

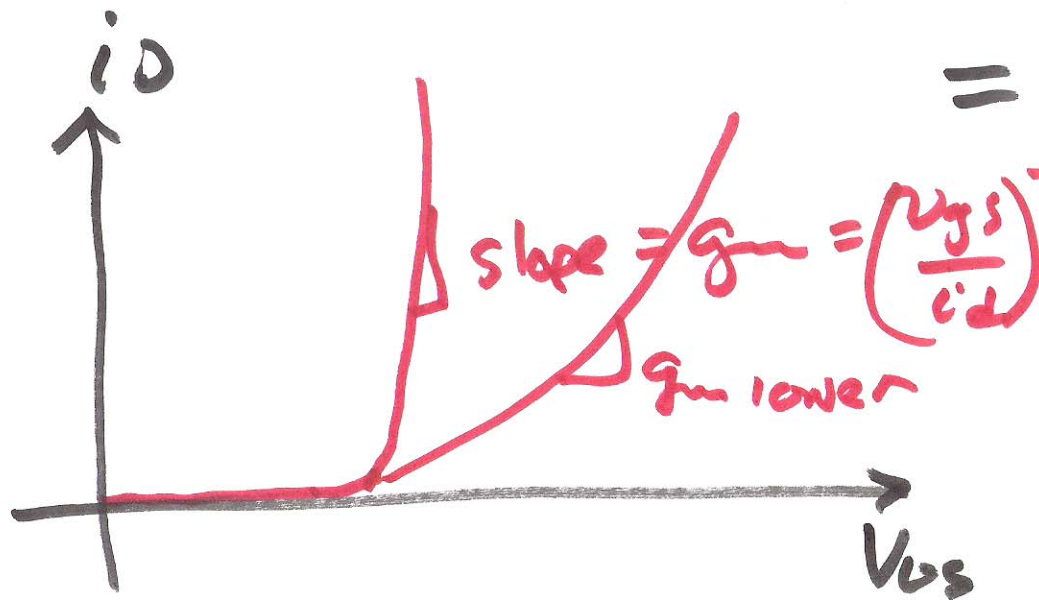
EE 422 AND ECG 622

Analog IC Design

2/6/13 Lecture 5.

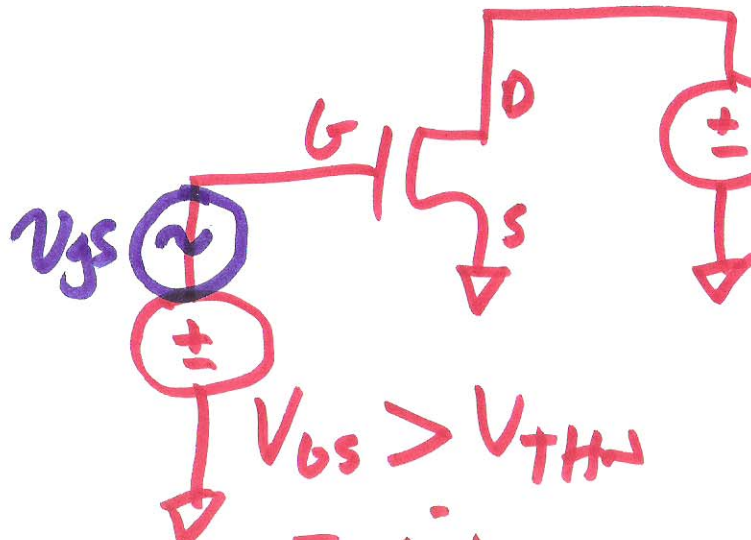
transconductance, $g_m = \frac{\Delta i_D}{\Delta v_{gs}}$

