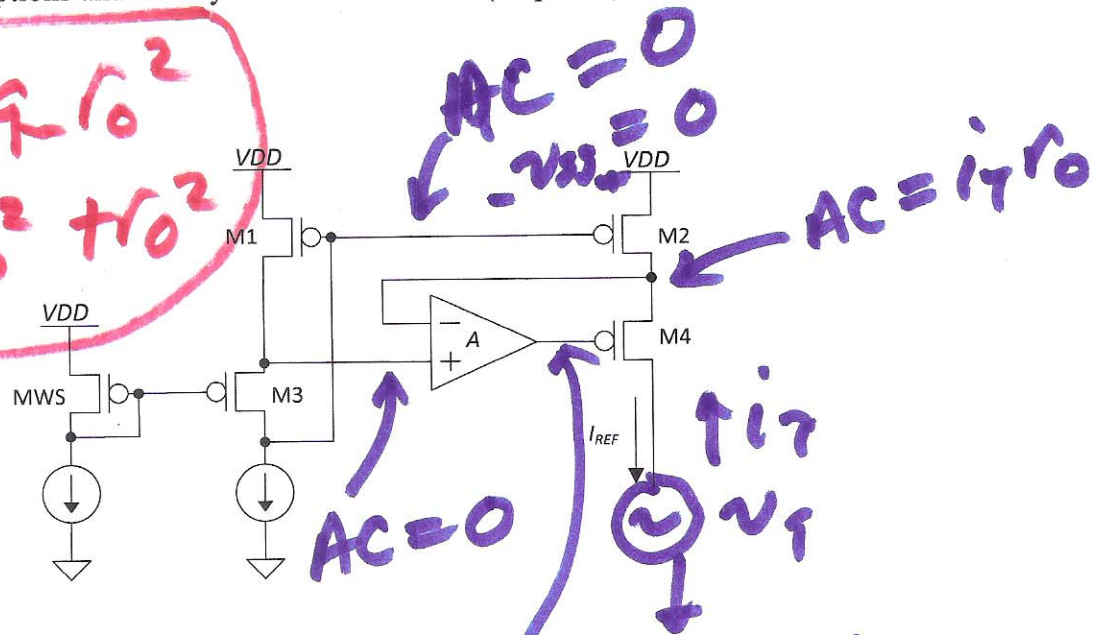
$$\sqrt{\frac{2}{\beta_N}} (\sqrt{K} - 1) = \sqrt{I_{REF}} \cdot R$$

$$\frac{2}{\beta_N \cdot R^2} (\sqrt{K} - 1)^2 = I_{REF}$$

6)

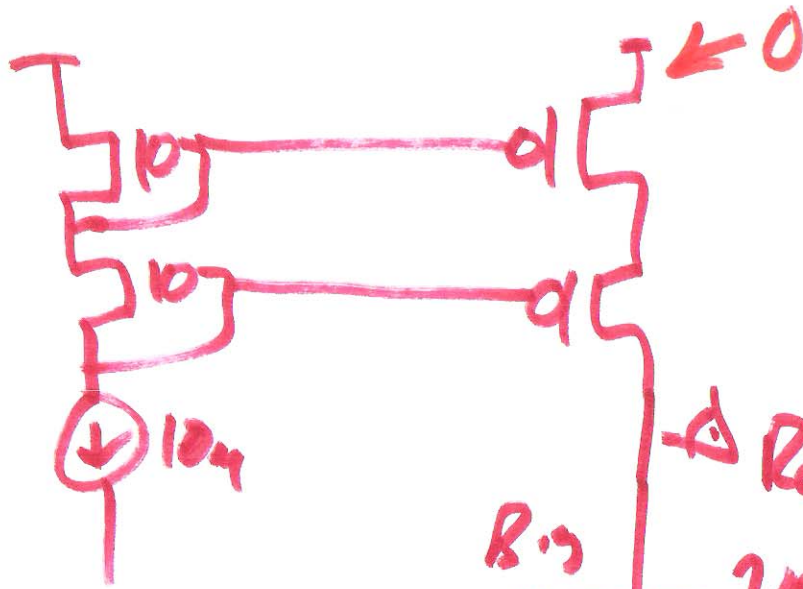
5. Show how to determine the small-signal output resistance of the following current mirror. State all assumptions and show your work for credit. (20 points)

$$\frac{v_T}{i_T} = r_o + g_m r_o^2 + g_m A r_o^2 + r_o^2$$



$$v_T = r_o (i_T + i_T g_m r_o + i_T g_m A r_o + i_T r_o)$$

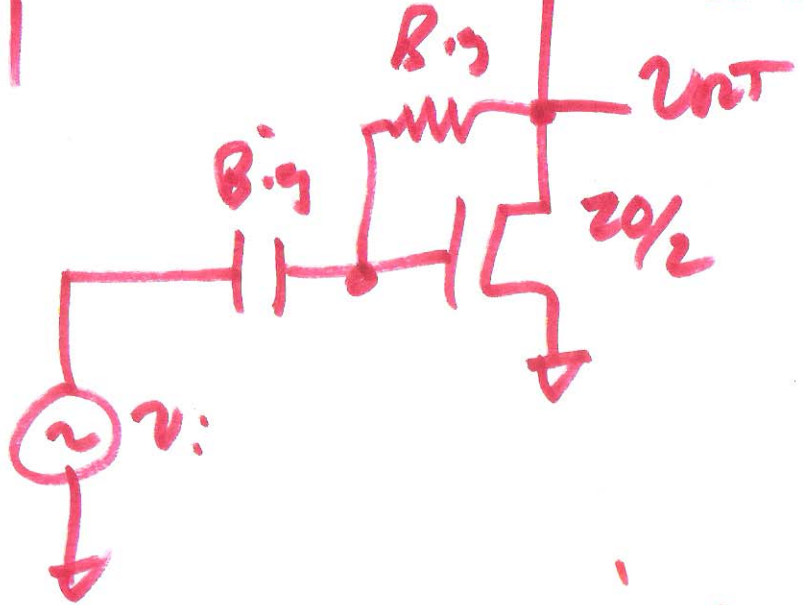