$$= \frac{\delta i_D}{\delta v_{gs}} \cdot \frac{1}{\sqrt{2}}$$



MHOS
SIEMENS

$$\beta_n = \kappa_{pn} \cdot \frac{W}{L}$$

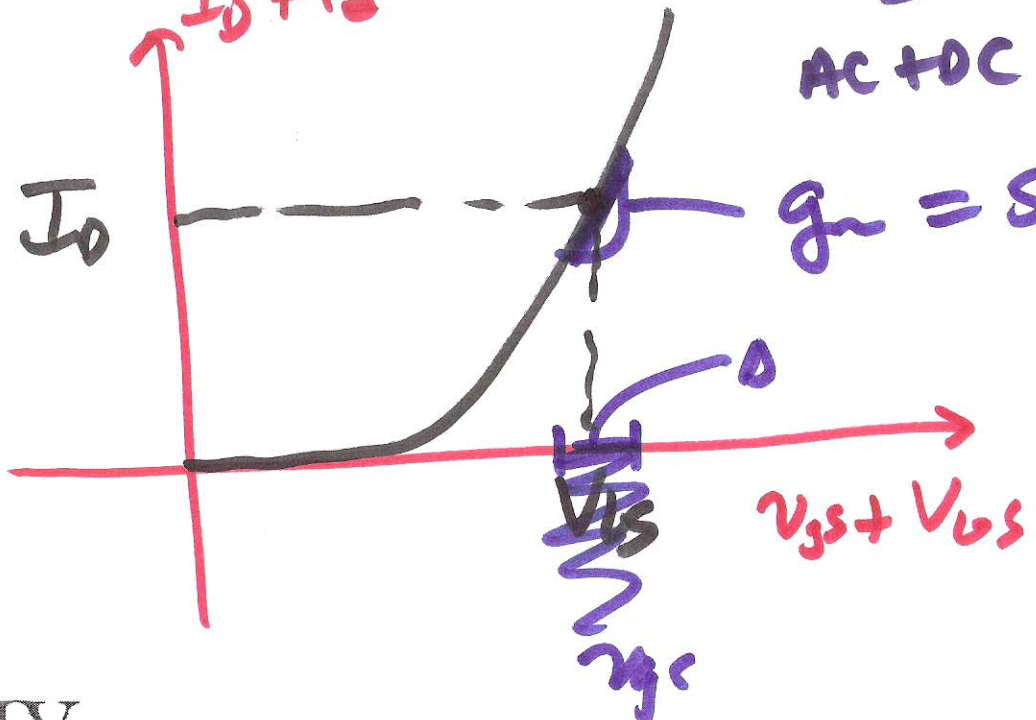


$$V_{DS} > V_{GS} - V_{THN}$$

$$V_{GS} > V_{THN}$$

$$I_0 + i_d = \frac{\kappa_{pn} \cdot W}{2 \cdot L} \left(\underbrace{V_{GS} + v_{gs}}_{\substack{\text{AC+DC} \\ \sim V_{GS}}} - V_{THN} \right)^2$$

I_D
AC+DC

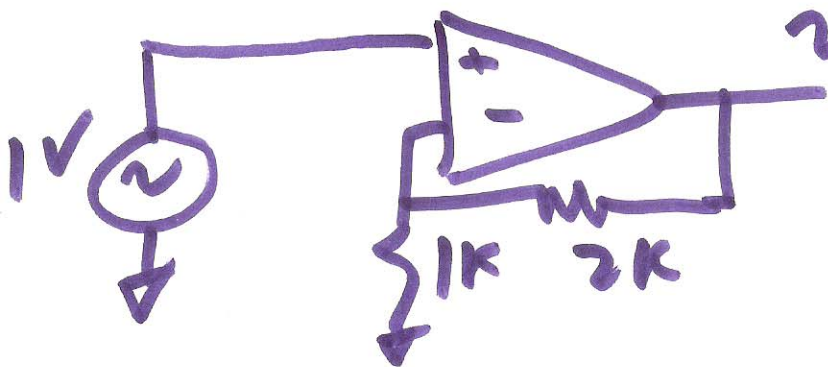


$$g_m = \text{slope}$$

$$\left. \frac{\delta i_d}{\delta v_{GS}} \right|_{\substack{I_D = \text{CONST} \\ V_{DS} = \text{CONST}}} = g_m$$

2)

$$g_m = \frac{\delta i_D}{\delta v_{GS}} \Bigg|_{\substack{I_D = \text{CONST} \\ v_{GS} = \text{CONST}}} = \delta \frac{\beta_N}{2} (v_{GS} - V_{THN})^2$$



$$g_m = 2 \cdot \frac{\beta_N}{2} (v_{GS} - V_{THN}) \frac{\delta (v_{GS} - V_{THN})}{\delta v_{GS}}$$

$$r_o = \frac{1}{\lambda I_{DSAT}}$$

$$g_m = \beta_N (v_{GS} - V_{THN})$$

$$= \beta_N (v_{GS} + v_{gs} - V_{THN})$$

$v_{GS} \gg v_{gs} \Rightarrow$ small-signal approx.

$$g_m \approx \beta_N (v_{GS} - V_{THN})$$

3)

$$r_o = \frac{1}{\lambda I_{D,SAT}}$$

$$g_m = \beta_n (V_{GS} - V_{THN}) = \left(\sqrt{\beta_n} \right)^2 \sqrt{\frac{2I_D}{\beta_n}}$$

$$I_D = \frac{\beta_n}{2} (V_{GS} - V_{THN})^2 = \sqrt{\frac{2I_D \beta_n^2}{\beta_n}}$$