A21.6



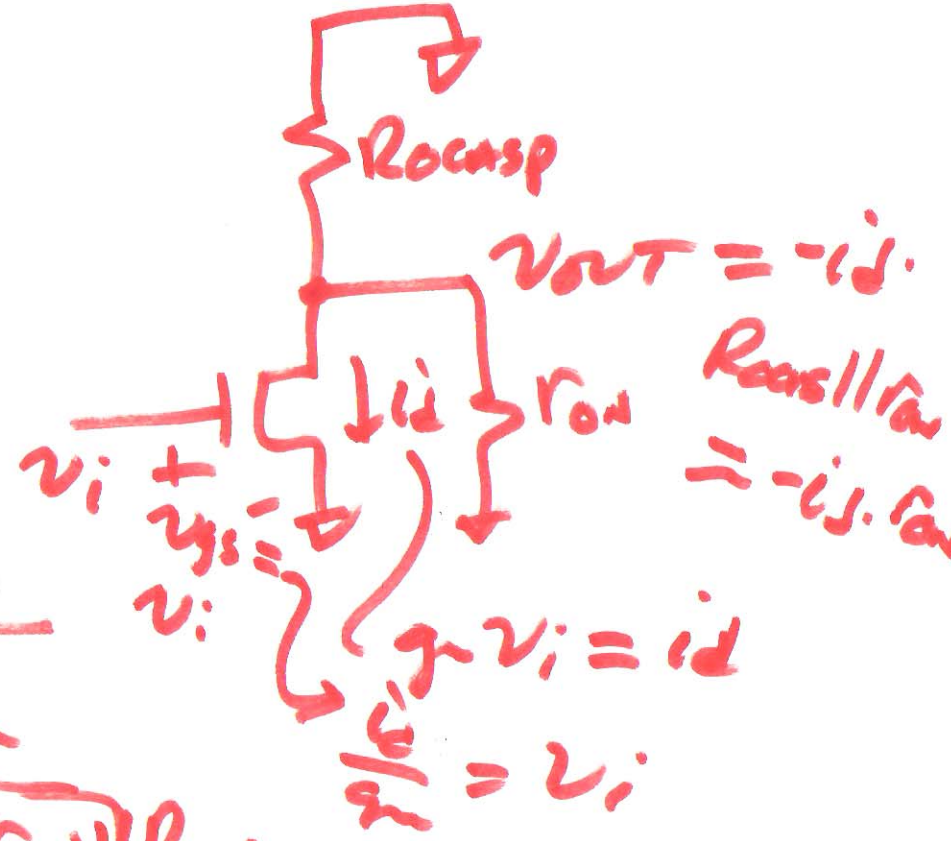
$$g_m = \sqrt{2I_Q \cdot \beta_P}$$

$$r_o = \frac{1}{\lambda I_Q}$$

$$R_{ocasp} = g_m r_o^2$$



$$A_v = \frac{v_{out}}{v_i} = -\frac{i_c \cdot r_{ov}}{i_d / g_m}$$

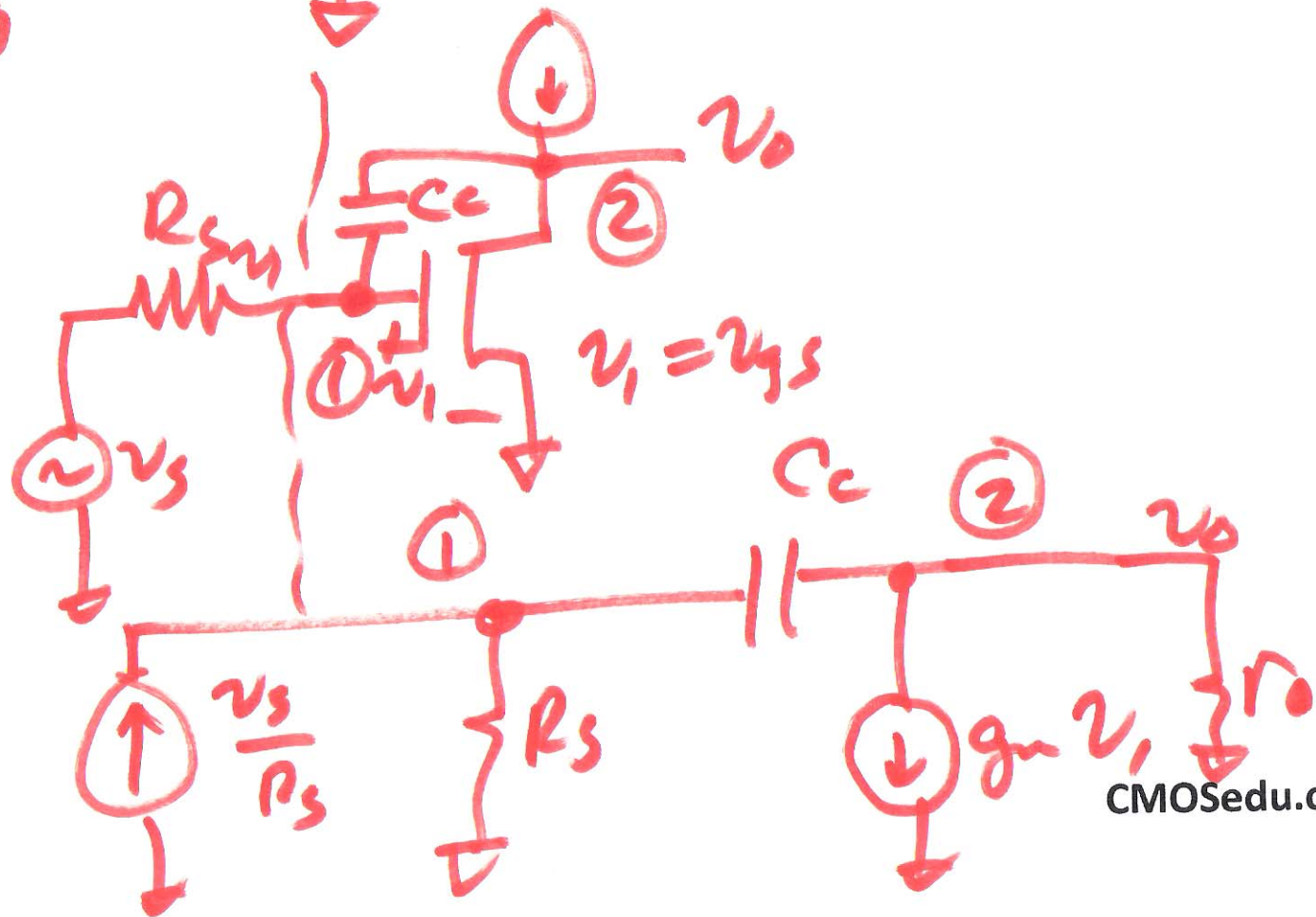
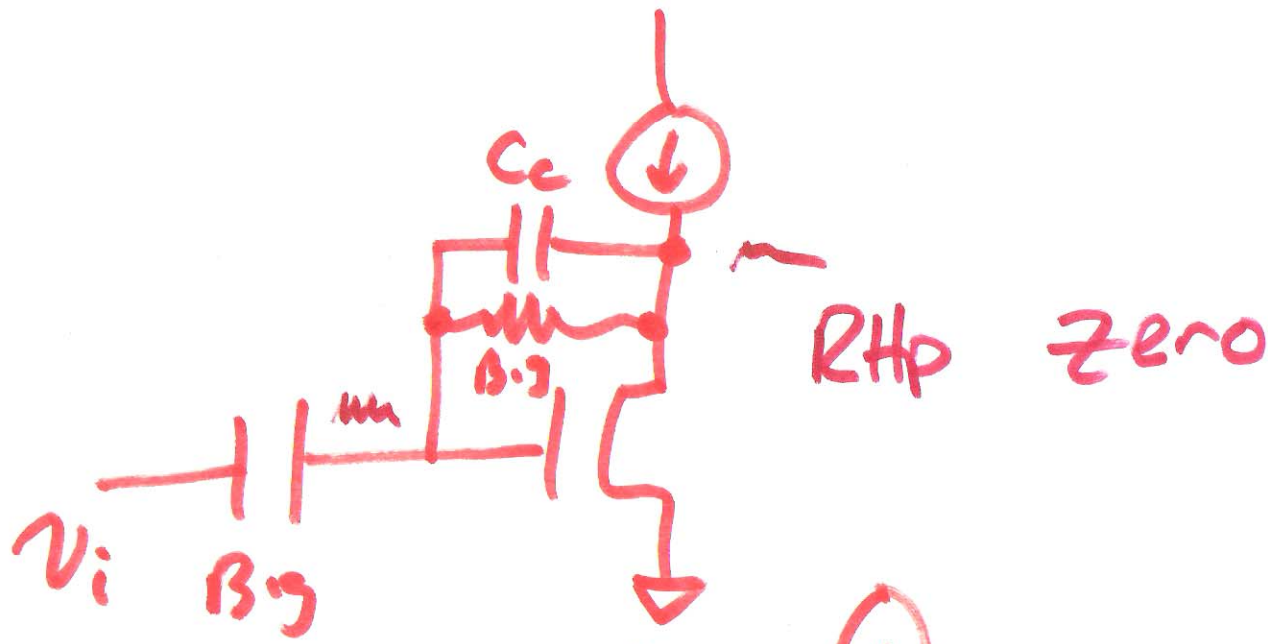