$$\frac{A(B+c)}{D \cdot E} = \frac{F}{G}$$

$$A = \frac{F \cdot D \cdot E}{G \cdot (B+c)}$$

$$\frac{1}{1} = \frac{1}{A}$$

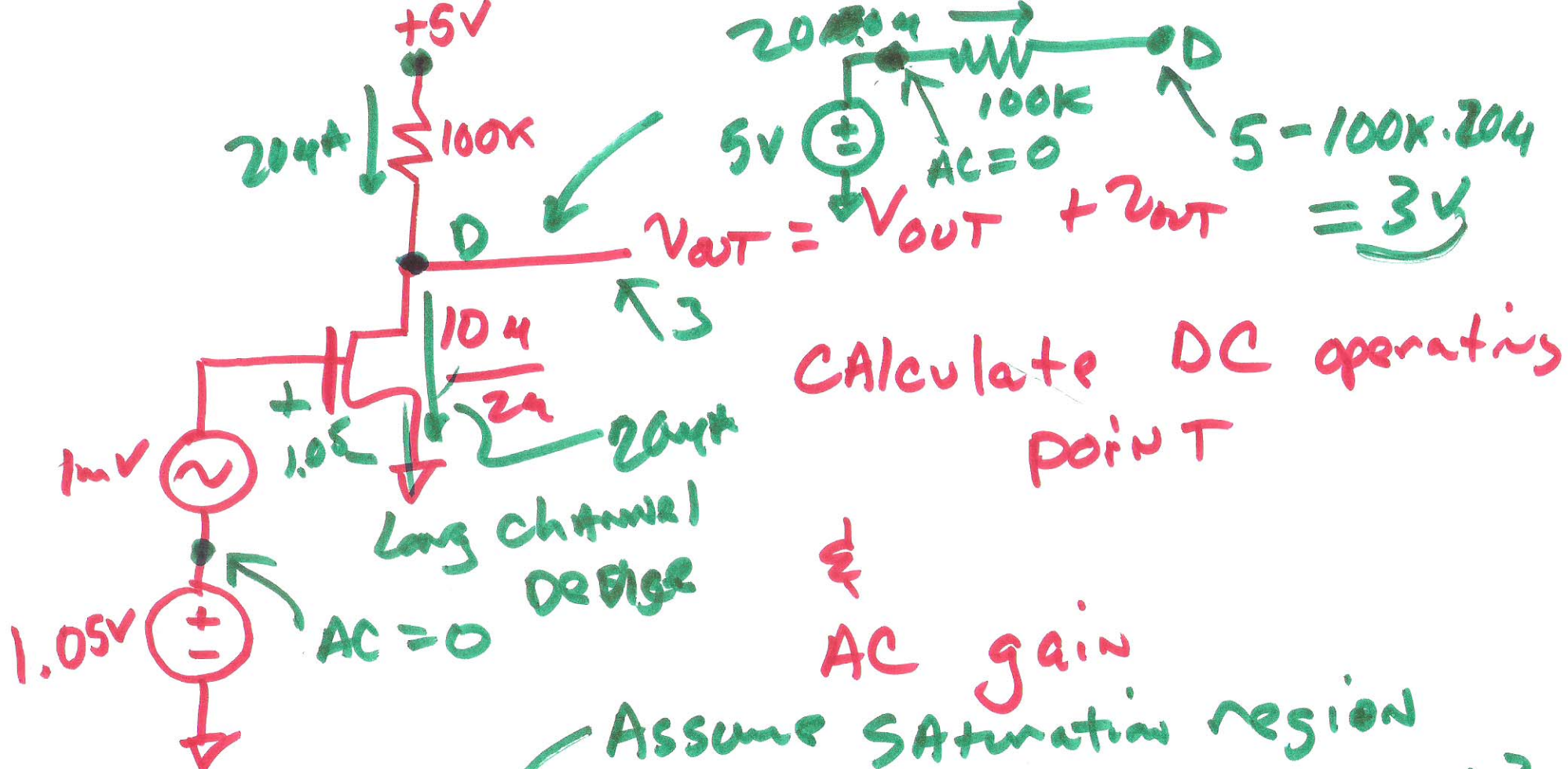
$$A = 1$$

$$V_{GS} - V_{THN} = \sqrt{\frac{2I_D}{\beta_n}}$$

$$g_m = \sqrt{2I_D \cdot \beta_n}$$

$$= \beta_n (V_{GS} - V_{THN})$$

4)



$204A$
 $5V$
 $100k$
 $AC=0$
 $V_{out} = V_{out} + 2uA = 3V$
 $5 - 100k \cdot 204 = 3V$

Calculate DC operating point

AC gain

Assume saturation region

$V_{DS} > V_{DS} - V_{th}$
 $3 > 1.05 - .8$
 IN SAT?
 YES!
 $I_D = \frac{1204A/\sqrt{2}}{2} \cdot \frac{10}{2} (1.05 - .8)^2$
 $= \frac{3004A}{\sqrt{2}} (.0625)$
 $= \underline{\underline{204A}}$

5)