$$v_{out} = -i_d \cdot R_{ocasp} \parallel r_{ov}$$

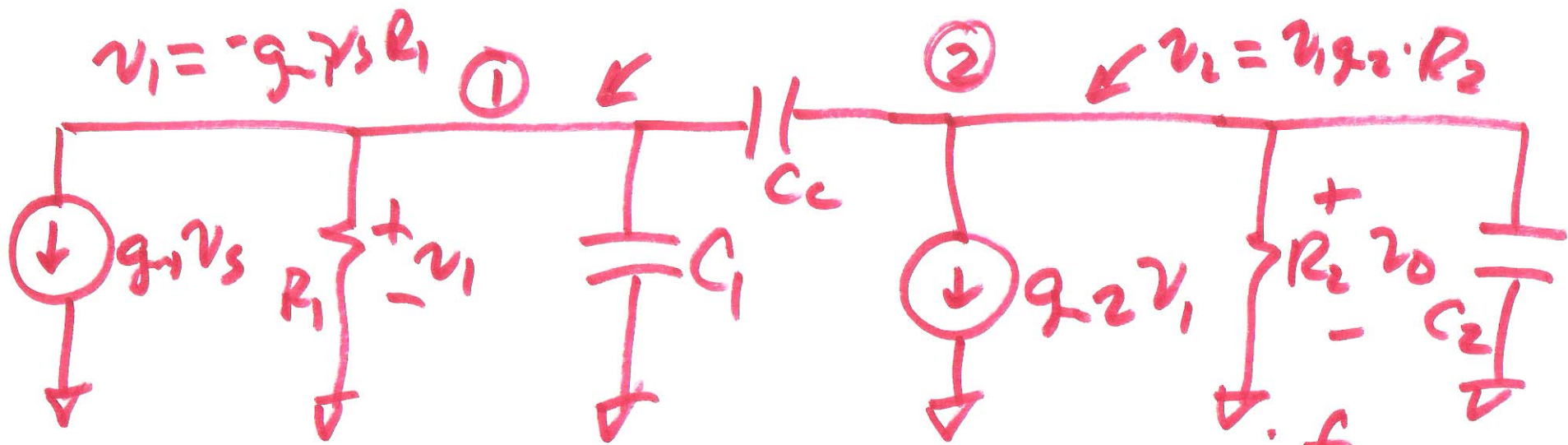
$$= -i_d \cdot r_{ov}$$

$$A_v = -g_m r_{ov} \parallel R_{ocasp}$$

8)



a)