AC CKT

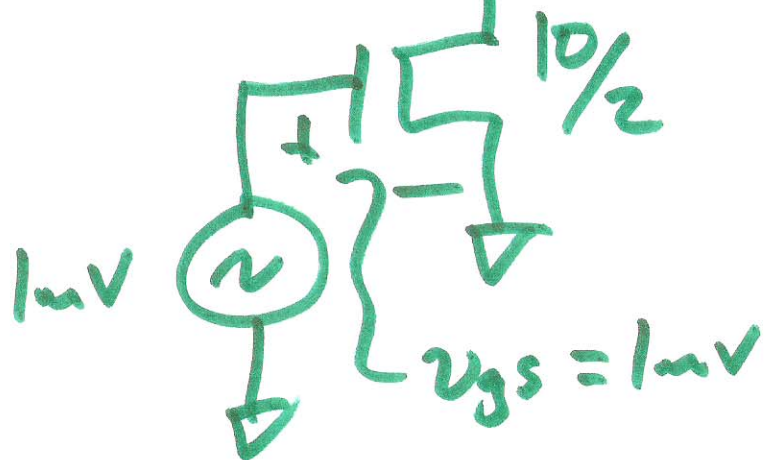
105



$$v_{nt} = -i_d \cdot 100k$$

$$i_d = g_m v_{gs}$$

$$= -i_d \cdot 100k = -150 \cdot 10^{-4}$$



$$v_{gs} = 1mV$$

$$i_d = 150 \mu A \cdot 1mV$$

$$i_d = 150 nA$$



$$g_m = \sqrt{2 \cdot k_p \cdot \frac{W}{L} I_D} = 150 \mu A/V$$

$$= k_p \cdot \frac{W}{L} (V_{GS} - V_{TH})$$

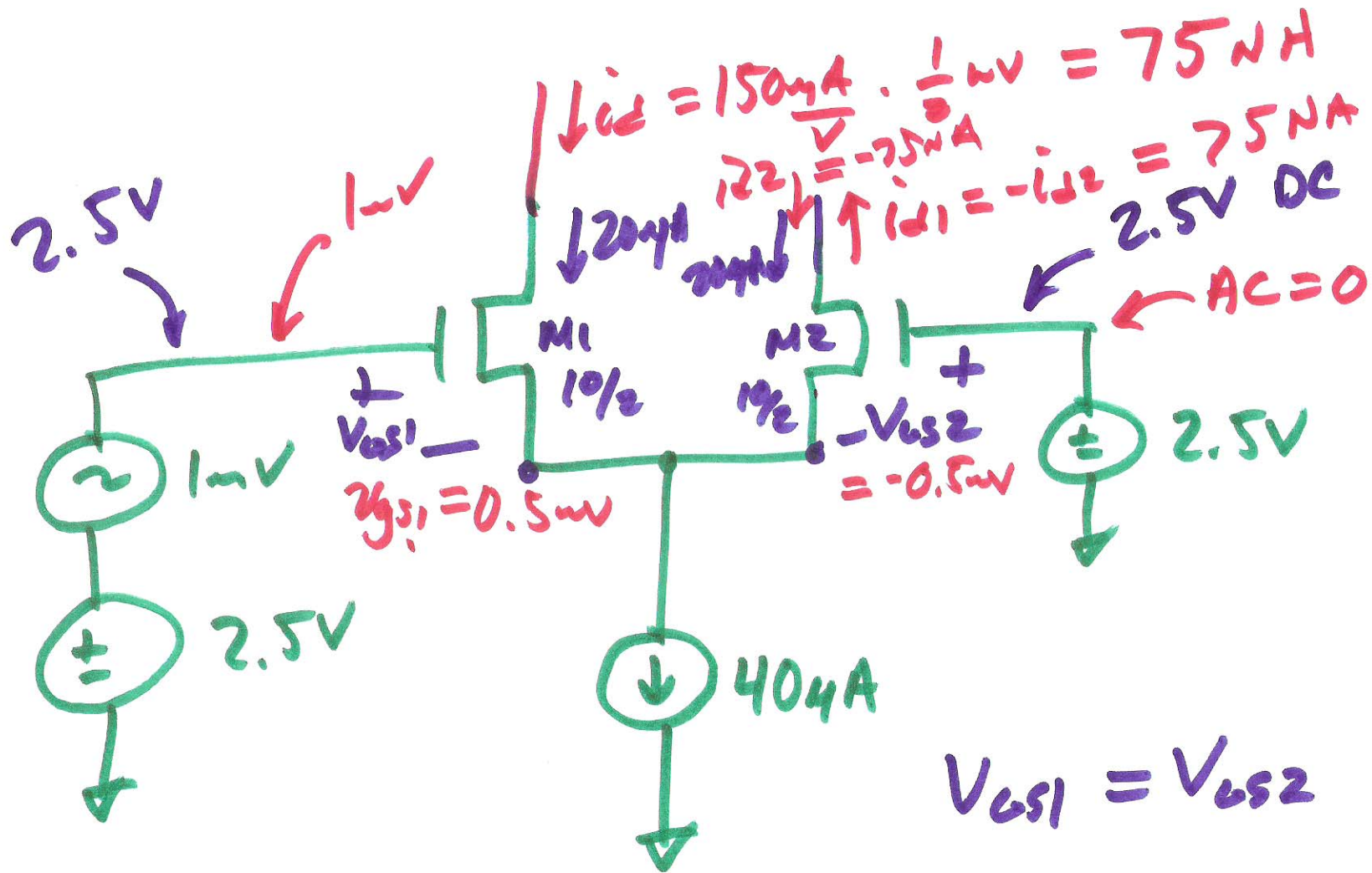
$$= \frac{120 \mu A}{\sqrt{2}} \cdot \frac{10}{2} \cdot (1.05 - 0.8)$$

$$= \frac{600 \mu A}{\sqrt{2}} \cdot 25V$$

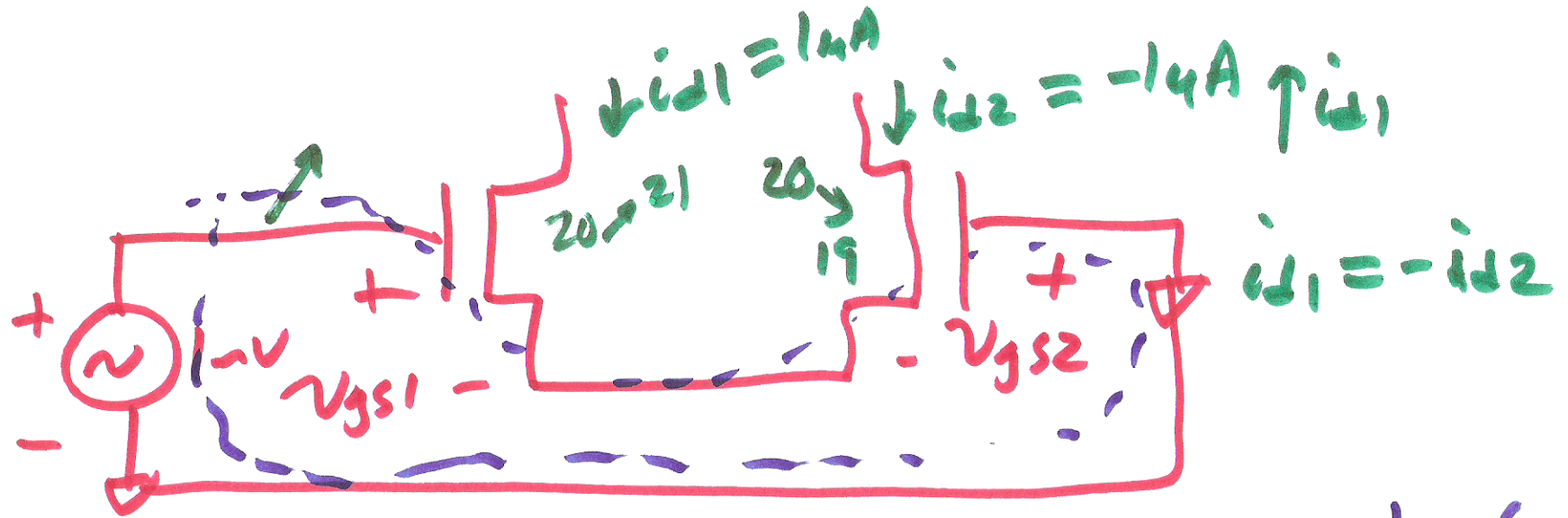
$$A_v = \frac{15}{1} = 15$$

$$g_m = \frac{150 \mu A}{V}$$

6)



$$g_{m1} = g_{m2} = \sqrt{2\beta_n \cdot I_0} = \sqrt{2 \cdot \frac{120\mu A}{V} \cdot \frac{10 \cdot 20\mu A}{2}} = 150\frac{\mu A}{V}$$



$$1\text{mV} - V_{gs1} + V_{gs2} = 0, V_{gs1} = \frac{1}{2}\text{mV}$$

$$V_{gs1} - V_{gs2} = 1\text{mV} \quad V_{gs2} = -\frac{1}{2}\text{mV}$$

$$i_{d1} = g_{m1} \cdot V_{gs1}$$

$$i_{d2} = g_{m2} \cdot V_{gs2}$$

$$g_{m1} = g_{m2}$$

$$i_{d1} = -i_{d2}$$

$$V_{gs1} = -V_{gs2}$$