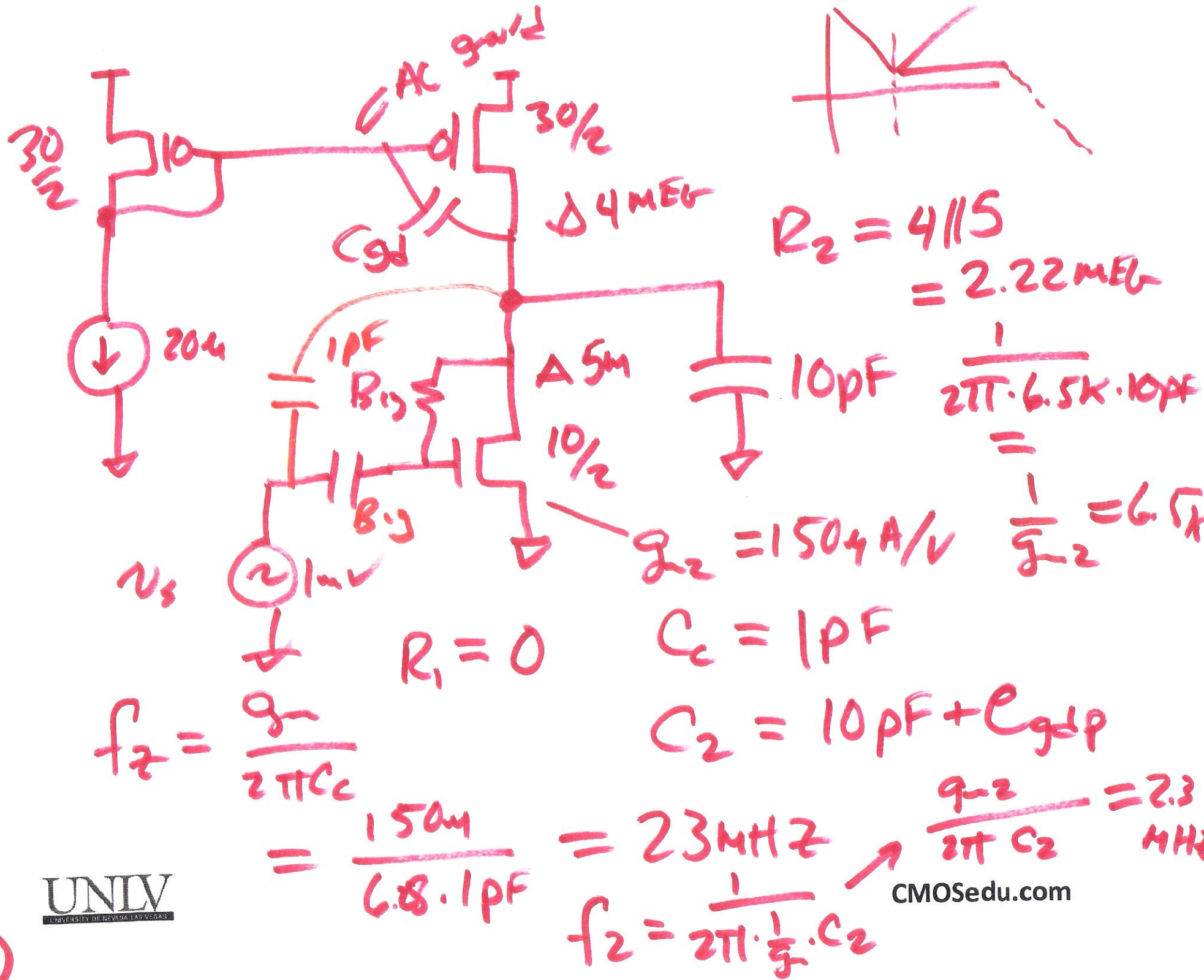
$$A_v(f) = \frac{v_{out}}{v_s} = g_{m1} R_1 \cdot g_{m2} R_2 \cdot \frac{1 - j \frac{f}{f_2}}{(1 + j \frac{f}{f_1})(1 + j \frac{f}{f_2})}$$

$$f_1 = \frac{2\pi [(C_c + C_2)R_2 + (C_1 + C_c(1 + g_{m2}R_2)) \cdot R_1]}{1}$$

$$\approx \frac{2\pi g_{m2} R_2 R_1 C_c}{1}$$

$$f_2 \approx \frac{g_{m2} C_c}{1}$$

$$\frac{2\pi (C_c C_1 + C_1 C_2 + C_c C_2)}{1}$$



$$R_2 = 4 || 5 = 2.22 \text{ M}\Omega$$

$$\frac{1}{2\pi \cdot 6.5 \text{ K} \cdot 10 \text{ pF}} = \frac{1}{f_z} = 6.5 \text{ K}$$

$$g_{m2} = 150 \mu\text{A/V}$$

$$f_z = \frac{g_m}{2\pi C_c} = \frac{150 \mu\text{A}}{6.8 \cdot 1 \text{ pF}} = 23 \text{ MHz}$$

$$C_2 = 10 \text{ pF} + C_{gd}$$

$$f_2 = \frac{g_{m2}}{2\pi C_2} = 2.3 \text{ MHz}$$

$$f_2 = \frac{1}{2\pi \cdot \frac{1}{g_m} \cdot C_2}$$

11)

$$\begin{aligned}
 f_1 &= \frac{1}{2\pi R_2 C_C} \\
 &= \frac{1}{2\pi \cdot 2.2 \text{e}6 \cdot 1 \text{pF}} \\
 &= \frac{1}{2\pi \cdot 10^{-6} \cdot 2.2} = \frac{159 \text{kHz}}{2.2} \\
 &\approx \frac{72 \text{kHz}}{2}
 \end{aligned}$$